# AMPLIFIER CIRCUITS 

Brian Moore<br>and John Donaghy

# OPERATIONAL AMPLIFIER CIRCUITS 

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## CONTENTS

PREFACE ..... viii
INTRODUCTION ..... ix
Chapter 1
INVERTING AND NON-INVERTING AMPLIFIERS
1.1 Characteristics of an ideal operational amplifier ..... 1
1.2 Definitions ..... 2
1.3 Circuit symbols for differential operational amplifiers ..... 4
1.4 Basic practical operational amplifier configurations: the inverting amplifier ..... 5
1.5 Review of ideal inverting operational amplifier characteristics ..... 6
1.6 Ideal non-inverting amplifier ..... 7
1.7 Summary of some practical operational amplifier parameters ..... 11
1.8 Differential amplifier circuits using operational amplifiers ..... 11
1.9 Summing inverter ..... 12
1.10 The real operational amplifier (introduction) ..... 14
1.11 Additional operational amplifier configurations ..... 14
1.12 Worked examples on multi-input configurations ..... 16
1.13 Practical operational amplifier packages ..... 20
1.14 Important review points ..... 21
1.15 Superposition theorem ..... 26
1.16 Nodal analysis ..... 28
1.17 Additional examples ..... 31
Chapter 2
FREQUENCY RESPONSE, SLEW RATE AND BAND WIDTH
2.1 Frequency response of the operational amplifier (introduction) ..... 33
2.2 Operational amplifier: input signal variations (introduction) ..... 35
2.3 Bode approximations (introduction) ..... 36
2.4 Bode approximation: multistage amplifier ..... 38
2.5 Rise time ..... 38
2.6 Small signal bandwidth ..... 39
2.7 Open loop/closed loop relationship for non-inverting amplifier circuits ..... 40
2.8 Slew rate ..... 42
2.9 Slew rate limiting of sine waves ..... 43
2.10 Full power bandwidth (large signal bandwidth) ..... 44
2.11 Slew rate limiting of square wave input ..... 45
2.12 Slew rate limiting of triangular wave input ..... 45
2.13 Worked examples ..... 46
2.14 Important review points ..... 47
2.15 Problems for readers ..... 49
Chapter 3
WAVEFORM GENERATORS
3.1 Introduction ..... 51
3.2 Square wave generator ..... 51
3.3 Basic principles of a bistable npn transistor multivibrator ..... 51
3.4 Operational amplifier as a free-running symmetrical multivibrator ..... 53
3.5 Ramp-generator theory ..... 58
3.6 Basic triangular wave generator circuit ..... 59
3.7 Triangular wave generator circuit ..... 59
3.8 Sawtooth wave generator ..... 61
3.9 Introduction to sine wave generators (oscillators) ..... 62
3.10 Oscillators ..... 63
3.11 Wien bridge oscillator ..... 65
3.12 Additional worked examples ..... 65
3.13 Important review points ..... 71
3.14 Problems for readers ..... 73
Chapter 4
POWER AMPLIFIERS AND POWER SUPPLIES
4.1 Amplifier classification (introduction) ..... 76
4.2 Ideal Class A direct-coupled stage ..... 76
4.3 Ideal Class A transformer-coupled output stage ..... 78
4.4 Ideal Class B transformer-coupled output stage ..... 79
4.5 Push-pull Class B power amplifier ..... 79
4.6 Crossover distortion ..... 81
4.7 Transistor power relationships for ideal push-pull amplifier circuit ..... 84
4.8 Disadvantages of a transformer as a phase splitter ..... 84
4.9 Complementary symmetry amplifier ..... 84
4.10 Development of a power amplifier using an operational amplifier ..... 85
4.11 Bridge amplifiers ..... 87
4.12 Integrated circuit power amplifiers ..... 90
4.13 Discrete power output stage ..... 91
4.14 Bridge amplifier circuit incorporating IC power amplifiers ..... 92
4.15 Basic heat sink theory ..... 93
4.16 Heat flow model ..... 94
4.17 Introduction to regulators ..... 96
4.18 Basic discrete series regulator circuit ..... 96
4.19 Basic regulator with increased loop gain ..... 97
4.20 Regulators producing output voltages lower than the internal reference element ..... 99
4.21 Pre-regulation ..... 100
4.22 Current limiting circuit ..... 102
4.23 Integrated circuit regulators ..... 102
4.24 Three terminal regulators ..... 103
4.25 Integrated circuit series voltage regulator ..... 103
4.26 Important review points ..... 105
4.27 Problems for readers ..... 108
Chapter 5
SELECTED APPLICATIONS OF OPERATIONALAMPLIFIERS
5.1 Introduction ..... 110
5.2 Audio circuits ..... 111
5.3 Precision rectifiers ..... 111
5.4 High impedance DC voltmeter ..... 112
5.5 Application in medical electronic monitoring systems ..... 113
5.6 Measurement of incident radiation using a photodiode ..... 114
5.7 Full wave ideal rectifier ..... 115
5.8 Peak detector ..... 116
5.9 Variable gain AC amplifier ..... 117
5.10 Differential light intensity circuit ..... 118
5.11 Filter applications ..... 119
5.12 Linear read-out amplifier for resistive bridge circuit ..... 120
5.13 Miscellaneous circuit functions of operational amplifiers ..... 121
5.14 Additional worked examples ..... 124
INDEX ..... 133

## PREFACE

This handbook provides a single source of information covering the basic principles of operational amplifier circuits. It will interest both the new and the experienced user of operational amplifiers.

We assume that readers possess a basic knowledge of simple electrical networks and of how transistors operate, but that they have no particular knowledge of operational amplifiers.

In some cases, circuit diagrams and symbol allocations are slightly unconventional. This is a deliberate attempt to simplify the information for the reader. In order to make some circuit diagrams clearer, supply connections have not always been shown.

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Brian Moore<br>John Donaghy<br>September 1985

## INTRODUCTION

The initial concept of the operational amplifier comes from the field of analogue computers. The term operational amplifier now applies to a very high gain, differential input, direct coupled amplifier whose operating characteristics are determined by external feedback elements. By altering the nature of the feedback elements, different analogue operations can be achieved. The important point is that the overall circuit characteristics are, for the majority of practical purposes, determined only by these feedback elements.

Widespread use of integrated circuit operational amplifiers did not really commence until the 1960s. However, within a few years, they have become a standard design tool for applications far beyond the original scope of analogue computer circuits.

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## Chapter 1

## INVERTING AND NON-INVERTING AMPLIFIERS

### 1.1 Characteristics of an ideal operational amplifier

The best approach to understanding the ideal operational amplifier is to consider the terminal characteristics of the amplifier in 'black box' form. The operational amplifier will be treated in this sense and, in general, what is inside the box will be disregarded.

It is convenient to assume that the amplifier has certain ideal characteristics. The effects of departures from the ideal exhibited by real operational amplifiers may then be expressed in terms of the errors to which they give rise. The ideal amplifier is assumed to have the following characteristics:
a The differential voltage gain is infinite $\left(\mathrm{A}_{\mathrm{V} 0}=\infty\right)$. This will, in general, make the performance entirely dependent on input and feedback networks.
b The input resistance is infinite $\left(r_{i n}=\infty\right)$. This will ensure that no current flows into the amplifier input terminals and the source network is not loaded.
c The output resistance is zero $\left(r_{o}=0\right)$. Ensures that the amplifier performance is not affected by the load.
d The bandwidth is infinite ( $\mathrm{BW}=x$ ). This is a bandwidth extending from zero to infinity, ensuring a response to DC signals and no phase change with frequency.
e When the input signal is zero the output signal will also be zero, ie $\mathrm{V}_{o}=$ 0 if $\mathrm{V}_{\text {in }}=0$.

Since the input impedance is infinite, there will be no current flowing into the amplifier input terminals. In addition, when negative feedback is employed, the differential input voltage reduces to zero. Proof of this is shown in Section 1.14A. These two statements are used as starting points for the analysis of negative feedback type amplifier circuits and will be explored in detail later on.

The equivalent circuit for an ideal operational amplifier (with $r_{i n}=\infty$ and $r_{o}=0$ ) is shown in Fig 1.1.


Fig. 1-1 Equivalent circuit for ideal operational amplifier

The amplifier responds only to the difference in voltage between the two input terminals. A positive-going signal at the inverting (-) input produces a negative-going signal component at the output, whereas the same signal at the non-inverting ( + ) input produces a positive-going output signal component. Essentially, the output signal is the combined response to such input signals. With an input voltage $\mathrm{V}_{\text {in }}$ the output voltage $\mathrm{V}_{0}$ will be $\mathrm{A}_{\mathrm{V} 0} \mathrm{~V}_{\mathrm{in}}$, where $\mathrm{A}_{\mathrm{V} 0}$ is the differential gain of the amplifier.

### 1.2 Definitions

The following definitions should be referred to when appropriate.

## - Differential amplifier

A differential amplifier is an amplifier designed to amplify the difference between two signals. Ideally:
$\mathrm{V}_{o}=\left(+\mathrm{A}_{d}\right) \mathrm{V}_{1}+\left(-\mathrm{A}_{d}\right) \mathrm{V}_{2}$ hence $\mathrm{V}_{o}=\mathrm{A}_{d}\left(\mathrm{~V}_{1}-\mathrm{V}_{2}\right)$ where $\mathrm{A}_{d}=$ differential gain.


Fig. 1-2 Differential input, single ended output

## - Differential input signal $\left(\mathbf{V}_{\boldsymbol{d}}\right)$

Referring to Fig 1.2, $\left|\mathrm{V}_{d}=\mathrm{V}_{1}-\mathrm{V}_{2}\right|$ or $\mid \mathrm{V}_{d}=\left(\mathrm{V}^{+}\right)-\left(\mathrm{V}^{-}\right)$iwhere $\left(\mathrm{V}^{+}\right)$ is the signal at the non-inverting input, relative to ground potential, and $\left(\mathrm{V}^{-}\right)$is that at the inverting input.

## - Common-mode input signal $\left(\mathbf{V}_{c}\right)$

$\mathrm{V}_{c}=1 / 2\left(\mathrm{~V}_{1}+\mathrm{V}_{2}\right)$, the average of the two input signals.

## - Differential gain

This is the ratio: $\frac{\text { output voltage }}{\text { differential input voltage }}$ when the common-mode input signal is zero.
Hence, $\quad \mathrm{A}_{d}=\frac{\mathrm{V}_{o}}{\mathrm{~V}_{d}}$ when $\mathrm{V}_{c}=0$, ie when $\left(\mathrm{V}_{1}=-\mathrm{V}_{2}\right)$

- Common-mode gain $\left(A_{c}\right)$
$A_{c}=\frac{\mathrm{V}_{o}}{\mathrm{~V}}$ when $\mathrm{V}_{d}=0$, ie when $\left(\mathrm{V}_{1}=\mathrm{V}_{2}\right)$


## - Common-mode rejection ratio (CMRR)

A real differential amplifier responds not only to the difference between the input signals, but also to their average. The CMRR indicates how much better the differential amplifier is at amplifying differential signals than common-mode signals. That is, the CMRR is a figure of merit for the differential amplifier. The CMRR should be high, so that:
$\mathrm{V}_{o}=\mathrm{A}_{d} \mathrm{~V}_{d}+\mathrm{A}_{c} \mathrm{~V}_{c} \simeq \mathrm{~A}_{d} \mathrm{~V}_{d}$ for many practical applications.

$$
\begin{aligned}
\mathrm{CMRR} & =\left|\frac{\mathrm{A}_{d}}{\mathrm{~A}_{c}}\right| \\
\mathrm{CMRR}(\mathrm{~dB}) & =20 \log _{10}\left|\frac{\mathrm{~A}_{d}}{\mathrm{~A}_{c}}\right| \\
& =\mathrm{A}_{d}(\mathrm{~dB})-\mathrm{A}_{c}(\mathrm{~dB})
\end{aligned}
$$

### 1.3 Circuit symbols for differential operational amplifiers

There are three main varieties of single-ended and differential connections, as shown in Fig 1.3.


Fig. 1-3 Circuit symbols for operational amplifiers

### 1.4 Basic practical operational amplifier configurations: the inverting amplifier

Operational amplifiers can be connected in two basic amplifying configurations:

- Inverting
- Non-inverting

The circuit of Fig 1.4 is one of the most widely used operational amplifier circuits. It is an amplifier whose closed-loop gain (gain of amplifier with feedback) from $V_{i n}$ to $V_{o}$ is set by $R_{1}$ and $\mathrm{R}_{2}$. It can amplify AC or DC signals. To understand how this circuit operates under ideal conditions, we use the two assumptions referred to in Section 1.1:
a The voltage $\mathrm{V}_{d}$ between $(+)$ and ( - ) inputs tends to 0 , as $\mathrm{A}_{d} \rightarrow \infty$ (from definition 1.2(a)).
b The current drawn by both the $(+)$ and the $(-)$ input terminals is zero.


Fig 1-4 Ideal inverting operational amplifier configuration

It is worth pointing out that this circuit only functions properly when the junction of the two resistors $\mathrm{R}_{1}$ and $\mathrm{R}_{2}$ goes to the ( - ) or inverting input of the amplifier. This provides negative feedback, and only negative feedback gives a 'stable amplifier'.

### 1.5 Review of ideal inverting operational amplifier characteristics

a Since the ideal operational amplifier has infinite gain, it can develop a finite output voltage, $\mathrm{V}_{o}$, with zero differential input voltage, $\mathrm{V}_{d}$ (Fig 1.4).
b The summing point is a virtual ground at the same potential as the ( + ) input. $\left(\mathrm{V}_{d}=0, \mathrm{~V}^{+}=0\right.$, hence $\left.\mathrm{V}^{-}=0\right)$.
c The differential input to $\mathrm{N}_{1}$ is $\mathrm{V}_{d}=0$. If $\mathrm{V}_{d}$ is zero, then the full input voltage, $\mathrm{V}_{i n}$, must appear across $\mathrm{R}_{2}$, because $\mathrm{V}^{-}=0$, making the current in $\mathrm{R}_{2}$ :
$i_{i n}=\frac{\mathrm{V}_{\text {in }}}{\mathrm{R}_{2}}$.
d Since $i_{s}=0$ due to infinite input impedance, the input current $i_{i n}$ must also flow in $\mathrm{R}_{1}$ (Kirchhoff's Current Law), thus
$i_{f}=i_{i n}$.
e The voltage across $\mathrm{R}_{1}$ is $i_{f} \mathrm{R}_{1}$, and since $\mathrm{V}^{-}=0$ this implies that $\mathrm{V}_{o}=$ $-i_{f} \mathrm{R}_{1}=-i_{i n} \mathrm{R}_{1}=-\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}} \cdot \mathrm{~V}_{i n}$

The minus sign implies a $180^{\circ}$ phase relationship with the input signal, ie inversion.

This is the characteristic voltage gain transfer function of the ideal inverting amplifier.
$f$ The closed loop voltage gain of the amplifier
$\mathrm{A}_{\mathrm{CL}}=\frac{\mathrm{V}_{o}}{\mathrm{~V}_{\text {in }}}=-\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\left(\right.$ Note the gain is strictly $\left.\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}.\right)$
$g$ The load current, $i_{\mathrm{L}}$, flows through $\mathrm{R}_{\mathrm{L}}$.
Thus $i_{\mathrm{L}}=-\frac{\mathrm{V}_{o}}{\mathrm{R}_{\mathrm{L}}}$
The operational amplifier output current, $i_{o}$, is: $i_{o}=i_{i n}+i_{\mathrm{L}}$
$h$ The input resistance seen by the input signal $\mathrm{V}_{\text {in }}$ is $\mathrm{R}_{2}$ since $\left(\mathrm{V}^{-}\right)$is at zero potential.

## Example 1

Given that:

$$
\begin{aligned}
\mathrm{R}_{2} & =15 \mathrm{k} \\
\mathrm{R}_{1} & =150 \mathrm{k} \\
\mathrm{~V}_{\mathrm{in}} & =1 \mathrm{~V} \\
\mathrm{R}_{\mathrm{L}} & =10 \mathrm{k}
\end{aligned}
$$

Refer to Fig 1.5 and determine:

| a | $i_{\text {in }}$ |
| :--- | :--- |
| b | $\mathrm{A}_{\mathrm{CL}}$ |
| c | $\mathrm{V}_{o}$ |
| d | $i_{o}$ |



Fig $1-5$

## Solution

a $i_{\text {in }}=\frac{\mathrm{V}_{\text {in }}}{\mathrm{R}_{2}}=\frac{1}{15 \mathrm{k}}=0.07 \mathrm{~mA}$
b $\quad \mathrm{A}_{\mathrm{CL}}=-\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}=-\frac{150 \mathrm{k}}{15 \mathrm{k}}=-10$
c $\frac{\mathrm{V}_{o}}{\mathrm{~V}_{\text {in }}}=-\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}$, so $\frac{\mathrm{V}_{o}}{\mathrm{IV}}=-\frac{150 \mathrm{k}}{15 \mathrm{k}}$ so $\mathrm{V}=-10 \mathrm{~V}$
d As $i_{o}=i_{i n}+i_{\mathrm{L}}$
where $i_{\mathrm{L}}=\frac{-\mathrm{V}_{o}}{\mathrm{R}_{\mathrm{L}}}=-\frac{(-10)}{10 \mathrm{k}}=1 \mathrm{~mA}$
Hence $i_{o}=0.07+1=1.07 \mathrm{~mA}$.

### 1.6 Ideal non-inverting amplifier

The second basic amplifying configuration of the operational amplifier is the non-inverting amplifier. Fig 1.6 shows a non-inverting amplifier circuit. The output voltage, $\mathrm{V}_{o}$, has the same phase (or polarity, in the case of DC signals) as the input voltage.

The input resistance of the practical non-inverting amplifier is very large, often over 100 M , and depends on the actual closed loop gain. This very high input resistance, compared to the inverting circuit, is often a reason for choosing this arrangement. An analysis follows:


Fig. 1-6 The non-inverting amplifier

$$
\begin{aligned}
& \begin{array}{l}
\mathrm{V}^{-}=\mathrm{V}^{+}=\mathrm{V}_{\text {in }}, \text { so } i=\frac{\mathrm{V}_{i n}}{\mathrm{R}_{2}} \\
\mathrm{~V}_{\mathrm{R}_{1}}
\end{array}=i \mathrm{R}_{1}=\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}} \cdot \mathrm{~V}_{i n} \\
& \mathrm{~V}_{o}
\end{aligned}=\mathrm{V}^{-}+\mathrm{V}_{\mathrm{R}_{1}}=\mathrm{V}_{\mathrm{m}}+\mathrm{V}_{\mathrm{R}_{1}} .
$$

Another method of proving this relationship is shown in Section 1.14B.

## Example 2

Determine, for the non-inverting amplifier shown in Fig 1.7,
a the output voltage
b the output current

## Solution

a Output voltage $\mathrm{V}_{o}=\left\{1+\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\right\} \mathrm{V}_{\text {in }}=\left\{1+\frac{20 \mathrm{k}}{5 \mathrm{k}}\right\}_{2}$
Hence: output voltage $=+10 \mathrm{~V}$
b $i=\frac{\mathrm{V}_{i n}}{\mathrm{R}_{\mathrm{L}}}=\frac{2}{5 \mathrm{k}}=0.4 \mathrm{~mA}$ and $i_{\mathrm{L}}=\frac{\mathrm{V}_{o}}{\mathrm{R}_{\mathrm{L}}}=\frac{10}{5 \mathrm{k}}=2 m \mathrm{~mA}$ Hence: output current $\mathrm{I}_{o}=0.4 \mathrm{~mA}+2 \mathrm{~mA}=2.4 \mathrm{~mA}$


Fig $1-7$

## Example 3



Fig 1.8

For the circuit shown in Fig 1.8, containing a real operational amplifier whose characteristics are given, determine the approximate value of the input signal current if $\mathrm{v}_{o}$ is 4 volts (rms).

Solution
$\mathrm{v}_{d}=\frac{\mathrm{v}_{o}}{\mathrm{~A}_{d}}=\frac{4}{200000}$ volts (rms) $=20 \mu \mathrm{~V}(\mathrm{rms})$
$i_{s}=\frac{\mathrm{v}_{d}}{\mathrm{R}_{\text {in }}}=\frac{20 \mu \mathrm{~V}}{2 \mathrm{M}}=10 \mathrm{pA} \quad(\mathrm{rms})$

## Example 4

If $\mathrm{v}_{o}$ is 8 V (pk-pk) at 2 kHz for the 0.2 V input shown in Fig 1.9, determine $\mathrm{R}_{1}, \mathrm{R}_{2}, \mathrm{v}_{d}$ and the voltage across $\mathrm{R}_{2}, \mathrm{v}_{\mathrm{R}_{2}}$, given that the total load placed on the operational amplifier by the feedback resistors is to be 20 k .


Fig $1-9$

## Solution

Gain, required $=\frac{8}{0 \cdot 2}=+40$
Hence: $\frac{\mathrm{R}_{1}+\mathrm{R}_{2}}{\mathrm{R}_{2}}=40$. But $\left(\mathrm{R}_{1}+\mathrm{R}_{2}\right)=20000$
so $\quad \frac{20000}{\mathrm{R}_{2}}=40$ or $=\mathrm{R}_{2}=500 \Omega$
Hence: $\quad R_{1}=20000-500=19500 \Omega$
$\mathrm{v}_{d}=\frac{\mathrm{v}_{o}}{\mathrm{~A}_{d}}=\frac{8}{80000}$ volts (pk-pk) $=100 \mu \mathrm{~V}(\mathrm{pk}-\mathrm{pk})$
$\mathrm{v}_{\mathrm{R}_{2}}=$ inverting input voltage $\bumpeq$ non-inverting voltage since
$\mathrm{v}_{d}$ is negligible at $100 \mu \mathrm{~V}$ by comparison with $\mathrm{v}_{s}$, which is 200 mV
Hence: $\mathrm{v}_{\mathrm{R}_{2}}=0.2 \mathrm{~V}$ or 200 mV (pk-pk)

### 1.7 Summary of some practical operational amplifier parameters

a The open loop voltage gain, $\mathrm{A}_{\mathrm{OL}}$, is the circuit's differential gain without feedback, ie as if the feedback path was made an open circuit. It follows then that $\mathrm{A}_{\mathrm{OL}}=\mathrm{A}_{d}$ and $\mathrm{V}_{o}=\mathrm{A}_{\mathrm{OL}} \mathrm{V}_{d}$.
$\mathrm{V}_{o}$ can never exceed positive or negative saturation voltages. For a $\pm 15 \mathrm{~V}$ supply, the saturation voltages would be about $\pm 13$ volts. Because output voltages, $\mathrm{V}_{o}$, equals the differential input voltage, $\mathrm{V}_{d}$, multiplied by open loop gain, $\mathrm{A}_{\mathrm{OL}}$, it can be seen that to produce saturation
$\mathrm{V}_{d}= \pm \frac{13}{200000}= \pm 65 \mu \mathrm{~V}$ (approx).
$\mathrm{V}_{d}$ should, however, be neglected only if it is very small compared to $\mathrm{V}_{s}$, the input signal voltage.
b Some typical parameters of a 741C operational amplifier are as follows:
i Input resistance $=2 \mathrm{M}$
ii Output resistance $=75$ ohm
iii $\mathrm{CMRR}=90 \mathrm{~dB}$
iv Large signal voltage gain $=200000$.

### 1.8 Differential amplifier circuits using operational amplifiers

Refer to Fig 1.10. It can be shown that:
Differential mode gain, $V_{1} \neq V_{2}: \frac{V_{o}}{V_{2}-V_{1}}=\frac{R_{1}}{R_{2}}$.

Note that the differential gain is defined solely by resistors $\mathrm{R}_{1}$ and $\mathrm{R}_{2}$. Proof of this is left for the reader. (The analysis is simplified if $R_{1}$ is assumed to be equal to $n R_{2}$.)


Fig. 1-10 Differential amplifier

### 1.9 Summing inverter

A summing inverter circuit is used for adding signals, eg as in an audiomixing circuit. An example of a basic summing inverter circuit is shown in Fig 1.11. This circuit $i_{i n}$ is the algebraic sum of the input currents.


Fig. 1-11 Summing inverter circuit
The ( - ) input is a virtual earth since ( + ) input is grounded and $v_{d}$ is approximately zero.
so

$$
i_{1}=\frac{\mathrm{v}_{1}}{\mathrm{R}_{1}}, i_{2}=\frac{\mathrm{v}_{2}}{\mathrm{R}_{2}}, i_{3}=\frac{\mathrm{v}_{3}}{\mathrm{R}_{3}}
$$

Hence: $i_{\text {in }}=i_{1}+i_{2}+i_{3}=i_{4}$, since $i_{s}$ is relatively small enough to be
neglected.
so

$$
\begin{aligned}
\mathrm{v}_{o} & =\mathrm{V}^{-}-i_{4} \mathrm{R}_{4} \\
& =-i_{4} \mathrm{R}_{4}\left(\text { since } \mathrm{V}^{-}=0\right) \\
& =-\left(i_{1}+i_{2}+i_{3}\right) \mathrm{R}_{4} \\
\mathrm{v}_{o} & =-\left(\mathrm{v}_{1} \frac{\mathrm{R}_{4}}{\mathrm{R}_{1}}+\mathrm{v}_{2} \frac{\mathrm{R}_{4}}{\mathrm{R}_{2}}+\mathrm{v}_{3} \frac{\mathrm{R}_{4}}{\mathrm{R}_{3}}\right)
\end{aligned}
$$

## Example 5

Refer to Fig 1.12.
a Determine the voltage gain applied to each input voltage.
b Calculate the output voltage using Fig 1.12.


Fig 1-12

## Solution

a i $\mathrm{A}_{\mathrm{CL} 1}=-\frac{\mathrm{R}_{4}}{\mathrm{R}_{1}}=-\frac{200 \mathrm{k}}{10 \mathrm{k}}=-20$
ii $\mathrm{A}_{\mathrm{CL} 2}=-\frac{\mathrm{R}_{4}}{\mathrm{R}_{2}}=-\frac{200 \mathrm{k}}{20 \mathrm{k}}=-10$
iii $A_{C L 3}=-\frac{R_{4}}{R_{3}}=-\frac{200 \mathrm{k}}{40 \mathrm{k}}=-5$

$$
\text { b } \begin{aligned}
\mathrm{V}_{o} & =-\left\{\mathrm{V}_{1} \frac{\mathrm{R}_{4}}{\mathrm{R}_{1}}+\mathrm{V}_{2} \frac{\mathrm{R}_{4}}{\mathrm{R}_{2}}+\mathrm{V}_{3} \frac{\mathrm{R}_{4}}{\mathrm{R}_{3}}\right\} \\
\mathrm{V}_{o} & =-[(0 \cdot 1 \times 20)+(0 \cdot 2 \times 10)+((-0 \cdot 1) \times 5)] \\
& =-(2+2-0 \cdot 5) \\
& \text { Hence: } \mathrm{V}_{o}=-3.5 \mathrm{~V}
\end{aligned}
$$

### 1.10 The real operational amplifier (introduction)

## - Input offset voltage

Ideal amplifiers produce 0 volts out for 0 volts in. However, in the practical case there may be a small DC voltage at the output even though no differential input voltage is applied.

The 'input offset voltage' may be considered as the DC input voltage which would produce the equivalent DC output voltage. The output voltage is actually caused by differences in the base-emitter junction voltages of the operational amplifier's input differential amplifier.

A related parameter to offset voltage is input offset voltage drift, ie variation in output voltage with temperature. Typical amplifiers usually possess drift levels in the range $5 \mu \mathrm{~V}$ to $40 \mu \mathrm{~V}$ per ${ }^{\circ} \mathrm{C}$. Low drift amplifiers are available with 10 times better performance.

## - Input bias current and input offset current

The input bias current is the average of the DC currents required by the amplifier to properly bias its first stage.
$I$ (bias) is defined as: $I_{B}=\frac{I_{1}+I_{2}}{2}$


Fig. 1-13 Input bias current

Input offset current is the small difference in bias currents from one input to the other of the operational amplifier. For many applications, input offset current may be ignored. It is only of significance when the output DC level must be accurately related to the input DC level.

## - AC parameters

Parameter definitions have previously been mainly concerned with magnitudes of DC voltages and currents. Several important AC or frequency dependent parameters will be discussed in chapter 2.

### 1.11 Additional operational amplifier configurations

## - The integrator

If a constant current is applied to the input of the integrator it causes the


Fig. 1-14 Basic integrator circuit
output voltage of the circuit to decrease linearly with time. The square wave input shown causes the direction of the input current to change sense regularly, resulting in an output voltage which increases, then decreases, linearly with time, ie a triangular waveform.

The output voltage is proportioned to the integral of the input voltage. $\mathrm{v}_{o}=-\frac{1}{\mathrm{CR}} \int \mathrm{v}_{\text {in }} \mathrm{dt}$.
See Proof in Section 1.14C.

## - The differentiator



Fig. 1-15 Basic differentiator circuit
The input current is proportional to the rate of change of input voltage with respect to time.

Operational Amplifier Circuits
$\mathrm{v}_{o}=-\mathrm{RC}\left(\frac{\mathrm{d}}{\mathrm{dt}} \cdot \mathrm{v}_{\text {in }}\right)$.
See Proof in Section 1.14D.

- The voltage follower


Fig. 1-16 Basic voltage follower circuit
Ideally:

$$
\begin{aligned}
\text { Gain } & =1 \\
\text { Input Resistance } & =\infty \\
\mathrm{v}_{o} & =\mathrm{v}_{i n}
\end{aligned}
$$

See Proof in Section 1.14E.

### 1.12 Worked examples on multi-input configurations

Example 6


Fig 1-17

Determine the input, $\mathrm{V}_{3}$, if the output voltage, $\mathrm{V}_{o}$, is zero for the circuit diagram shown in Fig 1.17.

## Solution

Current in $\mathrm{R}_{4}=\left(\frac{\mathrm{V}_{1}-\mathrm{V}^{-}}{\mathrm{R}_{1}}\right)+\left(\frac{\mathrm{V}_{2}-\mathrm{V}^{-}}{\mathrm{R}_{2}}\right)+\left(\frac{\mathrm{V}_{3}-\mathrm{V}^{-}}{\mathrm{R}_{3}}\right)$
If $\mathrm{V}_{o}$ is zero, then current in $\mathrm{R}_{4}$ must also be zero, since $\mathrm{V}^{-}=\mathrm{V}^{+}=0$
Hence: $\left(\frac{1-0}{10 \mathrm{k}}\right)+\left(\frac{-0 \cdot 5-0}{15 \mathrm{k}}\right)+\left(\frac{\mathrm{V}_{3}-0}{60 \mathrm{k}}\right)=0$

$$
=\frac{1}{10 \mathrm{k}}-\frac{0 \cdot 5}{15 \mathrm{k}}+\frac{\mathrm{V}_{3}}{60 \mathrm{k}}=0
$$

Multiplying throughout by $60 \mathrm{k}: 6-2+\mathrm{V}_{3}=0$
Hence: $\mathrm{V}_{3}=-4 \mathrm{~V}$

## Example 7

Determine $\mathrm{I}_{4}, \mathrm{I}_{0}$ and $\mathrm{I}_{\mathrm{L}}$ for the circuit shown in Fig 1.18.


Fig 1-18

## Solution

a

$$
\begin{aligned}
\mathrm{I}_{4} & =\text { sum of currents in } \mathrm{R}_{1}, \mathrm{R}_{2} \text { and } \mathrm{R}_{3} . \\
& =\left(\frac{\mathrm{V}_{1}-\mathrm{V}^{-}}{\mathrm{R}_{1}}\right)+\left(\frac{\mathrm{V}_{2}-\mathrm{V}^{-}}{\mathrm{R}_{2}}\right)+\left(\frac{\mathrm{V}_{3}-\mathrm{V}^{-}}{\mathrm{R}_{3}}\right)
\end{aligned}
$$

But $\mathrm{V}^{-}=\mathrm{V}^{+}=\mathrm{V}_{4}$ since negligible current will flow in $\mathrm{R}_{5}$

$$
\begin{aligned}
& \text { so } \quad I_{4}=\left(\frac{0 \cdot 1-1 \cdot 5}{10 \mathrm{k}}\right)+\left(\frac{0 \cdot 2-1 \cdot 5}{20 \mathrm{k}}\right)+\left(\frac{0 \cdot 8-1 \cdot 5}{40 \mathrm{k}}\right) \\
& =\left[\left(\frac{-1 \cdot 4}{10 \mathrm{k}}\right)+\left(\frac{-1 \cdot 3}{20 \mathrm{k}}\right)+\left(\frac{-0 \cdot 7}{40 \mathrm{k}}\right)\right] \\
& =(-0.14-0.065-0.0175) \\
& \text { Hence: } \mathrm{I}_{4}=-0.22 \mathrm{~mA} \\
& \text { b } \quad \mathrm{V}_{o}=\mathrm{V}^{-}-\mathrm{I}_{4} \mathrm{R}_{4}=1.5-(-0.2225 \times 30 \mathrm{k}) \\
& =1.5+6.675=8.175 \mathrm{~V} \text {. } \\
& \mathrm{I}_{\mathrm{L}}=\frac{\mathrm{V}_{o}}{\mathrm{R}_{\mathrm{L}}}=\frac{8.175}{15 \mathrm{k}} \\
& \text { Hence: } \mathrm{I}_{\mathrm{L}}=0.545 \mathrm{~mA} \\
& \text { c } \mathrm{I}_{o}=\mathrm{I}_{\mathrm{L}}-\mathrm{I}_{4}=0.545 \mathrm{~mA}-(-0.2225 \mathrm{~mA}) \\
& \text { Hence: } \mathrm{I}_{o}=0.77 \mathrm{~mA} \text {. }
\end{aligned}
$$

## Check



## Fig $1-19$

From Fig 1.19: $\mathrm{V}^{-}=\left(\mathrm{I}_{\mathrm{L}} \mathrm{R}_{\mathrm{L}}\right)+\left(\mathrm{I}_{4} \mathrm{R}_{4}\right)$

$$
\begin{aligned}
& =(0.545 \mathrm{~mA} \times 15 \mathrm{k})+(-0.2225 \mathrm{~mA} \times 30 \mathrm{k}) \\
& =8.175-6.675
\end{aligned}
$$

Hence: $\quad V^{-}=1.5$ volts, which is correct.

## Example 8

Calculate $\mathrm{V}_{o}$, the output voltage of the circuit shown in Fig 1.20.
See Section 1.15 (Superposition theorem).

## Solution

Using superposition theorem: $\mathrm{V}^{+}=\frac{\mathrm{V}_{1} \cdot \mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}+\frac{\mathrm{V}_{2} \cdot \mathrm{R}_{1}}{\mathrm{R}_{1}+\mathrm{R}_{2}}$, ie the sum of the inputs from each source considered separately,


Fig $\mathbf{1 - 2 0}$

$$
\begin{aligned}
& =\frac{(0.02 \times 40 \mathrm{k})}{100 \mathrm{k}}+\frac{(0.1 \times 60 \mathrm{k})}{100 \mathrm{k}} \\
& =0.008+0.06 \\
\mathrm{~V}^{+} & =0.068 \text { volt }
\end{aligned}
$$

Hence: $V^{-}=0.068$ volt
$\left(\frac{\mathrm{V}_{3}-\mathrm{V}^{-}}{\mathrm{R}_{3}}\right)+\left(\frac{0-\mathrm{V}^{-}}{\mathrm{R}_{4}}\right)+\left(\frac{\mathrm{V}_{o}-\mathrm{V}^{-}}{\mathrm{R}_{5}}\right)=0$
$=\left(\frac{-0.2-0.068}{1 \mathrm{k}}\right)+\left(\frac{0-0.068}{4 \mathrm{k}}\right)+\left(\frac{\mathrm{V}_{o}-0.068}{20 \mathrm{k}}\right)=0$.
Multiplying by 1000 gives:
$-0.268-0.017+\frac{\mathrm{V}_{o}}{20}-0.0034=0$
$\frac{\mathrm{V}_{o}}{20}=0.0034+0.017+0.268=0.2884$
Hence: $\quad V_{o}=20 \times 0.2884=5.768 \mathrm{~V}$

## Check



Fig 1-21

From Fig 1.21: $\mathrm{V}^{-} \cdot\left(\frac{1}{\mathrm{R}_{3}}+\frac{1}{\mathrm{R}_{4}}+\frac{1}{\mathrm{R}_{5}}\right)=\left(\frac{\mathrm{V}_{3}}{\mathrm{R}_{3}}+\frac{0}{\mathrm{R}_{4}}+\frac{\mathrm{V}_{o}}{\mathrm{R}_{5}}\right)$ so $\mathrm{V}^{-} \cdot\left(\frac{1}{1 \mathrm{k}}+\frac{1}{4 \mathrm{k}}+\frac{1}{20 \mathrm{k}}\right)=\left(\frac{-0 \cdot 2}{1 \mathrm{k}}+\frac{5 \cdot 768}{20 \mathrm{k}}\right)$.
Multiplying by 1000 gives: $\mathrm{V}^{-} \cdot(1+0.25+0.05)=-0.2+0.2884$

$$
\mathrm{V}^{-}=\frac{0.0884}{1.3}
$$

Hence: $\mathrm{V}^{-}=0.068 \mathrm{~V}$ which is correct.

### 1.13 Practical operational amplifier packages

The LM741 series is a typical general purpose operational amplifier. Details of pin connections for two of its typical packages are shown in Fig 1.22. The exact meaning of some terminal connection applications will be explained in chapter 3 . Fig 1.23 indicates the pin connections for a practical inverting amplifier circuit based on the LM741C Operational Amplifier.



metal package
viewed from top (pins underneath)

Fig. 1-22 IC operational amplifier packages


Fig. 1-23 Connections for practical inverting amplifier circuit
The user of operational amplifiers does not require a detailed knowledge of their internal circuitry, but is mainly concerned with the external pin connections.

There is a degree of standardisation in the pin connections with some general purpose operational amplifiers.

### 1.14 Important review points

## A Proof of conditions for $\mathbf{v}_{\boldsymbol{d}}$ to be effectively zero in negative feedback non-inverting amplifier circuits

From Section 1.1.
With an ideal operational amplifier and negative feedback $\mathrm{v}_{\boldsymbol{d}}$ is zero, whereas with a practical operational amplifier and negative feedback, it is normally very close to zero.

Refer to Fig 1.24. Assume the operational amplifier has finite $A_{v o}$ and $\mathrm{R}_{\text {in }}$, and zero $\mathrm{R}_{o}$.

Note that the feedback is negative because the signal at the inverting input substracts from that at non-inverting input, as far as its effect on the output is concerned, and is derived from $\mathrm{v}_{o}$, which is in phase with $\mathrm{v}_{i n}$. $\mathrm{v}_{d}=\mathrm{v}_{\text {in }}-\mathrm{Bv}_{o}$ where B is the transfer function of the feedback network.
That is, $\mathrm{v}_{d}=\mathrm{v}_{\text {in }}-\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \mathrm{v}_{o}$.
But $\quad v_{o}=\mathrm{A}_{V o} \mathrm{v}_{d}$.
Hence: $\mathrm{v}_{d}=\mathrm{v}_{\text {in }}-\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \mathrm{A}_{V o} \mathrm{v}_{d}$.


Fig 1-24
$\mathrm{v}_{d}+\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \mathrm{A}_{V o} \mathrm{v}_{d}=\mathrm{v}_{\text {in }}$
$v_{d}\left(1+\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \mathrm{A}_{V o}=\mathrm{v}_{i n}$
Hence: $\mathrm{v}_{d}=\frac{\mathrm{v}_{i n}}{1+\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \mathrm{A}_{V o}}$
So $\mathrm{v}_{d} \rightarrow 0$ as $\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \mathrm{A}_{V o} \rightarrow \infty$.
But $\frac{\mathrm{R}_{1}+\mathrm{R}_{2}}{\mathrm{R}_{2}}=$ closed loop gain. So we need: $\frac{\text { open loop gain }}{\text { closed loop gain }} \rightarrow \infty$, that is, open gain $\gg$ closed loop gain.

The small size of $v_{d}$ is of no significance unless it can be shown that it may be neglected by comparison with related signal levels, mainly the input, $\mathrm{v}_{\text {in }}$ or $\mathrm{v}_{s}$ (Fig 1.25).


Fig. 1-25 Block diagram of feedback system

To make a more general analysis ' S ' is used to represent a signal level which may either be a voltage, or a current level. ' A ' is the amplifier gain and ' B ' the 'gain' of the feedback network.

$$
\text { Hence: } \begin{aligned}
\mathrm{S}_{i} & =\mathrm{S}_{s}+\mathrm{BS}_{o} \\
\mathrm{~S}_{o} & =\mathrm{AS}_{i} \\
\mathrm{~S}_{i} & =\mathrm{S}_{s}+\mathrm{ABS}_{i} \\
\mathrm{~S}_{i}-\mathrm{ABS}_{i} & =\mathrm{S}_{s} \\
\mathrm{~S}_{i}(1-\mathrm{AB}) & =\mathrm{S}_{s} \\
\mathrm{~S}_{i} & =\frac{\mathrm{S}_{s}}{(1-\mathrm{AB})}
\end{aligned}
$$

Hence: $\mathrm{S}_{i} \rightarrow 0$ as $-\mathrm{AB} \rightarrow \infty$
Thus loop gain, AB , needs to have an associated phase shift of $180^{\circ}$, (ie negative feedback) and be very large in comparison with unity, for $S_{i}$ to approach zero. Under such circumstances, $S_{i}$ becomes very much smaller than $S_{s}$ and may be neglected in comparison with it.

## B Proof of $\mathbf{A}_{\mathbf{c L}}$ for non-inverting amplifier (alternate method)

From Section 1.6. Refer to Fig 1.26.


Fig $\mathbf{1 - 2 6}$
$\mathrm{V}^{-}=\mathrm{V}^{+}=\mathrm{v}_{\text {in }}$
But $\quad \mathrm{V}^{-}=\mathrm{v}_{o}\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \quad \begin{aligned} & \text { by potential divider formula (amplifier } \\ & \text { input current being zero) }\end{aligned}$
so $\quad \mathrm{v}_{\text {in }}=\mathrm{v}_{o}\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right)$
Hence:

$$
\begin{aligned}
\mathrm{v}_{o} & =\left(\frac{\mathrm{R}_{1}+\mathrm{R}_{2}}{\mathrm{R}_{2}}\right) \mathrm{v}_{i n} \\
\text { so, } \quad \mathrm{v}_{o} & =\left(1+\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\right) \mathrm{v}_{i n}
\end{aligned}
$$

and $\quad \mathrm{A}_{\mathrm{CL}}=\left(1+\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\right)$,
where $\mathrm{A}_{\mathrm{CL}}=\frac{\mathrm{v}_{o}}{\mathrm{v}_{\text {in }}}$
C Proof of the integrator relationship: $\mathrm{v}_{0}=-\frac{1}{C R} \int \mathrm{v}_{\text {/n }} \mathrm{dt}$
From Section 1.11. Refer to Fig 1.27.


Fig 1 -27

The inverting input of the operational amplifier will remain close to ground potential due to the high open loop gain of the amplifier.

The voltage across the capacitor, $\mathrm{v}_{c}$, is given by:

$$
\mathrm{v}_{c}=\frac{1}{C} . \quad \mathrm{Q} \text { where } \mathrm{Q} \text { is the instantaneous value of the charge on the }
$$

Now $\mathrm{Q}=\int_{t_{1}}^{t_{2}} i \mathrm{dt}$
so $\quad \mathrm{v}_{c}=\frac{1}{C} \int_{t_{1}}^{t_{2}} i \mathrm{dt}$
Now $i=\frac{\mathbf{v}_{\text {in }}}{\mathrm{R}}$ if inverting input is near ground potential
so $\quad \mathrm{v}_{c}=\frac{1}{\mathrm{CR}} \int_{t_{1}}^{t_{2}} \mathrm{v}_{i n} \mathrm{dt}$
now $\mathrm{v}_{o}=0-\mathrm{V}_{\mathrm{c}}$
so

$$
\mathrm{v}_{o}=-\frac{1}{\mathrm{CR}} \int_{t_{1}}^{t_{2}} \mathrm{v}_{\text {in }} \mathrm{dt}
$$

That is, the output voltage of the circuit is the integral of $v_{\text {in }}$ over the time interval $t_{1}$ to $t_{2}$ seconds, with a constant of proportionality equal to $-\frac{1}{\mathrm{CR}}$.

## - The differentiator relationship

D Proof $v_{o}=-R C\left(\frac{d}{d t} \cdot v_{i n}\right)$
Refer to Section 1.11. Refer to Fig 1.28.


Fig 1-28
$\mathrm{Q}=\mathrm{Cv}_{i n}$, so $\Delta \mathrm{Q}=\mathrm{C} \Delta \mathrm{v}_{i n}$,
ie $\quad \int i_{i n} \mathrm{dt}=\mathrm{Cdv}_{\text {in }}$
or

$$
i_{i n}=\mathrm{C} \frac{\mathrm{dv}_{i n}}{\mathrm{dt}}
$$

and since $i_{i n}$ also equals current through R and $\mathrm{V}^{-}$will stay close to ground potential due to the high value of $\mathrm{A}_{V o}$, it follows that:
$\mathrm{v}_{o}=-i_{i n} \mathrm{R}$ since $\mathrm{V}^{-}$is approximately zero.
Hence: $-\frac{\mathrm{v}_{o}}{\mathrm{R}}=i_{i n}=\mathrm{C}\left(\frac{\mathrm{d}}{\mathrm{dt}} \cdot \mathrm{v}_{i n}\right)$
so

$$
\mathrm{v}_{o}=-\mathrm{RC}\left(\frac{\mathrm{~d}}{\mathrm{dt}} \cdot \mathrm{v}_{i n}\right)
$$

That is, $\mathrm{v}_{o}$ is proportional to the time derivative of $\mathrm{v}_{i n}$ with a proportionality constant equal to -RC .

## E Proof that the voltage follower circuit has a gain of unity

From Section 1.11. Refer to Fig 1.29.
$\mathrm{V}^{-}=\mathrm{V}^{+}=\mathrm{v}_{\text {in }}$
But $\mathrm{V}^{-}$also $=\mathrm{v}_{o}$, hence $\mathrm{v}_{o}=\mathrm{v}_{\text {in }}$.
An alternative method would be as follows (from Fig 1.30):
Considering the non-inverting amplifier circuit, the voltage gain
$\frac{\mathrm{v}_{o}}{\mathrm{v}_{\text {in }}}=1+\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}$


Fig 1-29


Fig 1-30

In the voltage follower circuit $\mathrm{R}_{1}=0$ and $\mathrm{R}_{2}=\infty$.
Hence: gain $=1$,
ie the voltage follower circuit is a special case of the non-inverting amplifier circuit.

### 1.15 Superposition theorem

a In any network containing more than one source (voltage and/or current) the current in, or the potential difference across any branch can be found by considering the effect of each source separately at the appropriate point, and adding the effects.
b Sources of emf not under consideration are replaced by short circuits, while current sources are replaced by open circuits; any internal resistances being left in circuit.

## Example 9

Determine the current in $\mathrm{R}_{2}$ of the circuit shown in Fig 1.31 by using the Superposition Theorem.


Fig 1-31

## Solution

Consider the effect of the current source alone as shown in Fig 1.32.


Fig 1-32
$\mathrm{R}_{1}$ is in parallel with $\mathrm{R}_{3}=10 \Omega \| 30 \Omega=7 \cdot 5 \Omega$
Hence: $\mathrm{I}_{1}=\left(\frac{7 \cdot 5}{7 \cdot 5+20}\right) 1 \mathrm{~A}=0.273 \mathrm{~A}$
Considering the effect of the voltage source alone, as shown in Fig 1.33:


Fig 1-33
$\mathrm{R}_{1}$ is in parallel with $\mathrm{R}_{2}=10 \Omega \| 20 \Omega=6.67 \Omega$
Hence: $I_{3}=\frac{20}{6.67+30}=0.545 \mathrm{~A}$
Hence: $I_{2}=\left(\frac{10}{10+20}\right) 0.545=0.182 \mathrm{~A}$.
The current in $R_{2}$ is the combined value of the currents produced by the current and the voltage source, ie the current in $R_{2}=I_{1}$ (from current source) $+\mathrm{I}_{2}$ (from voltage source) $=0.273 \mathrm{~A}+0.182 \mathrm{~A}=$ 0.455 A .

### 1.16 Nodal analysis

a Nodal analysis is a direct application of Kirchhoff's current law and is used to determine the voltage at nodes. Consider the circuit shown in Fig 1.34.


Fig 1. 34
b Kirchhoff's current law indicates that $I_{1}+I_{2}+I_{3}=0$. Now if the voltage at node $A$ is assumed to be $V$ volts, then the currents may be expressed in terms of the voltage drops across the resistors, giving:
$\frac{V-V_{1}}{R_{1}}+\frac{V-V_{2}}{R_{2}}+\frac{V+V_{3}}{R_{3}}=0$
c The currents do not have to be shown all proceeding away from the node. However, the advantage of this arrangement is that V always appears on the left hand side of the equation, making sign changes unnecessary. If the currents are shown going towards the node, V has a negative sign in the equation format.
d If the currents are as shown in Fig 1.35,
then: $I_{2}+I_{3}=I_{1}$
from Fig 1.35 it can be seen that:
$\frac{V_{2}-V}{R_{2}}+\frac{-V_{3}-V}{R_{3}}=\frac{V-V_{1}}{R_{1}}$
Note: This form of equation is disorderly, and so such a choice of current direction is inviting errors to be made.


Fig 1.35

## Example 10

With reference to the circuit network shown in Fig 1.36, determine:
a The voltage V at the node A relative to ground potential.
b The current in $\mathrm{R}_{2}$.


Fig 1.36

## Solution

a From Kirchhoff's current law, $\mathrm{I}_{1}+\mathrm{I}_{2}+\mathrm{I}_{3}=0$
so $\frac{V-V_{1}}{R_{1}}+\frac{V-0}{R_{2}}+\frac{V-\left(-V_{2}\right)}{R_{3}}=0$
Hence: $\frac{V-36}{18 k}+\frac{V}{100}+\frac{V-(-4)}{2 k}=0$
multiply throughout by 18 k
$V-36+180 V+9(V+4)=0$
$V-36+180 V+9 V+36=0$, hence $V=0$
b As the voltage at node $\mathrm{A}=0$, then the potential difference across $R_{2}=0$, hence the current in $R_{2}=0$.

## Example 11

With reference to the circuit shown in Fig 1.37, determine the voltage V at node A relative to ground potential.


## Fig 1-37

## Solution

From Kirchhoff's current law, $\mathrm{I}_{1}+\mathrm{I}_{2}+\mathrm{I}_{3}=0$
thus $\frac{V-10}{100}+\frac{V-20}{200}+\frac{V-(-30)}{300}=0$
multiply throughout by 600
$6 \mathrm{~V}-60+3 \mathrm{~V}-60+2 \mathrm{~V}+60=0$
Hence: $V=5.45$ volts
Note: The equations shown in Example 11 may also be expressed in the form:
$\mathrm{V}\left[\frac{1}{\mathrm{R}_{1}}+\frac{1}{\mathrm{R}_{2}}+\frac{1}{\mathrm{R}_{3}}\right]=\frac{\mathrm{V}_{1}}{\mathrm{R}_{1}}+\frac{\mathrm{V}_{2}}{\mathrm{R}_{2}}+\frac{\mathrm{V}_{3}}{\mathrm{R}_{3}}$
thus $\quad V=\frac{V_{1} G_{1}+V_{2} G_{2}+V_{3} G_{3}}{G_{1}+G_{2}+G_{3}}$
where $G=\frac{1}{R}=$ the conductance, measured in siemens.

### 1.17 Additional examples

## Example 12

For the circuit, confirm that the output waveform is as shown in Fig 1.38.


Fig 1-38

## Example 13

For the circuit, confirm that the waveforms are as shown in Fig 1.39.


Fig 1-39

## Chapter 2

## FRECUENCY RESPONSE, SLEW RATE AND BANDWMDTH

### 2.1 Frequency response of the operational amplifier (introduction)

Many types of operational amplifiers are internally compensated by a small capacitor, eg about 30 pF (for a 741). The internal frequency compensation capacitor prevents the operational amplifier from oscillating with resistive feedback.

Oscillation is prevented by causing the gain of the operational amplifier to decrease at high frequencies. Otherwise there would be sufficient gain and phase shift to cause oscillations. (At a particular high frequency some in-phase signal is fed back to the input, from the output, through the ordinary feedback network.) This particular point is reviewed in more detail in Section 2.14A.

A typical frequency response curve is as shown in Fig 2.1. At low frequencies, the open loop voltage gain is very high, eg a 741 has a gain of about 200000 times or 106 dB .


Fig 2-1 Open-loop voltage gain versus frequency

Point B in Fig 2.1 indicates the upper break, or cut-off, frequency. At this point the voltage gain is 0.707 times the gain value at very low frequencies, and corresponds to a halving of power output to a constant load, for constant amplitude input signal.

Points C and D indicate how the gain decreases by a factor of 10 as frequency increases by a factor of 10 , for frequencies greater than about ten times, or one decade, above the breakpoint. Also, from Fig 2.1 it can be seen that the voltage gain decreases by 20 dB , ie ten times, for an increase in frequency of ten times (one decade). Hence, the frequency response from B to A is often described as rolling off at a rate approaching $20 \mathrm{~dB} /$ decade.

This is equivalent to saying that the gain falls at a rate inversely proportional to the increase in frequency: due to the decreasing reactance of the compensating capacitor referred to earlier.

Point A is the unity gain frequency, and the product of the frequency and gain there is known as the gain-bandwidth product of the amplifier, being $(1 \mathrm{MHz} \times 1)=1 \mathrm{MHz}$ for the operational amplifier shown.

It can be shown that in the
$20 \mathrm{~dB} /$ decade roll-off region, the open loop gain at frequency $f$

## Example 1

Determine the open-loop gain of an operational amplifier at a frequency of 20 kHz , if it has a unity gain bandwidth of 1.4 MHz .

## Solution

From:

$$
\begin{aligned}
\mathrm{A}_{\mathrm{OL}} & =\frac{\text { Bandwidth at unity gain }}{\text { frequency }} \\
& =\frac{1 \cdot 4 \mathrm{MHz}}{20 \mathrm{kHz}}
\end{aligned}
$$

Hence $\mathrm{A}_{\mathrm{OL}}=70$

When an operational amplifier is used as the basis of a negative feedback amplifier, then:
closed loop gain $\times$ bandwidth of amplifier $=$ open loop gain $\times$ bandwidth of operational amplifier ie gain bandwidth product remains constant.

### 2.2 Operational amplifier: input signal variations (introduction)

The operational amplifier's response depends on the rate of change of the input signals applied to it. It is usual to consider the effect of sinusoidal signals, which have no abrupt discontinuity in their waveform, and square wave signals which consist of a succession of abrupt changes in slope. It is also usual to distinguish between low amplitude output signals (below about 1 V peak) and large signals (above 1V peak). For small input, and hence output, signals noise is often the limiting factor for undistorted output; for large output signals, slewing rate is frequently the limiting factor.

The gain/frequency response for sinusoidal input signals is represented graphically by a plot of gain in decibels against a logarithmic frequency scale.
Strictly speaking,
gain in $\mathrm{dB}=10 \log _{10}\left(\frac{\mathrm{P}_{o}}{\mathrm{P}_{\text {in }}}\right)$
where $\mathrm{P}_{o}=$ output power and $\mathrm{P}_{i n}=$ input power.
From the above definition, dB gain $=10 \log _{10}\left(\frac{\mathrm{~V}_{o}{ }^{2} / \mathrm{R}_{\mathrm{L}}}{\mathrm{V}_{\text {in }}{ }^{2} / \mathrm{R}_{\text {in }}}\right)$

$$
=20 \log _{10}\left(\frac{\mathrm{~V}_{o}}{\mathrm{~V}_{\text {in }}} \cdot \frac{\mathrm{R}_{\text {in }}}{\mathrm{R}_{\mathrm{L}}}\right)
$$

Accepted usage is only strictly correct if $\mathrm{R}_{\text {in }}=\mathrm{R}_{\mathrm{L}}$. It is nevertheless a convenient method of expressing and comparing voltage gains, eg a gain of 1000000 is equivalent to 120 dB , whereas one of 500000 is 114 dB , ie 6 dB less.

## Example 2

Determine the voltage gain in dB :
a if $\frac{\mathrm{V}_{o}}{\mathrm{~V}_{\text {in }}}=10$, voltage gain in $\mathrm{dB}=20 \log _{10} 10=20 \mathrm{~dB}$
b if $\frac{\mathrm{V}_{o}}{\mathrm{~V}_{\text {in }}}=100$, voltage gain in $\mathrm{dB}=20 \log _{10} 100=40 \mathrm{~dB}$
c if $\frac{\mathrm{V}_{o}}{\mathrm{~V}_{\text {in }}}=\frac{1}{\sqrt{ } 2}$, voltage gain in $\mathrm{dB}=20 \log _{10} \frac{1}{\sqrt{ } 2}=-3 \mathrm{~dB}$.
Note, since power is proportional to $\mathrm{V}^{2}$, a decrease in gain of 3 dB represents a halving of the output power, whereas a decrease of 6 dB corresponds to a halving of the voltage gain and the reduction of output power to a quarter of its original value.

### 2.3 Bode approximations (introduction)

Gain/frequency plots are often approximated by a set of straight lines known as Bode plots. The significance of Bode plots can be determined by an analysis of Fig 2.2.


Fig 2-2 Bode approximation (gain/frequency)

In Fig 2.2 it is seen that the two straight Bode approximation lines intersect at $f_{c}$, and at this frequency the response is 3 dB down. The two straight lines are tangential to the true response at frequencies remote from the cut-off frequency, assuming the absence of other nearby breakpoints.

The corresponding phase/frequency characteristic is as shown in Fig 2.3. It can be seen that the Bode phase plot approximates the phase shift with limits of $0^{\circ}$ and $-90^{\circ}$ for frequencies a decade below and above $f_{c}$ respectively.

A single reactive component will introduce a slope approximating to a magnitude of $20 \mathrm{~dB} /$ decade into a frequency response. The slope will be positive or negative, depending upon whether the reactive component is capacitive or inductive and its location in the circuit.


Fig 2-3 Bode approximation (phase/frequency)

It can be shown that: $\theta=-\tan ^{-1} \frac{f}{f_{c}}$
for the type of frequency roll-off under discussion.
The Bode frequency plot is useful because, with practice, it enables a good theoretical approximation to the frequency response to be produced quite rapidly.

As far as the response under discussion is concerned:
a when $f \leqslant 0 \cdot 1 f_{c}$, the phase shift due to the breakpoint is effectively zero;
b when $f=f_{c}$, the phase shift is $-45^{\circ}$;
C when $f \geqslant 10 f_{c}$, the phase shift is approximately $-90^{\circ}$.
The reader should consult a suitable text for further details.

### 2.4 Bode approximation: multistage amplifier

Bode diagrams are most useful in determining the frequency response characteristics of cascaded gain stages.

The gain of a multistage amplifier is the product of the gains of individual stages. However, since gain is shown logarithmically in Bode plots, the overall Bode response is obtained by adding the responses of the separate stages.

Fig 2.4 illustrates the basic concepts of the production of a Bode plot for cascaded gain stages. The method is applicable to operational amplifier stages having responses similar in their general nature to that of compensated 741 type amplifiers.


Fig 2-4 Frequency response of cascaded gain stages

Bode diagrams are particularly useful in determining the stability and frequency response of feedback circuits. A frequency dependent response automatically implies that the amplifiers' gain and phase response will both change with frequency. Bode plots are further reviewed in Section 2.14B.

### 2.5 Rise time

Rise time is defined as the time required for the output voltage to rise from $10 \%$ of its final value to $90 \%$ of its final value in response to a step input.

This is illustrated in Fig 2.5, and proved in Section 2.14C.


Fig 2-5 Rise time illustration

For a 741 operational amplifier, or any circuit that has a simple -20 dB / decade roll-off above its upper cut-off frequency, it may be shown that upper cut-off frequency $=\frac{0 \cdot 35}{\text { rise time }}$.

This relationship is very useful as the basis of a practical method of determining the upper cut-off frequency of amplifier circuits. It is thus only necessary to examine the output response to a square wave input to be able to determine the upper cut-off frequency with adequate accuracy.

### 2.6 Small signal bandwidth

The useful frequency range or bandwidth of an amplifier is defined by an upper frequency limit, $f_{2}$, and a lower frequency limit, $f_{1}$ (or zero hertz where amplifier is DC coupled).

At $f_{1}$ and $f_{2}$ the voltage gain is 0.707 its maximum value in the middle of the useful frequency range. This concept is represented in Fig 2.6.


Fig 2-6 Small signal bandwidth

### 2.7 Open loop/closed loop relationship for non-inverting amplifier circuits

Let $\quad f_{2}=$ upper cut-off frequency.
$f_{2(\mathrm{OL})}=$ upper cut-off frequency of open loop circuit, ie without negative feedback.
$f_{2(\mathrm{CL})}=$ upper cut-off frequency with negative feedback.
It can be shown that:
closed loop Bandwidth, $f_{2(\mathrm{CL})}=f_{2(\mathrm{OL})} \times\left(\frac{\mathrm{A}_{\mathrm{OL}}}{\mathrm{A}_{\mathrm{CL}}}\right)$.
Let $\mathrm{R}_{o(\mathrm{OL})}=$ output resistance, under open loop conditions,
and $\quad \mathrm{R}_{o(\mathrm{CL})}=$ output resistance, under closed loop conditions.
It can be shown that:
$\mathrm{R}_{o(\mathrm{CL})}=\frac{\mathrm{R}_{o(\mathrm{OL})}}{\left(\frac{\mathrm{A}_{\mathrm{OL}}}{\mathrm{A}_{\mathrm{CL}}}\right)}$ and $\mathrm{R}_{i n(\mathrm{CL})}=\mathrm{R}_{i n(\mathrm{OL})}\left(\frac{\mathrm{A}_{\mathrm{OL}}}{\mathrm{A}_{\mathrm{CL}}}\right)$.
The useful relationships above are valid under conditions where the feedback is derived from the output voltage and fed back to the input as a voltage to be added antiphase to the input signal, ie a negative feedback voltage amplifier.

The inverting amplifier obeys the relationship $f_{2(\mathrm{CL})}=f_{2(\mathrm{OL})} \times\left(\frac{\mathbf{A}_{\mathrm{OL}}}{\mathbf{A}_{\mathrm{CL}}}\right)$ approximately, providing $\mathrm{A}_{\mathrm{OL}}$ and $\mathrm{A}_{\mathrm{CL}}$ are gain magnitudes and provided that $\mathrm{A}_{\mathrm{CL}}$ is $>$ about 10 . Strictly speaking $f_{2(\mathrm{CL})}=f_{2(\mathrm{OL})}\left(\frac{\mathrm{A}_{\mathrm{OL}}}{\mathrm{A}_{\mathrm{CL}}+1}\right)$. $\mathrm{R}_{o}$ is reduced to a low value and $\mathrm{R}_{i n}=\mathrm{R}_{i}$.

## Example 3

A non-inverting amplifier circuit has an open loop $\mathrm{R}_{o}$ of $75 \Omega$ and a -3 dB cut-off frequency at 12 Hz . With feedback, $\mathrm{R}_{o}$ decreases to $25 \mathrm{~m} \Omega$; determine the amplifier's -3 dB bandwidth.

## Solution

$$
\begin{aligned}
\mathrm{R}_{o(\mathrm{CL})} & =\frac{\mathrm{R}_{o(\mathrm{OL})}}{\frac{\mathrm{A}_{\mathrm{OL}}}{\mathrm{~A}_{\mathrm{CL}}}} \\
\text { ie } \quad \frac{\mathrm{A}_{\mathrm{OL}}}{\mathrm{~A}_{\mathrm{CL}}}=\frac{\mathrm{R}_{o(\mathrm{OL})}}{\mathrm{R}_{o(\mathrm{CL})}} & =\frac{75 \Omega}{25 \mathrm{~m} \Omega}=3000 \\
\text { Closed loop bandwidth } & =f_{2(\mathrm{OL})} \times\left(\frac{\mathrm{A}_{\mathrm{OL}}}{\mathrm{~A}_{\mathrm{CL}}}\right) \\
& =12 \times 3000=36 \mathrm{kHz}
\end{aligned}
$$

Hence: -3 dB bandwidth $=36 \mathrm{kHz}$.

## Example 4

An inverting amplifier at constant amplitude input signal delivers a constant output power to its load over the frequency range 10 Hz to 30 kHz . Above 30 kHz the output power gradually decreases until at 350 kHz , for the same input power, the output power is halved, relative to that obtained at 20 kHz . If a 250 mV (rms) input signal at 20 kHz produces a 4 V (pk-pk) output waveform, determine the operational amplifier's upper cut-off frequency, if its open loop gain is approximately 106 dB .

## Solution

The implication is that the upper cut-off frequency of the closed loop amplifier must be 350 kHz if the power output is halved.

The closed loop gain of the operational amplifier is given by:
$\frac{4 \mathrm{~V}(\mathrm{pk}-\mathrm{pk})}{250 \mathrm{mV}(\mathrm{rms})}=\frac{\sqrt{ } 2 \mathrm{~V}(\mathrm{rms})}{250 \mathrm{mV}(\mathrm{rms})}=5 \cdot 656=\mathrm{A}_{\mathrm{CL}}$.
Given that $\quad \mathrm{A}_{\mathrm{OL}}=106 \mathrm{~dB}$

$$
\begin{aligned}
106 \mathrm{~dB} & =20 \log _{10}\left|\frac{\mathrm{~V}_{o}}{\mathrm{~V}_{\text {in }}}\right| \\
5 \cdot 3 & =\log _{10}\left|\mathrm{~A}_{\mathrm{OL}}\right|
\end{aligned}
$$

Hence: $\mathrm{A}_{\mathrm{OL}}=199526$, say 200000.

$$
\text { Now } \begin{aligned}
f_{2(\mathrm{CL})} & =f_{2(\mathrm{OL})} \times \frac{\mathrm{A}_{\mathrm{OL}}}{\left(\mathrm{~A}_{\mathrm{CL}}+1\right)} \\
\therefore f_{2(\mathrm{OL})} & =f_{2(\mathrm{CL})} \times \frac{6 \cdot 656}{200000}\left(\text { neglecting the ' } 1 \text { ' since } \mathrm{A}_{\mathrm{C}} \gg 1\right) \\
& =350 \mathrm{kHz} \times \frac{6 \cdot 656}{200000} .
\end{aligned}
$$

Hence: $f_{2(\mathrm{OL})}=11 \cdot 6 \mathrm{~Hz}$.

### 2.8 Slew rate

The slew rate of an operational amplifier indicates how fast its output voltages can change with respect to time. The general purpose operational amplifiers of the 741 series have a maximum slew rate of about $0.5 \mathrm{~V} / \mu \mathrm{s}$, whereas special purpose operational amplifiers may have slew rates of $100 \mathrm{~V} / \mu \mathrm{s}$ or more. The lowest slew rate usually occurs at unity gain (unity gain as a result of negative feedback). The limited slew rate capabilities occur because internal compensation circuitry can only change its voltage at a rate limited by associated current sources.

For a capacitor $\mathrm{V}=\frac{\mathrm{Q}}{\mathrm{C}}=\frac{\mathrm{I} \times \mathrm{t}}{\mathrm{C}}$ for a constant current, I

$$
\text { so } \frac{\Delta V}{\Delta t}=\frac{I}{C}
$$

Hence, maximum slew rate $=\frac{\text { change in output voltage }}{\text { change in time }}=\frac{\mathrm{I}}{\mathrm{C}}$
Where $I=$ maximum current able to be supplied to the compensating capacitor C.
The essential point is that the capacitor has a maximum charging current associated with it in the operational amplifier, and its maximum voltage change with respect to time occurs when this current is being fully utilised. If capacitor voltage is required to change at a faster rate, there will be distortion of the output signal.

## Example 5

A 741 operational amplifier, being used as a voltage follower, has an instantaneous input change of 5 volts. Determine how long it will take for the output voltage to change by 5 volts.

## Solution

From slew rate $=\frac{\text { change in output voltage }}{\text { time }}=\frac{0.5 \mathrm{~V}}{1 \times 10^{-6} \mathrm{~s}}=\frac{5 \mathrm{~V}}{\text { time }}$
since a voltage follower has unity gain.
So a change of 5 V at output will take $10 \mu \mathrm{~s}$

### 2.9 Slew rate limiting of sine waves

Consider the voltage follower in Fig 2.7 where $v_{i n}$ is a sine wave of peak amplitude $\mathrm{v}_{p}$. The maximum rate of change of $\mathrm{v}_{i n}$, with respect to time, can be shown to be $2 \pi f \mathrm{v}_{p}$ volts/sec where:
a $f$ is the frequency in Hz ,
b the peak amplitude is $\mathrm{v}_{p}$.
The maximum rate of change of voltage with time occurs at the zero crossing points of a sinusoidal waveform; ie the waveform is at its steepest at these points. It should be apparent that increasing amplitude and increasing frequency will cause an increase in steepness at these points. This is because $\frac{\mathrm{dv}_{o}}{\mathrm{dt}} \max =2 \pi f \mathrm{v}_{p}$, that is it is proportional to both $f$ and $\mathrm{v}_{p}$.

If the required rate of change is larger than the slew rate of the operational amplifier, the output, $\mathrm{v}_{o}$, will be distorted. If the slew rate is grossly exceeded, then the output waveform will become triangular in nature, as shown in Fig 2.7.




Fig 2-7 Extreme slew rate limiting of sinusoidal output voltage Vo (when 2miVp)/s)

The maximum frequency, $f_{\max }$, at which slew rate will not distort the output voltage is:
$f_{\text {max }}=\frac{\text { slew rate }}{2 \pi \mathrm{~V}_{o p}}$ where $\mathrm{V}_{o p}=$ maximum undistorted output voltage.

## Example 6

The typical slew rate of a 741 is $0.5 \mathrm{~V} / \mu \mathrm{s}$. Determine the typical maximum frequency that an output signal may have, at an amplitude of 5 volts peak, without slew rate distortion occurring.

## Solution

$$
\begin{aligned}
& \text { Since } f_{\max }=\frac{\text { slew rate }}{2 \pi \mathrm{~V}_{o p}}, \text { ie } f_{\max }=\frac{0.5 \times 10^{6}}{2 \pi \times 5} \\
& \text { then } f_{\max }=16 \mathrm{kHz} .
\end{aligned}
$$

### 2.10 Full power bandwidth (large signal bandwidth)

This is the range of frequencies, from zero, over which a specific type of operational amplifier should produce no slew rate distortion of a maximum amplitude sinusoidal output signal.

A 741C amplifier should be capable of producing about $14 \mathrm{~V}(0-\mathrm{pk})$ sinusoidal for loads greater than, or equal to, 10 k and has a typical maximum slew rate of $0.5 \mathrm{~V} / \mu \mathrm{s}$. It can be shown that the full power bandwidth (FPB, or large signal bandwidth) is given by: $f=\frac{\mathrm{s}}{2 \pi \mathrm{~V}_{p}}$.
Since $2 \pi f \mathrm{~V}_{p} \leqslant \mathrm{~s}$ to avoid slew rate distortion, it follows that $f \leqslant \frac{\mathrm{~s}}{2 \pi \mathrm{~V}_{p}}$ is the range of frequencies over which an output signal of amplitude $\mathrm{V}_{p}$ can be obtained without slew rate distortion.

So full power bandwidth for the 741C will be about
$f \leqslant \frac{0.5 \times 10^{6}}{2 \pi \times 14} \mathrm{~Hz}$,
$\mathrm{FPB}=5.684 \mathrm{kHz}$.

## Example 7

Calculate the full power bandwidth (FPB) of an operational amplifier operating from $\pm 15 \mathrm{~V}$ supply rails, if it saturates within 2 volts of these rails and has a maximum slew rate of $0.8 \mathrm{~V} / \mu \mathrm{s}$.
$\mathrm{FPB}=\frac{\text { slew rate }}{2 \pi \mathrm{~V}_{\text {op }}}=\frac{0.8 \times 10^{6}}{6.28 \times(15-2)}$
Hence: $\mathrm{FPB}=9.8 \mathrm{kHz}$

### 2.11 Slew rate limiting of square wave input

In essence, slew rate limiting is the result of a limit in the ability of the internal circuitry of an operational amplifier to drive capacitive loads, either internal or external. The capacitance that limits the slewing ability is generally the compensation capacitance, although in some instances, it is the load capacitance.

Fig 2.8 shows that at high required rates of signal change the current available to charge or discharge the capacitance is insufficient, and slew rate limiting of the actual output signal occurs.


Fig 2-8 The effect of slew rate on a square wave input

### 2.12 Slew rate limiting of triangular wave input

A triangular wave input will be correctly reproduced, in amplified form, at the output until the repetition rate of the signal is such that the rate of change of voltage inherent in the sloping edge waveform exceeds the slew rate capabilities of the operational amplifier.


Fig 2-9 Waveform diagram for 2.12
It can be shown that to avoid slew rate distortion:
slew rate $>\frac{\mathrm{V}_{o}(\mathrm{pk}-\mathrm{pk})}{(\mathrm{T} / 2)}$ is necessary (Fig 2.9),
ie slew rate $>2 \mathrm{~V}_{o}$ (pk-pk) $f_{\mathrm{r}}$ where $f_{\mathrm{r}}=$ repetition rate .
Hence: $f_{\mathrm{r}} \leqslant \frac{\text { slew rate }}{2 \mathrm{~V}_{o}(\mathrm{pk}-\mathrm{pk})}$, to avoid slew rate distortion.

In practice, two effects distort the output waveform. One is the maximum slew rate and the other is the frequency response limitations of the amplifier. The former tends to make triangular type waveforms, whereas frequency response limit tends to introduce an exponential component. At any instant it is the slower of these two effects that determines the actual waveform shape.

### 2.13 Worked examples

## Example 8

A square wave input to an inverting amplifier circuit results in the output waveform shown in Fig 2.10.


Fig 2-10
The time taken for each positive going output pulse to increase from 0.4 V to 3.6 V is $14 \mu \mathrm{~s}$. Determine the closed loop upper cut-off frequency (bandwidth).

## Solution

The 0.4 V and 3.6 V represent $10 \%$ and $90 \%$ respectively of the maximum amplitude.

Since the closed loop upper cut-off frequency (see Section 2.5)
$=\frac{0.35}{\text { rise time }}$ then $f_{\mathrm{CL}}=\frac{0.35}{14 \times 10^{-6}}$.
Hence: bandwidth or closed loop upper cut-off frequency $=25 \mathrm{kHz}$.

## Example 9

Determine the highest repetition rate of a symmetrical triangular waveform input to an operational amplifier circuit before it suffers from slew-rate distortion.

## Date given

Maximum slew rate $=2 \mathrm{~V} / \mu \mathrm{s}$
pk-pk input amplitude $=600 \mathrm{mV}$
Amplifier gain $=12$

## Solution

Output waveform is as shown in Fig 2.11.


Fig 2-11

$$
\mathrm{v}_{o}(\mathrm{pk}-\mathrm{pk})=12 \times 600 \mathrm{mV}=7.2 \mathrm{~V}
$$

From diagram:
$\frac{\mathrm{v}_{o(\mathrm{pk}-\mathrm{pk})}}{\mathrm{T} / 2} \leqslant$ slew rate to avoid distortion, ie $f_{\mathrm{r}} \leqslant \frac{\text { slew rate }}{2 \mathrm{v}_{o(\mathrm{pk}-\mathrm{pk})}}$
$=\frac{2}{10^{-6} \times 2 \times 7.2}$.
Hence: $f_{\mathrm{r}}=139 \mathrm{kHz}$.

### 2.14 Important review points

## A Prevention of oscillation

Refer to Section 2.1.
One method of preventing unwanted oscillation is to cause the gain to roll off at high frequencies so that there is insufficient gain available for oscillation to take place at the frequencies where there is the necessary loop phase shift of zero degrees.

Whereas negative feedback reduces the effective input signal to the operational amplifier, positive feedback increases it to a point where the
operational amplifier circuit may produce a sinusoidal output signal independent of any external input signal.

## B Bode plot

Refer to Section 2.4.
A Bode plot is a graphical method for showing how the gain and phase shift of an amplifier vary with frequency.

A typical plot for an arbitrary RC coupled amplifier is shown in Fig 2.12.


## Fig 2.12 Bode plot for an RC coupled amplifier

At low frequencies, due to the coupling capacitors' high reactance, the gain is very low, and the phase angle of the output, relative to the input, is leading by $90^{\circ}$. At frequency $f_{1}$ the magnitude of the gain is 3 dB less than its mid-frequency value, and the phase lead is now $45^{\circ}$.

Over the bandwidth the gain and phase shift are reasonably constant. However, at $f_{2}$, the gain has again fallen to 3 dB below its mid-frequency value and the phase lag is $45^{\circ}$.

For this amplifier, the phase angle between output and input increases to a maximum of $-90^{\circ}$. The fall in gain at high frequencies is due to internal active device capacity tending to short the signal to ground, whilst the phase lag is due to the input, output and interstage coupling capacitors.

C Proof of: $f_{2}=\frac{0.35}{\text { rise time }}$
Refer to Section 2.5.


Fig 2-13
An amplifier with a single upper cut-off frequency, $f_{2}$, may be represented by the circuit shown in Fig 2.13.

If $\mathrm{v}_{i n}$ in a step function of amplitude E , the output voltage, $\mathrm{v}_{o}$, will be: $\mathrm{v}_{o}=\mathrm{AE}\left(1-\mathrm{e}^{-t / \mathrm{CR}}\right)$.

The times $t_{1}$ and $t_{2}$ taken to reach $10 \%$ and $90 \%$ respectively of full amplitude will be: $t_{1}=\mathrm{CR} \ln 0.9$ and $t_{2}=\mathrm{CR} \ln 0 \cdot 1$
so $10 \%$ to $90 \%$ rise time is $t_{2}=\mathrm{CR}(\ln 0.9-\ln 0 \cdot 1)$

$$
\text { Now } \begin{aligned}
f_{2} & =\frac{1}{2 \pi \mathrm{CR}} \\
& =\frac{(\ln 0 \cdot 9-\ln 0 \cdot 1)}{2 \pi t_{2}}
\end{aligned}
$$

Hence: $f_{2}=\frac{0.35}{t_{2}}$.

### 2.15 Problems for readers

## Example 10

An operational amplifier, with open loop cut-off frequency equal to 10 Hz , is used in a non-inverting circuit with closed loop voltage gain of 12 . With a square wave input signal, the output rise time is measured as $7 \mu \mathrm{~s}$. Determine the open loop gain of the operational amplifier, in dB .

## Solution

95.6 dB

## Operational Amplifier Circuits

## Example 11

A standard non-inverting amplifier circuit has an output resistance of $30 \mathrm{~m} \Omega$. The operational amplifier has an open loop output resistance of $120 \Omega$, an upper -3 dB cut-off frequency of 10 Hz and an open loop gain of 102 dB . Determine the amplifier's -3 dB bandwidth.

Solution
40 kHz

## Chapter 3 <br> WAVEFORM GENERATORS

### 3.1 Introduction

This chapter deals with operational amplifier circuits which generate signals.

The four common circuits are:

- Square wave
- Triangular wave
- Sawtooth wave
- Sine wave


### 3.2 Square wave generator

A multivibrator is a circuit which essentially generates square waves.
There are three types of multivibrator:
Astable (free running) - The two states of the circuit are momentarily stable, and the circuit switches repetitively between these states.
Monostable (one shot) - Has only one stable state, but it can be made to change to another state by the application of a suitable trigger pulse. It then returns to the stable state after a time interval determined by circuit component values.
Bistable (flip-flop) - Has two stable states and remains in one until suitably triggered to the other, in which it remains until again triggered to the first state, and so on.

### 3.3 Basic principles of a bistable npn transistor multivibrator

It is useful to note the basic principles of a bistable npn transistor multivibrator before considering the operational amplifier configurations. First
consider the transistor as a switch, as shown in Fig 3.1, as the base voltage is changed from reverse bias to forward bias. The resulting voltage waveforms are also shown in Fig 3.1.


Fig 3-1 Basic principles of a transistor as a switch
Reverse bias Leakage current only in the collector circuit. The voltage drop across $\mathrm{R}_{c}$ is very small. The collector voltage is effectively ${ }_{c}+\mathrm{V}_{c c}$. Forward bias Collector current flows. The collector voltage falls until it saturates, in this case, at just about the base voltage.

The principle of the above action is now applied to a bistable npn transistor multivibrator circuit as shown in Fig 3.2.


Fig 3-2 Bistable npn transistor multivibrator
a Initially assume that the base-emitter junction of $V_{1}$ is reverse biased. The collector of $\mathrm{V}_{1}$ will be at $\mathrm{V}_{c c}$. A positive trigger pulse raises $\mathrm{V}_{1}$ base above zero. $\mathrm{V}_{1}$ collector voltage falls, causing $\mathrm{V}_{2}$ base voltage to fall, cutting off $V_{2}$. The collector voltage of $V_{2}$ rises to $V_{c c}$.
b A negative trigger pulse lowers collector current of $\mathrm{V}_{1}$, causing $\mathrm{V}_{1}$ collector voltage to rise, which raises $\mathrm{V}_{2}$ base above zero. $\mathrm{V}_{2}$ collector voltage falls, assisting the fall of $\mathrm{V}_{1}$ base voltage and resulting in the cut-off of $\mathrm{V}_{1}$. The collector voltage of $\mathrm{V}_{1}$ rises to $\mathrm{V}_{c c}$, the initial condition.

### 3.4 Operational amplifier as a free-running symmetrical multivibrator



Fig 3-3 Free running symmetrical multivibrator
a Refer to Fig 3.3. The two states of the circuit, between which it switches are:

- positive saturation
- negative saturation
b The output is a square wave of frequency:
$f=\frac{1}{\mathrm{~T}}=\frac{1}{2 \mathrm{RC} \ln \left(\frac{1+\beta}{1-\beta}\right)}$
C The feedback ratio ( $\beta$ ) is established by the potential divider made up of $R_{1}$ and $R_{2}$, ie $\beta=\frac{R_{2}}{R_{1}+R_{2}}$
d The amplitude of the exponential triangular waveform is $\beta \mathrm{V}_{o}$


Fig 3-4 Waveforms of free running multivibrator
a Assume that at time $t_{\mathrm{A}}$ the amplifier output is at $\mathrm{V}_{o}^{-}$(sat). The voltage at terminal A (Fig 3.3) is $\beta \mathrm{V}_{o}^{-}$(sat).
b Simultaneously, at time $t_{\mathrm{A}}$, terminal B is positive with respect to terminal A and its potential decreases as C discharges through R towards $\mathrm{V}_{o}^{-}$(sat).
c When $V_{B}=V_{A}$ (since $V_{B}$ is changing in potential, whereas $V_{A}$ is static), the amplifier will start to come out of saturation. The positive feedback to terminal A will then assist in driving the output towards the positive saturation level.
d The voltage across $C$ cannot change instantaneously. $C$ will now charge up through R towards $\mathrm{V}_{o}^{+}$(sat) and the potential at B will rise exponentially to $\beta V_{o}^{+}$(sat).
e The circuit will start to switch back to the initial state of negative saturation when $V_{B}$ again equals $V_{A}$.

## Example 1

Assume that the output of the circuit in Fig 3.5 saturates at some level between +12 V and +14 V .


## Fig 3 -5

a Determine the frequency and amplitude of the waveforms at A and B.
b Determine the possible variation in frequency and amplitude that would be caused by using resistors with tolerance of $\pm 5 \%$ and a capacitor with a tolerance of $\pm 10 \%$.

## Solution

a

$$
\begin{aligned}
\beta & =\frac{R_{2}}{R_{1}+R_{2}}=\frac{3 k}{6 \cdot 8 k+3 k}=\frac{3 k}{9.8 k}=0.306 \\
T & =2 R C \ln \frac{(1+\beta)}{(1-\beta)}
\end{aligned}
$$

Hence: $T=2 \times 8.2 \mathrm{k} \times 0.18 \times 10^{-6} \ln \left(\frac{1+0.306}{1-0.306}\right)$
$=2.952 \times 10^{-3} \ln \left(\frac{1.306}{0.694}\right)$
$=0.002952 \times 0.633$
Hence: $\mathrm{T}=0.001867$ seconds and, since $\mathrm{T}=\frac{1}{f}$,

$$
f=535 \cdot 6 \mathrm{~Hz}=\text { frequency at } \mathrm{A} \text {, and } \mathrm{B}
$$

The amplitude of the square wave output will be between +12 volts and +14 volts, so the exponential triangular waveform will be $\beta$ times these values, ie between $12 \times 0.306$ and $14 \times 0.306$.

Hence, range is: 3.67 V and $4.29 \mathrm{~V}(0-\mathrm{pk})$
Amplitude of waveform at A between 3.67 and 4.29 V
Amplitude of waveform at B between 12 and 14 V
b $\beta_{(\max )}=\frac{3 \mathrm{k} \times 1.05}{(3 \mathrm{k} \times 1.05)+(6.8 \mathrm{k} \times 0.95)}=\frac{3 \cdot 15 \mathrm{k}}{3 \cdot 15 \mathrm{k}+6.46 \mathrm{k}}=\frac{3.15 \mathrm{k}}{9.61 \mathrm{k}}$
$\beta_{(\text {max })}=0.328$
$\beta_{(\text {min })}=\frac{3 \mathrm{k} \times 0.95}{(3 \mathrm{k} \times 0.95)+(6.8 \mathrm{k} \times 1.05)}=\frac{2.85 \mathrm{k}}{2.85 \mathrm{k}+7.14 \mathrm{k}}=\frac{2.85 \mathrm{k}}{9.99 \mathrm{k}}$
$\beta_{(\text {min })}=0.285$
so $T_{(\max )}=2 \times 1.05 \times 8.2 \mathrm{k} \times 1.1 \times 0.18 \times 10^{-6} \ln \left(\frac{1+0.328}{1-0.328}\right)$
$=3.41 \times 10^{-3} \ln \left(\frac{1.328}{0.672}\right)$
$=0.00341 \times 0.681=0.00232$ seconds
so $f_{(\min )}=\frac{1}{0.00232}=430.9 \mathrm{~Hz}$
$T_{(\text {min })}=2 \times 0.95 \times 8.2 \mathrm{k} \times 0.9 \times 0.18 \times 10^{-6} \ln \left(\frac{1+0.2853}{1-0.2853}\right)$
$=2.52 \times 10^{-3} \ln \left(\frac{1.2853}{0.7147}\right)$
$=0.00252 \times 0.587=0.00148$ seconds
so $f_{(\max )}=\frac{1}{0 \cdot 00148}=675 \cdot 1 \mathrm{~Hz}$.
The frequency is not affected by the square wave amplitude. The square wave amplitude will still be between 12 and 14 volts.

The exponential triangular waveform will be between:
$\beta_{(\text {min })} \times 12$ and $\beta_{(\max )} \times 14$
$=0.285 \times 12$ and $0.328 \times 14$
$=3.42 \mathrm{~V}$ and $4.59 \mathrm{~V}(0-\mathrm{pk})$.

## Example 2

The basic square wave generator (astable or free running multivibrator) shown in Fig 3.6 is to be constructed so that the 'triangular' waveform is to be half the amplitude of the square wave output. The frequency of the oscillation is to be 200 Hz . Determine the constraints that these requirements place on the component values.


Fig 3-6

## Solution

$T=2 R C \ln \left(\frac{1+\beta}{1-\beta}\right)$ and the required value of $T=\frac{1}{200} \mathrm{~s}=5 \mathrm{~ms}$ so: $\quad 0.005=2 \mathrm{RC} \ln \left(\frac{1+\beta}{1-\beta}\right)$

The amplitude relationship requires that $\beta=0.5$
Substituting (2) in (1) gives: $0 \cdot 005=2 \mathrm{RC} \ln \left(\frac{1 \cdot 5}{0 \cdot 5}\right)$
Hence: $0.005=2 \mathrm{RC} \ln 3$

$$
0.005=2.197 \mathrm{RC}
$$

$$
\begin{equation*}
\text { so } \mathrm{RC}=0.00228 \tag{3}
\end{equation*}
$$

Also from (2) $\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}=0 \cdot 5$, so $\mathrm{R}_{1}=\mathrm{R}_{2}$ is required, and from (3) $\mathrm{R}(\mathrm{k} \Omega) \times \mathrm{C}(\mu \mathrm{F})=2.28$ is necessary.

A suitable set of values would be:
$\mathrm{R}_{1}=\mathrm{R}_{2}=10 \mathrm{k}$
$\mathrm{R}=2.2 \mathrm{k}$
$\mathrm{C}=\frac{2.28}{2.2 \mathrm{k}}=1.036 \mu \mathrm{~F}$
In practice C would be $1 \mu \mathrm{~F}$ and R either a variable resistor or a variable resistor in series with a fixed resistor. This would enable the frequency to be adjustable to 200 Hz while using standard value components.

Some other restrictions on component values would exist to ensure the circuit operated correctly. These would include $R$ and $\mathbf{R}_{1} \| \mathbf{R}_{2}$ both very much lower than $\mathrm{R}_{\text {in }}$ of the operational amplifier. R and $R_{1} \| R_{2}$ should be such as to ensure that the output current of the operational amplifier was below its rated maximum output current, or its current limited output, as applicable.

### 3.5 Ramp-generator theory

It will be useful to note the basic principles of ramp-generator theory, before considering triangular wave generator principles.

Consider a constant current source as shown in Fig 3.7. Capacitor C is charged by the constant current when the switch is closed.


Fig 3-7 Constant-current source ramp generation
$\mathrm{V}_{c}$ is called a ramp voltage. If the constant current source is replaced by $\mathrm{V}_{\text {in }}$ and $\mathrm{R}_{\text {in }}$ and an operational amplifier, as shown in Fig 3.8, I will equal $\frac{\mathrm{V}_{\text {in }}}{\mathrm{R}_{\text {in }}}$ since negative input will remain close to ground potential, due to the high open-loop gain of the operational amplifier.


Fig 3-8 The basic integrator circuit as a ramp generator

The circuit shown in Fig 3.8 has several disadvantages:
a $\mathrm{V}_{o}$ can only go to -V (sat).
b When $\mathrm{V}_{\text {in }}=0, \mathrm{~V}_{o} \neq 0$ because the small bias currents will charge the capacitor.
c To obtain a positive-going ramp, $\mathrm{V}_{i n}$ must be reversed.

### 3.6 Basic triangular wave generator circuit



Fig 3-9 Basic triangular wave generator circuit

In Fig 3.9 the size of the triangular amplitude is equivalent to $\frac{R_{1}}{R_{2}} V_{\text {sat }}$ (0-pk).
The frequency of the waveform is given by: $f=\frac{\mathbf{R}_{2}}{4 \mathbf{R}_{1} \mathrm{RC}} \mathrm{Hz}$
This relationship is proved in Section 3.13A (Important review points).

### 3.7 Triangular wave generator circuit

Fig 3.10 shows the essential elements of a circuit that combines positive and negative ramp generation to produce a triangular waveform.


Fig 3-10 Triangular wave generator
a Adjustment of R controls the frequency.
b $\mathrm{R}_{1}$ applies a voltage, $\mathrm{V}_{1}$, to the inverting input of $\mathrm{N}_{2}$. Varying the setting of $R_{1}$ alters the DC level of the triangular wave.
C $\mathrm{R}_{2}$ controls the peak to peak swing of the triangular wave.
d $\mathrm{R}_{3}$ controls the triangular waveform symmetry, ie the relative rise and fall times of the triangular waveform.
e The zener diode clipping circuit limits the square wave amplitude to $\left(\mathrm{V}_{\mathrm{Z}}+\mathrm{V}_{\mathrm{D}}\right)$ as shown in Fig 3.10: $\mathrm{V}_{\mathrm{D}}$ is the zener diode forward voltage drop.
$f$ The feedback capacitor from the output to the inverting input of $\mathrm{N}_{1}$ means that this circuit can be classified as an integrator. This is consistent with the above description, because the integral of the constant capacitor charging current is a ramp voltage.
(See Section 1.14.)

## Example 3

In Fig 3.11 the operational amplifiers saturate at $\pm 14 \mathrm{~V}$ output levels.
The reverse biased zener diode voltage drops equal 6.2 V and $\mathrm{V}_{\mathrm{D}_{1}}=$ $\mathrm{V}_{\mathrm{D}_{2}}=0.6 \mathrm{~V}$.
a Determine the frequency of oscillation of the circuit shown.
b State the function of $\mathrm{R}_{1}$.
c What is the voltage ( $\mathrm{pk}-\mathrm{pk} \mathrm{)} \mathrm{at} \mathrm{point} \mathrm{A} \mathrm{?}$
d What is the voltage (pk-pk) at point B ?
e State the function of the zener diodes $V_{1}$ and $V_{2}$.


Fig 3-11

## Solution

a $f=\frac{\mathrm{R}_{2}}{4 \mathrm{R}_{4} \mathrm{CR}_{3}}=\frac{20 \mathrm{k}}{4 \times 5 \mathrm{k} \times 0.1 \times 10^{-6} \times 10 \mathrm{k}}=1 \mathrm{kHz}$
b Essentially, the function of $\mathrm{R}_{1}$ is to limit the output current of $\mathrm{N}_{1}$, since when $\mathrm{V}_{\mathrm{A}}$ exceeds $\left(\mathrm{V}_{\mathrm{Z}}+\mathrm{V}_{\mathrm{D}}\right)$, the clipping circuit will appear as almost a short-circuit load.
c The peak-to-peak voltage at point $A$ must equal $\left[+V_{\text {sat }}-\right.$ $\left.\left(-\mathrm{V}_{\text {sat }}\right)\right]=2 \mathrm{~V}_{\text {sat }}$. Hence, the peak-to-peak voltage is $2 \times 14=28$ volts.
d The peak-to-peak voltage at point $B=2\left(V_{D}+V_{Z}\right)$,

$$
\text { ie } B=2(0.6+6 \cdot 2)=13.6 \mathrm{~V}
$$

e The zener diodes $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ ensure that $\mathrm{N}_{1}$ does not saturate heavily, which avoids discrepancies between theoretical and practical frequency values.

### 3.8 Sawtooth wave generator

The single ramp generator mentioned in Section 3.5 can be modified to make a sawtooth wave generator. A typical circuit is shown in Fig 3.12, where it can be seen that a programmable unijunction transistor (PUT) has been connected across C . The function of the PUT is as follows:
a When the voltage across $\mathrm{C}=\mathrm{V}_{p}$, the PUT short-circuits C by becoming a low resistance from A to K .
b When the voltage across $\mathrm{C}=\mathrm{V}_{\mathrm{F}}$, the PUT becomes an open circuit from A to K .


Fig 3-12 Sawtooth wave generator
a The voltage, $\mathrm{V}_{p}$, applied to the gate terminal of the PUT corresponds to the peak amplitude of the sawtooth waveform.
b The PUT will act as an open circuit from A to K prior to the circuit being energised. C will charge up when the circuit is energised, with the terminal connected to the amplifier output becoming more positive due to the current flowing via $\mathrm{R}_{1}$ to $-\mathrm{V}_{1}$. This will continue until the potential at A becomes about 0.7 volts higher than that at $G$, ie 0.7 volts higher than that at $\mathrm{V}_{p}$. The PUT will then act as a short circuit from A to K.
C C then discharges rapidly until the current from A to K falls below the holding current of the PUT, when the PUT returns to its initial state and the cycle recommences.
d The frequency of oscillation, $f \simeq \frac{\mathrm{~V}_{1}}{\mathrm{R}_{1} \mathrm{CV}_{p}}$

### 3.9 Introduction to sine wave generators (oscillators)

Consider a feedback amplifier in which the feedback network has a gain (B) at one frequency, $f_{o}$, as shown in Fig 3.13.

At the same frequency, the amplifier's gain is A and the product, AB , being the loop gain, is exactly unity, which is the highest value of the loop gain at any frequency.


## Fig 3-13 Principles of sinusoidal oscillation

a The amplifier and the feedback network also have the property that, at the same frequency, $f_{o}$, as before, the sum of their phase shifts is exactly $0^{\circ}$, or (which amounts to the same thing) $360^{\circ}$. Any signal introduced into the feedback network at the frequency $f_{o}$ will continue to traverse the feedback loop indefinitely without changing its amplitude, at any specific point in the circuit, even if the initiating signal is removed.
b Signals at other frequencies circulate, but die out since they would not experience the unity loop gain, or the zero, or $360^{\circ}$, loop phase shift, necessary for their regeneration.
c The circuit is, in fact, then a signal generator in its own right. If the loop gain is increased to greater than unity at $f_{o}$ then a signal at that frequency will build up to a usable level when it has traversed the loop a sufficient number of times.
d By altering appropriate components in the feedback network, the frequency may be easily varied. Feedback networks can be constructed that give the required loss and phase shift combination necessary for oscillation over a wide, tuneable range of frequencies. Hence variable frequency oscillators may be constructed.

### 3.10 Oscillators

Figure 3.14 shows a typical circuit diagram of a sine wave oscillator using an operational amplifier and a twin $T$ network. In addition, Fig 3.14 also
shows the characteristic frequency response of the network. The frequency of oscillation is given by:
$f_{o}=\frac{1}{2 \pi \mathrm{RC}}$


Fig 3-14 Sine wave oscillator and frequency response curve
a A twin $T$ network is used as the feedback network of the oscillator. Since it is the feedback circuit to the operational amplifier's inverting input, as the frequency response shows, there is no negative feedback at the notch frequency and very high negative feedback at all other frequencies.
b Increasing $\mathrm{R}_{2}$ will increase the amount of positive feedback to the amplifier. It is only at the notch frequency that there is no counterbalancing negative feedback, so that at that frequency the loop gain is relatively high and enables any signals at that frequency to build up to a useful amplitude as they circulate around the circuit.
c $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ tend to stabilise the output signal amplitude since, if it increases in amplitude, their resistance tends to decrease, so increasing the amount of negative feedback and vice versa for decreasing output amplitude.

### 3.11 Wien bridge oscillator



Fig 3-15 Basic circuit of Wien bridge oscillator

It can be shown that if $\mathrm{C}_{1}=\mathrm{C}_{2}=\mathrm{C}$ and $\mathrm{R}_{1}=\mathrm{R}_{2}=\mathrm{R}$,
a $\mathrm{v}_{f}=\frac{\mathrm{v}_{o}}{3}$ at the oscillation frequency, $f_{o}$
b $f_{o}=\frac{1}{2 \pi \mathrm{CR}}$
These relationships are proved in Section 3.13B.

### 3.12 Additional worked examples

## Example 4

Assume that the operational amplifiers shown in Fig 3.16 saturate at $\pm 13 \mathrm{~V}$. Describe the effect upon the output signals, $\mathrm{v}_{o 1}$ and $\mathrm{v}_{o 2}$, of adjusting $\mathrm{R}_{\mathrm{V}_{1}}$, from 0 to 10 k .


Fig 3-16

## Solution

Let $\mathrm{R}_{\mathrm{V}_{1}}=0 . \quad f=\frac{\left(\mathrm{R}_{2}+\mathrm{R}_{\mathrm{V}_{1}}\right)}{4 \mathrm{R}_{1} \mathrm{R}_{3} \mathrm{C}}=\frac{5000}{4 \times 5000 \times 3900 \times 0.2 \times 10^{-6}}$

$$
=320 \cdot 5 \mathrm{~Hz}
$$

Let $\mathrm{R}_{\mathrm{v}_{1}}=10 \mathrm{k}, f=\frac{15000}{4 \times 5000 \times 3900 \times 0.2 \times 10^{-6}}$

$$
=961 \cdot 5 \mathrm{~Hz}
$$

So as $\mathrm{R}_{\mathrm{V}_{1}}$, varies from 0 to 10 k , the frequency will vary from $320 \cdot 5 \mathrm{~Hz}$ to $961 \cdot 5 \mathrm{~Hz}$, proportional to $\left(\mathrm{R}_{2}+\mathrm{R}_{\mathrm{V}_{1}}\right)$.

The amplitude of the triangular waveform, $\mathrm{v}_{o 1}$, is:
$\left(\frac{\mathrm{R}_{3}}{\mathrm{R}_{2}+\mathrm{R}_{\mathrm{v}_{1}}}\right) \mathrm{V}_{o 2}$
where $\mathrm{V}_{o 2}$ is a square wave of amplitude $\pm 13 \mathrm{~V}(0-\mathrm{pk})$ at the same frequency.

Hence, amplitude of triangular waveform will vary between

$$
\begin{aligned}
\pm\left(\frac{3900}{5000}\right) 13 & =10 \cdot 14 \mathrm{~V} \\
\text { and } \pm\left(\frac{3900}{15000}\right) 13 & =3 \cdot 38 \mathrm{~V}
\end{aligned}
$$

These waveforms are shown in Fig 3.17.


Fig 3-17

## Example 5

Assuming that the operational amplifiers in Fig 3.18 go into saturation when their respective outputs get to within 2 volts of their supply rails, determine suitable component values to produce a triangular output signal of amplitude 7 volts (pk-pk) at a frequency of 1.5 kHz . Assume $R_{3}=6.8 \mathrm{k}$, and that $R_{1}$ and $R_{2}$ together are to have a combined value of 10 k .

## Operational Amplifier Circuits



Fig 3-18

## Solution

$\mathrm{v}_{o 1}$ is a square wave output and $\mathrm{v}_{o 2}$ is a triangular wave output.
The frequency of both is given by: $f=\frac{\mathrm{R}_{1}}{4 \mathrm{R}_{2} \mathrm{R}_{3} \mathrm{C}}$
so $\frac{R_{1}}{4 \mathrm{R}_{2} \mathrm{R}_{3} \mathrm{C}}=1500$
The amplitude of the triangular wave output is: $\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}}\right) \mathrm{V}_{o 1}$ where $\mathrm{v}_{o 1}$ will be a square wave of amplitude, $\mathrm{V}_{o 1}= \pm 10 \mathrm{v}$. Considering the given data, a requirement is: $\pm\left(\frac{R_{2}}{R_{1}}\right) 10= \pm 3 \cdot 5$

From equation (1) $\frac{R_{2}}{R_{1}}=\frac{1}{6000 \mathrm{R}_{3} \mathrm{C}}$, and substituting this in equation (2) gives: $\frac{10}{6000 \mathrm{R}_{3} \mathrm{C}}=3.5$ so, given that $\mathrm{R}_{3}=6.8 \mathrm{k}$, $\mathrm{C}=007 \mu \mathrm{~F}$ from equation (2) $10 \mathrm{R}_{2}=3.5 \mathrm{R}_{1}$ so $2.857 \mathrm{R}_{2}=\mathrm{R}_{1}$.

Since $R_{1}+R_{2}=10 \mathrm{k}$ is given, this means $2 \cdot 857 R_{2}+R_{2}=10 \mathrm{k}$.

$$
\begin{aligned}
& \mathrm{R}_{1}=7.41 \mathrm{k} \\
& \mathrm{R}_{2}=2.59 \mathrm{k}
\end{aligned}
$$

## Example 6

In Fig $3.19 \mathrm{C}_{1}$ and $\mathrm{C}_{2}$ are ganged, matched variable capacitors, with a range covering at least 45 pF to 500 pF each. Determine:
a The nominal loop gain of the circuit at oscillation frequencies.
b The nominal range of frequencies obtainable from the oscillator.
c By considering the equation in Section 3.13B, determine whether the circuit can be guaranteed to oscillate under worst conditions, if the resistors are $\pm 5 \%$ tolerance.
d Comment on some of the characteristics that a practical operational amplifier would require, to enable the circuit to function correctly.


Fig 3-19

## Solution

a Amplifier gain is nominally: $1+\frac{\mathrm{R}_{3}}{\mathrm{R}_{4}}=1+\frac{100 \mathrm{k}}{39 \mathrm{k}}=3.564$ and the loss through the CR network is nominally $1 / 3$. So loop gain is nominally
$\frac{1}{3} \times 3.564=1.19$
b Maximum nominal frequency of oscillation is:
$\frac{1}{2 \pi \mathrm{RC}_{(\text {min })}}=\frac{1}{2 \pi \times 45 \times 10^{-12} \times 330 \times 10^{3}}=10.72 \mathrm{kHz}$
Frequency is inversely proportional to C , and so with $\mathrm{C}=500 \mathrm{pF}$, will be: $\frac{45 \mathrm{pF}}{500 \mathrm{pF}} \times 10.72 \mathrm{kHz}=965 \mathrm{~Hz}$.
Hence, the range of frequencies $=965 \mathrm{~Hz}$ to 10.72 kHz .
c In cases where $R_{1} \neq R_{2}$ and $C_{1} \neq C_{2}$,
$f=\frac{1}{2 \pi \sqrt{\mathrm{C}_{1} \mathrm{C}_{2} \mathrm{R}_{1} \mathrm{R}_{2}}}$
and the 'gain' of the $C R$ network is: $\frac{1}{1+\frac{C_{2}}{C_{1}}+\frac{R_{1}}{R_{2}}}$
The 'gain' of the network with $5 \%$ tolerance resistors will vary between:

$$
\frac{1}{1+1+\frac{0.95 \times 330 \mathrm{k}}{1.05 \times 330 \mathrm{k}}} \text { and } \frac{1}{1+1+\frac{1.05 \times 330 \mathrm{k}}{0.95 \times 330 \mathrm{k}}}
$$

ie the 'gain' of the network will vary between:
$\frac{1}{2+\frac{0.95}{1.05}}$ and $\frac{1}{2+\frac{1.05}{0.95}}$
$=\frac{1}{2 \cdot 905}$ and $\frac{1}{3 \cdot 11}$
$=0.344$ and 0.322 .
The gain of the amplifier will be between:
$1+\frac{\mathrm{R}_{3}}{\mathrm{R}_{4}}=1+\frac{0.95 \times 100 \mathrm{k}}{1.05 \times 39 \mathrm{k}}$ and $1+\frac{1.05 \times 100 \mathrm{k}}{0.95 \times 39 \mathrm{k}}$
$=1+\frac{95 \mathrm{k}}{40.95 \mathrm{k}}$ and $1+\frac{105 \mathrm{k}}{37 \cdot 05 \mathrm{k}}$
$=3.32$ and 3.83 .
Hence the loop gain will vary between a minimum of $3.32 \times 0.322$ and a maximum of $3.83 \times 0.344$, ie between 1.07 and 1.32 .

Thus the circuit should always oscillate since, with an ideal operational amplifier, the loop gain always exceeds unity. (Even with a practical amplifier with an open loop gain exceeding about 50 , the circuit should still oscillate.) The actual frequency range would vary from:

$$
\begin{aligned}
& \frac{1}{2 \pi \times 500 \times 10^{-12} \times 330 \times 10^{3} \times 1.05} \text { to } \\
& \frac{1}{2 \pi \times 45 \times 10^{-12} \times 330 \times 10^{3} \times 1.05} \\
& =918.6 \mathrm{~Hz} \text { to } 10.2 \mathrm{kHz} \text {. } \\
& \text { for } \mathrm{R}_{1} \text { and } \mathrm{R}_{2} \text { at the top of tolerance limit. } \\
& \text { and } \frac{1}{2 \pi \times 500 \times 10^{-12} \times 330 \times 10^{3} \times 0.95} \text { to }
\end{aligned}
$$

$\frac{1}{2 \pi \times 45 \times 10^{-12} \times 330 \times 10^{3} \times 0.95}$
$=1.02 \mathrm{kHz}$ to 11.3 kHz ,
for $R_{1}$ and $R_{2}$ at the bottom of tolerance limit.
d To avoid slew rate effects, S would have to be at least the maximum value of $2 \pi f \mathrm{~V}$, ie $2 \pi \times 11.3 \mathrm{kHz} \times 15=1.06 \mathrm{~V} / \mu \mathrm{s}$.

To avoid problems associated with phase shift in the amplifier, the closed loop upper cut-off frequency should be at least about 10 times higher than the highest oscillation frequency, ie $10 \times$ $11.3 \mathrm{kHz}=113 \mathrm{kHz}$. This implies a closed loop gain-bandwidth product of $3 \times 113 \mathrm{kHz}$, ie 339 kHz . Now, assuming the minimum gain-bandwidth product is around $1 / 10$ of the typical figure for an operational amplifier, this implies that the nominal gain-bandwidth product requirement is about 3.4 MHz , ie an open loop gain of 200000 and an open loop upper cut-off frequency of 17 Hz , for example.

### 3.13 Important review points

A Proof of $\boldsymbol{f}=\frac{\mathbf{R}_{\mathbf{2}}}{\mathbf{4 \mathbf { R } _ { 1 } \mathbf { R C }}}$
Refer to Section 3.6.


Fig $\mathbf{3 . 2 0}$

Total voltage change in time $T / 2$ is:
$\left(\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\right) \mathrm{V}_{\text {sat }}-\left[-\left(\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\right) \mathrm{V}_{\text {sat }}\right]=\left(\frac{2 \mathrm{R}_{1}}{\mathrm{R}_{2}}\right) \mathrm{V}_{\text {sat }}$
$\mathrm{V}_{\mathrm{C}}=\frac{\mathrm{Q}}{\mathrm{C}}=\frac{\mathrm{It}}{\mathrm{C}} \quad\left(\right.$ Where $\mathrm{I}=\frac{\mathrm{V}_{\text {sat }}}{\mathrm{R}}$, due to negative input of $\mathrm{N}_{1}$ (Fig 3.9) remaining close to ground potential because of high open loop gain)
so: $\mathrm{V}_{\mathrm{C}}=\frac{\mathrm{V}_{\text {sat }} \times \mathrm{t}}{\mathrm{RC}}$.
In this case $V_{C}=\left(\frac{2 R_{1}}{R_{2}}\right) V_{\text {sat }}$
ie $\left(\frac{2 R_{1}}{R_{2}}\right) V_{\text {sat }}=\frac{V_{\text {sat }} \times t}{R C}($ where $t=T / 2)$
so $\frac{2 R_{1}}{R_{2}}=\frac{T}{2 R C}$ hence $T=\frac{4 R_{1} R C}{R_{2}}$

$$
f=\frac{\mathrm{R}_{2}}{4 \mathrm{R}_{1} \mathrm{RC}} \mathrm{~Hz}
$$

B Proof of: $V f=\frac{V_{0}}{3}$ and $f=\frac{1}{2 \pi C R}$
From Section 3.11. The basic circuit of the Wien bridge oscillator is as shown in Fig 3.21.


## Fig 3.21

The relationship between $\mathrm{v}_{f}$ and $\mathrm{v}_{o}$ is given by the equation:
$\mathrm{v}_{f}=\frac{\mathrm{V}_{o}}{1+\frac{\mathrm{C}_{2}}{\mathrm{C}_{1}}+\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}+j\left(\omega \mathrm{C}_{2} \mathrm{R}_{1}-\frac{1}{\omega \mathrm{C}_{1} \mathrm{R}_{2}}\right)}$

The $j$ term disappears when: $\omega \mathrm{C}_{2} \mathrm{R}_{1}=\frac{1}{\omega \mathrm{C}_{1} \mathrm{R}_{2}}$
This occurs when: $\omega=\frac{1}{\sqrt{\mathrm{C}_{1} \mathrm{C}_{2} \mathrm{R}_{1} \mathrm{R}_{2}}}$
This leaves

$$
\begin{equation*}
\mathrm{v}_{f}=\frac{\mathrm{v}_{o}}{1+\frac{\mathrm{C}_{2}}{\mathrm{C}_{1}}+\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}} \tag{1}
\end{equation*}
$$

when $\omega=\frac{1}{\sqrt{\mathrm{C}_{1} \mathrm{C}_{2} \mathrm{R}_{1} \mathrm{R}_{2}}}, \mathrm{v}_{f}$ is therefore in phase with $\mathrm{v}_{o}$ but with a magnitude determined by the denominator of the relationship shown in equation (2).

If $C_{1}=C_{2}=C$ and $R_{1}=R_{2}=R$, then equation (1) reduces to
$2 \pi f=\omega=\frac{1}{\sqrt{\mathrm{C}^{2} \mathrm{R}^{2}}}=\frac{1}{\mathrm{CR}} \quad$ ie $\quad f=\frac{1}{2 \pi \mathrm{CR}}$
Equation (2) reduces to:

$$
\mathrm{v}_{f}=\frac{\mathrm{v}_{o}}{1+\frac{\mathrm{C}}{\mathrm{C}}+\frac{\mathrm{R}}{\mathrm{R}}}
$$

ie $\quad \mathrm{v}_{f}=\frac{\mathrm{v}_{o}}{3}$
Hence, if the amplifier is non-inverting and with a gain of slightly more than 3 , the circuit will function as an oscillator at a frequency $f=$ $\frac{1}{2 \pi \mathrm{CR}}$.

Discrete circuit Wien oscillators may be designed to operate satisfactorily up to about 1 MHz . At higher frequencies the value of C and R become comparable with circuit stray capacity and capacitor loss resistance. Consequently, frequency prediction becomes unreliable.

### 3.14 Problems for readers

## Example 7

In Fig $3.22 V_{1}$ and $V_{2}$ are $6 \cdot 2 \mathrm{~V} \pm 5 \%$ zener diodes when operated at a reverse current of 5 mA . Their forward voltage drop is nominally 0.65 volts at 5 mA forward current. Determine:
a A suitable value for $\mathrm{R}_{4}$ if the zener diodes are to clip the output waveform of the operational amplifier to a nominal amplitude of 6.85 volts. Assume that the operational amplifier output saturates at $\pm 13$ volts.
b The effect on the frequency and amplitude of the triangular and square wave waveforms if:
i $R_{1}$ is doubled in value,
ii $R_{3}$ is doubled in value.


Fig 3 -22

## Solution

a $\quad \mathrm{R}_{4}=1.23 \mathrm{k}$.
b The amplitude of the square wave is governed by the zener diode, so it is unaffected. The frequency of both triangular and square waveforms changes from 3.61 kHz to 5.46 kHz . The amplitude of the triangular waveform will decrease from 4.11 V to 2.94 V .
c No effect on the amplitude of the waveforms. The frequencies of both waveforms halve in value,
ie from 3.61 kHz to $1.80 \mathrm{kHz}\left(f \propto \frac{1}{\mathrm{R}_{3}}\right)$

## Example 8

Assume that the operational amplifier shown in Fig 3.23 saturates when the output reaches the $\pm 13 \mathrm{~V}$ levels.


Fig 3-23
a With $\mathrm{R}_{1}=\mathrm{R}_{2}=1.5 \mathrm{k}$ and $\mathrm{C}_{1}=\mathrm{C}_{2}=001 \mu \mathrm{~F}$
i confirm that the circuit is capable of oscillating with nominal value components as shown
ii check whether the circuit is capable of oscillating in all cases, if resistors are $\pm 5 \%$ and the capacitors are $\pm 10 \%$
iii determine the slew rate requirement for the operational amplifier if slew rate distortion is to be avoided. Assume nominal conditions as in (i).
b If $\mathrm{R}_{1}=20 \mathrm{k}$ and $\mathrm{R}_{2}=2 \mathrm{k}$ with $\mathrm{C}_{1}=2200 \mathrm{pF}$ and $\mathrm{C}_{2}=220 \mathrm{pF}$
$\mathbf{i}$ determine the necessary nominal gain of the amplifier if the circuit is to oscillate (Assume nominal loop gain is 1.1.)
ii determine suitable values for $\mathrm{R}_{3}$ and $\mathrm{R}_{4}$ if the circuit is to be bias current compensated (For the circuit to be bias current compensated: $\mathrm{R}_{2}=\mathrm{R}_{3} \| \mathrm{R}_{4}$.)
iii determine the nominal frequency of oscillation
iv what is the nominal slew rate requirement of the operational amplifier now?

## Solution

a i Loop gain is 1.11 so circuit should oscillate.
ii Loop gain can vary between 0.935 and 1.314 , so in some cases, circuit tolerances may combine to prevent circuit oscillation.
iii $S \geqslant 0.87 \mathrm{~V} / \mu \mathrm{s}$ necessary.
b i 12.21
ii $\mathrm{R}_{3}=24.4 \mathrm{k}, \mathrm{R}_{4}=2.18 \mathrm{k}$
iii $36 \cdot 2 \mathrm{kHz}$
iv $\mathrm{S} \geqslant 2.96 \mathrm{~V} / \mu \mathrm{s}$ necessary

## Chapter 4

POWER AMPLIFIERS
AND POWER SUPPLIES

### 4.1 Amplifier classification (introduction)

Power amplifiers are classified in accordance with the fraction of each cycle of a sinusoidal signal during which the active devices in the output stage are forward biased, ie passing collector current in the case of transistors.
Class A The active device(s) are forward biased throughout the entire period of each cycle of a sinusoidal signal. The signal increases the forward bias during one half of each cycle and decreases it during the other, but never reverse biases the stage.
Class B The active devices are reverse biased for one half of each sinusoidal signal cycle and are forward biased by the signal during the other half. Where the signal's instantaneous amplitude is of importance, as in audio amplifiers, two active devices are required - one to amplify positive going half cycles and the other to amplify negative going half cycles.
Class AB This is a classification for amplifiers operating between the A and $B$ classes, ie where the active devices are forward biased for less than the complete cycle, but for more than half of each cycle.
Class C In Class C operation the collector current will be zero for more than half the input signal cycle. The Class C amplifier has the highest efficiency, of the classes referred to, and is mainly used in radio frequency power amplifiers. It is especially useful where the signal is frequency modulated, but cannot be used to amplify amplitude modulated signals.

### 4.2 Ideal Class A direct-coupled stage

An 'ideal' amplifier output stage has: no losses due to transistors saturating, no losses due to electrical dissipation within transformers, and no losses due to the addition of extra components to the basic circuit for the purpose of overcoming problems such as transistor non-linearity and temperature dependence, etc.


Fig 4-1 Basic ideal Class A direct-coupled circuit and load line

When the circuit in Fig 4.1 is biased in Class A operation:
a The circuit is biased to give equal positive and negative output swings by making $V_{C E}$ at point $Q$ equal to $\frac{V_{C C}}{2}$.
b The optimum quiescent collector current value $=\frac{\mathrm{V}_{\mathrm{CC}}}{2 \mathrm{R}_{\mathrm{L}}}$.
C The transistor, $\mathrm{Q}_{1}$, must be capable of dissipating $2 \mathrm{P}_{o}$ (max) watts, where $P_{o}(\max )=\frac{\mathrm{V}_{C C}{ }^{2}}{8 \mathrm{R}_{\mathrm{L}}}$, is the maximum signal power output to the load $\mathrm{R}_{\mathrm{L}}$.
d The transistor must also be able to withstand $\mathrm{V}_{\mathrm{CC}}$ volts from collector to emitter and a peak collector current of $\frac{V_{C C}}{R_{L}}$ amperes.
e Output stage efficiency refers to the effectiveness of the output stage of a power amplifier in converting DC input power to the stage into useful signal output power to the load. It is the ratio of useful output power, $\mathrm{P}_{o}$, to DC input power, $\mathrm{P}_{\mathrm{CC}}$, expressed as a percentage. Efficiency $\eta=\frac{P_{o}}{P_{C C}} \times 100 \%$
f The maximum efficiency of such a stage is $25 \%$ and this occurs at $\mathrm{P}_{o}$ (max).
$g$ The low efficiency is due to the presence of a DC current component in the load. The DC power dissipation is entirely lost, contributing no useful output power component.
h In many cases, the DC current also produces other undesirable effects, especially in the case of electromagnetic loads such as speakers and motors, since the magnetic flux produced by the current may tend to saturate the magnetic circuitry.

### 4.3 Ideal Class A transformer-coupled output stage

The circuit shown in Fig 4.2 is biased to give equal positive and negative output swings by making the quiescent collector current, $\mathrm{I}_{\mathrm{CE}}$, such that $I_{C E}=\frac{V_{C C}}{R_{L}^{\prime}}$ where $R_{L}^{\prime}$ is the reflected load seen by the transistor and equals $n^{2} R_{L}$ where $n=$ transformer primary to secondary turns ratio, $n: 1$.



Fig 4-2 Basic ideal Class A transformer-coupled output stage and load line

The ideal circuit action is:
a The reflected collector load impedance, seen by the transistor, is $\mathrm{R}_{\mathrm{L}}^{\prime}$ $=\mathrm{n}^{2} \mathrm{R}_{\mathrm{L}}$.
b The optimum $Q$ point bias current is $I_{C E}=\frac{V_{C C}}{R_{L}^{\prime}}$
c The transistor must be capable of dissipating $2 \mathrm{P}_{o}(\max )$ watts, which occurs at zero input signal conditions, where $P_{o}(\max )=\frac{\mathrm{V}_{\mathrm{CC}}^{2}}{2 \mathrm{R}_{\mathrm{L}}^{\prime}}$ watts.
d The transistor must also be capable of withstanding $2 \mathrm{~V}_{\mathrm{CC}}$ volts from collector to emitter and a peak collector current of $\frac{2 \mathrm{~V}_{\mathrm{CC}}}{\mathrm{R}_{\mathrm{L}}^{\prime}}$ amperes.
e The maximum efficiency of the stage is $50 \%$ and this occurs at $\mathrm{P}_{o}(\max )$. Because the DC component of the collector current is isolated from the load efficiency is improved.
$f$ The only power dissipation in the load is due to the reflected signal component of the collector current.
$g$ The load $\mathrm{R}_{\mathrm{L}}$ must not be disconnected from the amplifier when the amplifier is operating, since the increased value of $R_{L}^{\prime}$ will cause $V_{C E}$ to greatly exceed $2 \mathrm{~V}_{\mathrm{CC}}$ volts.

### 4.4 Ideal Class B transformer-coupled output stage

The circuit shown in Fig 4.3 when functioning in Class B operation, acts as follows:
a The transistor is biased at cut off, ie the Q point is on the $\mathrm{V}_{\mathrm{CE}}$ axis.
b If the input signal is sinusoidal in nature, a current flows for only half of each cycle and is zero during each other half cycle.
C Class B is more efficient than Class A because there is no power dissipation in the transistor during one half of each input cycle. When Class B amplifiers are used to amplify amplitude modulated signals, eg in an audio amplifier, two active devices are employed, one to amplify positive-going half cycles and the other to amplify the negativegoing half cycles.


Fig 4-3 Ideal Class B transformer-coupled output stage and load line

A Class AB amplifier operates between Class A and Class B: operating the point lies between cut off and the centre of the load line.

### 4.5 Push-pull Class B power amplifier

If a Class B amplifier is to reproduce amplitude modulated waveforms correctly, a transformer-coupled, push-pull amplifier may be used. A typical circuit is shown in Fig 4.4.


Fig 4.4 Transformer-coupled push-pull amplifier
a In this case $V_{1}$ and $V_{2}$ are a matched pair of silicon transistors. Under quiescent conditions both are biased off, since both bases are held at ground potential via the secondary winding of transformer $T_{1}$.
b Transformer $\mathrm{T}_{1}$ splits the input signal (assumed sinusoidal, into two equal amplitude, antiphase signals to drive $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$. During positive half cycles of the signal at the base of $\mathrm{V}_{1}, \mathrm{~V}_{1}$ will conduct and $\mathrm{V}_{2}$ will be reverse biased, and vice-versa during negative half cycles.
c It should be noted that $i_{\mathrm{C}_{1}}$, and $i_{\mathrm{C}_{2}}$ flow in opposite directions through their halves of the primary of transformer $\mathrm{T}_{2}$, which results in the formation of a sinusoidal signal at the secondary of transformer $T_{2}$.
d Transformer $T_{2}$ not only acts to combine the signal from $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ into a sinusoidal signal at $\mathrm{R}_{\mathrm{L}}$, but also, if its turns-ratio is chosen correctly, optimises the reflected load resistance presented to $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ by maximising the power delivered to $\mathrm{R}_{\mathrm{L}}$. Note that the transformer $\mathrm{T}_{2}$ normally does not match the load to the transistors in the maximum power transfer sense, rather the match is one which takes into account the limited voltage, current and power dissipation capabilities of the transistors.
e Several important relationships may be shown in the ideal case where all losses due to saturation are neglected:
i $i_{\mathrm{CC}}=i_{\mathrm{C}_{1}}+i_{\mathrm{C}_{2}}$
ii $\quad R_{L}^{\prime}=\mathrm{n}^{2} \mathrm{R}_{\mathrm{L}}$
iii $i_{\mathrm{L}}=\frac{\mathrm{n}_{1}}{\mathrm{n}_{2}}\left(i_{\mathrm{C}_{1}}-i_{\mathrm{C}_{2}}\right)$
iv $\mathrm{P}_{\mathrm{CC}}=\frac{2 \mathrm{~V}_{\mathrm{CC}}^{2}}{\pi \mathrm{R}_{\mathrm{L}}^{\prime}}$ at $\mathrm{P}_{o}(\max )$ (See Section 4.26A for Proof.)
The respective waveforms are illustrated in Fig 4.5.


Fig 4-5 Waveforms for the push-pull amplifier circuit in Fig 4-4

### 4.6 Crossover distortion

The $\mathrm{V}_{\mathrm{BE}}, \mathrm{I}_{\mathrm{C}}$ characteristic of an npn transistor is shown in Fig 4.6. It may be seen that the relationship between $\mathrm{I}_{\mathrm{C}}$ and $\mathrm{V}_{\mathrm{BE}}$ becomes markedly nonlinear for $\mathrm{V}_{\mathrm{BE}}$ values below the knee. This results in distortion of the output signal called crossover distortion.


Fig 4-6 $\mathbf{V}_{\mathrm{BE}}, \mathrm{I}_{\mathbf{C}}$ characteristic of npn transistor
The effect of non-linearity is shown in Fig 4.7. The non-linearity is introduced when the forward biasing input signal, which is effective in producing the output signal, crosses over from one transistor to the other.
 bias changes over from


Fig 4.7 Illustration of the effect of crossover distortion

Clearly, if the input waveform signal is to be reproduced accurately in the output circuit, the crossover distortion must be considerably reduced. The basis of the usual method of minimising crossover distortion is as follows: a A small forward bias is applied to the base emitter junctions of $V_{1}$ and $\mathrm{V}_{2}$. This places the operating points of $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ more or less at the knee of their respective $\mathrm{V}_{\mathrm{BE}}, \mathrm{I}_{\mathrm{B}}$ characteristics.
b The $V_{B E}, I_{C}$ characteristics of the transistors $V_{1}$ and $V_{2}$ (Fig 4.4) now effectively become as shown in Fig 4.8.


Fig 4.8 $\mathbf{V}_{\mathbf{B E}}, \mathrm{I}_{\mathbf{C}}$ characteristic of forward biased npn transistors

A typical bias circuit is shown in Fig 4.9.
a Diode $V_{3}$ provides sufficient voltage drop to bias $V_{1}$ and $V_{2}$ to the knee of their input volt-ampere characteristic. Resistor R determines the diode's bias current.
b The diode also helps to stabilise the Q points against temperature variation, since its forward voltage drop, $\mathrm{V}_{\mathrm{D}}$, and the transistors' $\mathrm{V}_{\mathrm{BE}} \mathrm{S}$ decrease with temperature in the similar fashion necessary to maintain constant $\mathrm{I}_{\mathrm{C}}$.


Fig 4-9 Transformer-coupled push-pull amplifier with forward biasing

### 4.7 Transistor power relationships for ideal push-pull amplifier circuit

Let $\mathrm{P}_{o}(\max )=$ Maximum power output.
a The efficiency at $\mathrm{P}_{o}(\max )=78.5 \%$ (for proof see Section 4.26A). This implies that $78.5 \%$ of the supply power is converted into useful output power and $21.5 \%$ is dissipated in heating up the transistors, ie about $10.75 \%$ in each or about $\frac{\mathrm{P}_{o}(\max )}{7 \cdot 3}$ watts
b It might be thought that the transistors would dissipate most power in themselves at $\mathrm{P}_{o}(\max )$. This is not so. It can be shown that the transistors' average power dissipation is greatest when they are delivering approximately $40 \%$ of maximum power output to the load. At this point the efficiency is about $50 \%$ and the dissipation in each transistor is about $\frac{\mathrm{P}_{o}(\max )}{5}$
c The peak instantaneous power dissipation in the transistor is $\frac{\mathbf{P}_{o}(\max )}{2}$, but this is only of significance when operation occurs at low frequencies where the thermal time constant of the transistor is relatively short enough to allow the transistor to respond to the instantaneous power dissipation.

### 4.8 Disadvantages of a transformer as a phase splitter

a Distortion due to poor frequency response. The upper end of the frequency range is affected by the stray capacitance and inductance of the transformer. The lower end is affected by the primary self-inductance. The poor frequency response also produces considerable phase shift which makes the successful application of negative feedback difficult to achieve, because the feedback may turn out to be positive at some frequencies.
b The non-linear characteristic of the magnetic core material of the transformer.

### 4.9 Complementary symmetry amplifier

The push-pull circuit was originally a legacy from thermionic valve circuits, when only the 'npn type' valve, with conduction from plate to cathode, was
available. With the advance of transistor design, both npn and pnp type transistors with similar characteristics became available and these enabled the transformer to be eliminated by using the now familiar complementary symmetry circuits.


Fig 4-10 Basic circuit for a complementary symmetry amplifier
$R V_{1}$ sets the collector current of $V_{3}$ and so by varying the voltage drop across $R_{C}$ provides optimum bias at $X$ for $V_{1}$ and $V_{2} . V_{3}$ is a common emitter stage, providing voltage gain for the amplifier of about $-\frac{R_{B}}{R_{S}}$ due to the negative feedback provided by $\mathrm{R}_{\mathrm{B}}$. Readers should consult other appropriate texts for details of complementary symmetry amplifiers.

### 4.10 Development of a power amplifier using an operational amplifier

A development of a complementary symmetry amplifier could be a circuit as shown in Fig 4.11. The power output capability of the monolithic IC device is boosted by the addition of the complementary symmetry output stage composed of $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$.


Fig 4.11 Power amplifier utilising an operational amplifier voltage gain stage
a When $R_{1}=R_{2}$, the quiescent voltage at the inverting terminal of $N_{1}$ will be $\frac{\mathrm{V}_{\mathrm{CC}}}{2}$.
b 'Earthing' $\mathrm{R}_{3}$ via $\mathrm{C}_{2}$ rather than directly to ground provides two benefits:
$i$ The gain of the circuit at medium frequencies is $1+\frac{R_{4}}{R_{3}}$. This reduces in value at low frequencies, as the increasing reactance of $\mathrm{C}_{2}$ increases the impedance of the $\mathrm{R}_{3}$ branch of the circuit. This is useful in audio circuits where undesirable signals may be present at much lower frequencies than the desired signal.
ii At DC, the circuit from the non-inverting input of $\mathrm{N}_{1}$ to its output becomes a voltage follower due to $\mathrm{C}_{2}$ becoming an open circuit element. This forces the quiescent bias level at point $A$ to be $\frac{V_{\mathrm{CC}}}{2}$, thereby enabling maximum obtainable power output to be realisable when required.
C By moving the point $A$ connection of $R_{4}$ to point $B$, crossover distortion is considerably reduced since the source of the distortion is then placed within the feedback loop where it is reduced by the same factor that the other properties are improved by negative feedback.
Additional notes on biasing are given in Section 4.26B.

### 4.11 Bridge amplifiers

The power available from the various power amplifier circuits is proportioned to $\frac{\mathrm{V}_{\mathrm{CC}}^{2}}{\mathrm{R}_{\mathrm{L}}}$, hence any increase in output power is only possible by increasing $\mathrm{V}_{\mathrm{CC}}$ or decreasing $\mathrm{R}_{\mathrm{L}}$. Fig 4.12 represents two power amplifiers connected in bridge configuration. This arrangement provides a large increase in maximum output power capability over that available from a single amplifier, but with no increase in supply voltage or change in $\mathrm{R}_{\mathrm{L}}$. This is especially useful when the supply rail voltage has a fixed predetermined value, as in the case of automobile audio equipment.


Fig 4-12 Bridge amplifier

In this arrangement, two amplifiers with numerically equal voltage gains, $A_{V}$, are used with anti-phase outputs, ie one inverting and one non-inverting amplifier. If the same signal is applied to both amplifier inputs, the magnitude of the output signal across the load will be twice that obtainable for a single amplifier, providing the load, $\mathrm{R}_{\mathrm{L}}$, is connected between the two amplifier outputs.

Thus, if it is within the two amplifier capabilities, the power output will be four times that from a single amplifier.

## Example 1

In the bridge amplifier basic circuit diagram shown in Fig 4.13 it is assumed that points A and B are biased to a quiescent value of 20 V and that the power amplifiers $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ are operating ideally with no losses. Determine the efficiency of the bridge amplifier at (a) maximum power output, and at (b) 10 watts output. Assume that the integrated power amplifiers are ideal, ie they experience no losses due to saturation and both have a complementary symmetry output configuration.


Fig 4-13

## Solution

At maximum power output ( $\mathrm{P}_{\mathrm{o}}$ (max))
The maximum output signals at points A and B will be as shown in Fig 4.14.


Fig 4-14 Waveforms at $A$ and $B$ at $P_{o}$ (max)

The supply currents to $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ would be as shown in Fig 4.15.


Fig 4-15 $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ supply current waveforms at $\mathrm{P}_{\mathrm{O}}$ (max)

The power drawn from the supply by each amplifier would have an average value of: $40 \times \mathrm{I}_{\mathrm{av}} \mathrm{W}=40 \times \frac{2 \cdot 5}{\pi} \mathrm{~W}=\frac{100}{\pi} \mathrm{~W}\left(\right.$ where $\mathrm{I}_{\mathrm{Av}}=$ average supply current).
Hence, total supply power $=\frac{200}{\pi}$ watts for the two amplifiers.

$$
\text { The efficiency at } \begin{aligned}
\mathrm{P}_{o}(\max ) & =\frac{\mathrm{P}_{o}(\max )}{\text { total supply power }} \times 100 \% \\
& =\frac{50}{200 / \pi} \times 100 \%=78.5 \%
\end{aligned}
$$

## At 10 W power output

The load current (rms) value would be given by: $I_{(r m s)}^{2} R_{L}=P_{o}$ so $I_{(\mathrm{rms})}^{2} \times 16=10 . \quad I_{(\mathrm{rms})}=\sqrt{\frac{10}{16}}=0.79 \mathrm{~A}$
so $I_{(0-\mathrm{pk})}=0.79 \times \sqrt{ } 2=1.118 \mathrm{~A}$
Hence: $\mathrm{I}_{\mathrm{DC}_{(a v)}}=\frac{\mathrm{I}_{(0-\mathrm{pk})}}{\pi}=0.3559 \mathrm{~A}$
and $P_{C C}=V_{C C} \times I_{D C_{(m)}}=40 \times 0.3559 \times 2=28.46 \mathrm{~W}$
The efficiency $=\frac{10 \mathrm{~W}}{28 \cdot 46 \mathrm{~W}} \times 100 \%=35 \cdot 14 \%$

## Example 2

In the circuit diagram shown in Fig 4.16, the amplifiers ( $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ ) each have a gain of 26 dB . The respective outputs are automatically biased to $\left(\frac{\mathrm{V}_{\mathrm{CC}}}{2} \pm 1\right)$ volts and they saturate when their output voltages are within 2 volts of the supply rails.

Determine: (a) the variation in maximum output power due to the variation in output bias voltage settings, and (b) the range of output power available corresponding to variation of $\mathrm{R}_{v_{1}}$ if $\mathrm{v}_{s}=1$ volt (rms) and the bias voltages are both set to 9 V .


Fig 4-16

## Solution

a Maximum power, $\mathrm{P}_{o}(\max )$, capability without clipping will be attained when output bias setting is exactly 9 V for both amplifiers. Then, allowing for a total of 4 volts loss due to saturation voltages, the peak swing across the load will be $(18-4)=14 \mathrm{~V}$.
so $\mathrm{P}_{o}(\max )=\frac{\mathrm{V}_{\mathrm{rms}}^{2}}{\mathrm{R}_{\mathrm{L}}}=\frac{(14 / \sqrt{ } 2)^{2}}{8}=12.25 \mathrm{~W}$.
The minimum value of $\mathrm{P}_{o}(\max )$ will occur when at least one of the amplifier's bias voltages is at an extreme value, such as 8 or 10 volts. The maximum unclipped ( $0-\mathrm{pk}$ ) swing at the amplifier's output would then be limited to 6 volts (allowing for 2 volts saturation level). This would give a ( $0-\mathrm{pk}$ ) swing across the load of 12 volts maximum, without clipping.
Then minimum $\mathrm{P}_{o}(\max )=\frac{\mathrm{V}_{\mathrm{rms}}^{2}}{\mathrm{R}_{\mathrm{L}}}=\frac{(12 / \sqrt{ } 2)^{2}}{8}=9 \mathrm{~W}$
Hence variation in maximum output power is from 9 to $12 \cdot 25 \mathrm{~W}$ $=3.25 \mathrm{~W}$.
b $\mathrm{V}_{\text {in }}$ will vary from: $\left(\frac{22 \mathrm{k}}{82 \mathrm{k}+22 \mathrm{k}}\right) 1000 \mathrm{mV}_{(\mathrm{rms})}$ to zero V

$$
=211.5 \mathrm{mV} \text { to zero } \mathrm{V} .
$$

Hence, the rms signal at each amplifier output $=211.5 \mathrm{mV} \times$ voltage gain. Voltage gain of each amplifier, $\mathrm{A}_{v}$, is such that 20 $\log _{10} \mathrm{~A}_{v}=26 \mathrm{~dB}$
so $\log _{10} \mathrm{~A}_{v}=1 \cdot 3$, hence $\mathrm{A}_{v}=20$ times,
ie rms signal output from each amplifier $=211.5 \mathrm{mV} \times 20$ to zero

$$
\begin{aligned}
= & 4 \cdot 231 \text { volts }(\mathrm{rms}) \text { to } \\
& \text { zero }
\end{aligned}
$$

The ( $0-\mathrm{pk}$ ) equivalent of 4.231 volts (rms) $=5.983 \mathrm{~V}$.
This gives a $(0-\mathrm{pk})$ load voltage swing maximum of $2 \times 5.983=$ 11.97 V .

Hence, maximum output power would be: $\frac{(11.97 / \sqrt{ } 2)^{2}}{8}=8.95 \mathrm{~W}$
so range is from 8.95 W to zero.

### 4.12 Integrated circuit power amplifiers

The general design philosophy of integrated circuit power amplifiers is similar to that of discrete power amplifiers. It would therefore, at this stage, be worthwhile considering some important design factors in discrete power amplifiers.
a The input stages combine to give high voltage gain, whilst the output stage gives unity voltage gain, but high current and hence power gain.
b High maximum slew rate capabilities are required because of the large voltage swing requirements. Consider a 50 V (pk-pk) signal that is required at 18 kHz , then $\mathrm{S} \geqslant 2 \pi f \mathrm{~V}_{p}=2 \pi \times 18 \times 10^{3} \times 25 \mathrm{~V} / \mathrm{s}=$ $2 \cdot 83 \mathrm{~V} / \mu \mathrm{s}$ is necessary. The design factors needed for high slew rate to be achieved are beyond the level of this present text, however Section 4.13 examines a few important factors pertaining to discrete power output stages.

### 4.13 Discrete power output stage

Fig 4.17 represents a very much simplified discrete power output stage.


Fig 4.17 Sample discrete power output stage
a $\mathrm{R}_{\mathrm{V}_{1}}$ is used to adjust the base current of $\mathrm{V}_{1}$. This, in turn, varies the collector current of $V_{1}$ and the quiescent voltages at the bases of $V_{2}$ and $\mathrm{V}_{3}$. The overall result is that the voltage at point X is varied and adjusted to approximately $\frac{\mathrm{V}_{\mathrm{CC}}}{2}$ to obtain equal maximum positive and negative voltage swing capabilities across $R_{L}$. This ensures that the circuit is adjusted to a point such that maximum output power capability, without distortion due to clipping, is achieved.
b $\quad \mathrm{V}_{1}$ provides voltage gain, whilst $\mathrm{V}_{2}$ and $\mathrm{V}_{3}$ are emitter followers giving unity voltage gain but considerable current gain.

C $\mathrm{R}_{\mathrm{B}}$ and $\mathrm{R}_{\mathrm{V}_{1}}$ provide DC shunt feedback to stabilise the DC operating voltage at point X .
d $R_{B}$ and the driving source impedance $R_{S}$ provide feedback at signal frequencies to give a gain close to $-\frac{R_{B}}{R_{S}}$, in a similar way to the inverting amplifier circuit.
e The collector current of $V_{1}$, derived from the current source, causes a voltage drop across diodes $\mathrm{V}_{4}$ and $\mathrm{V}_{5}$ to provide the forward bias necessary to minimise crossover distortion in $\mathrm{V}_{2}$ and $\mathrm{V}_{3}$.
$f$ The current source itself, because of its high internal impedance, ensures that the voltage gain of $\mathrm{V}_{1}$ is quite large.

### 4.14 Bridge amplifier circuit incorporating IC power amplifiers



Fig 4-18 Bridge amplifier using integrated circuit power bridge amplifier incorporating IC power amplifiers
a The load $\mathrm{R}_{\mathrm{L}}$ is connected between the output of an inverting amplifier $\mathrm{N}_{2}$ and a non-inverting amplifier $\mathrm{N}_{1}$.
b The gains of the two amplifiers are made equal and stabilised by the feedback presented by $R_{2}, R_{3}$ and $R_{4}, R_{5}$.
c The gain of the inverting stage at signal is $-\frac{R_{4}}{R_{5}}$ while that of the non-inverting stage is $1+\frac{\mathrm{R}_{3}}{\mathrm{R}_{2}}$. Hence $1+\frac{\mathrm{R}_{3}}{\mathrm{R}_{2}}=\frac{\mathrm{R}_{4}}{\mathrm{R}_{5}}$ for equal gains.
d The terminal X provides a voltage which is equal to half the supply voltage. This is fed to $N_{1}$ via resistor $R_{1}$. The resistor $R_{1}$ serves to isolate the terminal X from the input signal to avoid loading effects. Since loading effects are not present in the case of the inverting amplifier, no isolating resistor is needed for the connection to the non-inverting input of $\mathrm{N}_{2}$.
e Resistors $R_{3}$ and $R_{4}$ combine with capacitors $C_{3}$ and $C_{1}$ to make $N_{1}$ and $\mathrm{N}_{2}$ function as DC voltage followers between their non-inverting inputs and outputs, forcing the quiescent voltages at outputs $Y$ and $Z$ to be at $\mathrm{V}_{\mathrm{X}}=\frac{\mathrm{V}^{+}}{2}$ supply volts.
$f$ Capacitor $\mathrm{C}_{4}$ acts to 'clean up' any unwanted signals that might be present on the bias line, while $\mathrm{C}_{5}$ performs the same function for the main supply rail.

### 4.15 Basic heat sink theory

a When electrical power is dissipated within a semiconductor device it is converted into heat.
b Since the semiconductor junction would initially have been at the same temperature as its immediate surroundings, the ambient temperature, the junction will increase its temperature above its surroundings to an extent determined by the electrical power dissipated and by its ability to lose heat to its surroundings.
c The term 'thermal resistance' is nothing more than an indication of how difficult it is for heat to pass through the material in question to some point at a lower temperature. The original electrical power dissipated is converted into thermal energy, which may be thought of as escaping to lower temperature surroundings in the form of a thermal current which obeys a thermal 'Ohm's law'.
d Thermal resistance $=\frac{\text { temperature drop }}{\text { power dissipated }}$ and so has the physical dimension of ${ }^{\circ} \mathrm{C} / \mathrm{W}$. This text uses the symbol $\theta_{a-b}$ for the thermal resistance between points $a$ and $b$ of a thermal circuit.
e Just as an electrical circuit may have resistances in series or in parallel, so may a thermal circuit. The resistance from semiconductor junction to ambient is the series combination of the thermal resistance from junction to case and case to ambient, ie $\theta_{j-a}=\theta_{j-c}+\theta_{c-a}$.
$f$ Often the junction of the device is not able to cool via the relevant thermal resistance path to its surroundings at a sufficient rate to prevent overheating occurring. It is then necessary to reduce this thermal resistance by using a heat sink.
g The heat sink must have a low thermal resistance between itself and the case, ie it must make good thermal contact with the device case. It must
also have a low thermal resistance between itself and the air surrounding the device. Therefore, the device is often bolted to a heat sink which has a large surface area in contact with the air.
h A matt black finish and suitably shaped fins give good radiation, conduction and convection characteristics from the heat sink to its surroundings.
i In extreme situations, forced air cooling by means of a fan may also be necessary.

### 4.16 Heat flow model



Fig 4-19 Mechanical diagram of a semiconductor device mounted on a heat sink

Most of the heat generated inside the device is transferred to the relatively heavy mounting base and then to the case, from which it is dissipated to the surroundings. In general, the case is not large enough to adequately dissipate the generated heat. Hence, the effective surface area must be increased by attaching a heat sink.

There are typically three stages to the heat transfer system of a semiconductor heat sink combination, each having its own thermal resistance to the next stage. The equivalent thermal diagram is shown in Fig 4.20.


Fig 4-20 Thermal resistances

A summary of the relationships existing in the thermal equivalent circuit is as follows:
a $\Delta \mathbf{T}=\mathbf{P} \theta_{j-a}$
where $\Delta \mathrm{T}=\mathrm{T}_{j}-\mathrm{T}_{a}=$ (Junction temperature - ambient temperature)
and $\quad \theta_{j-a}=$ Thermal resistance from junction to ambient in ${ }^{\circ} \mathrm{C} / \mathrm{W}$.
$P=$ power dissipated at device function in watts.
b $\quad \theta_{j-a}=\theta_{j-c}+\theta_{c-s}+\theta_{s-a}$
where $\theta_{j-c}=$ Thermal resistance from junction to case,
$\theta_{c-s}=$ Thermal resistance from case to heat sink, $\theta_{s-a}=$ Thermal resistance from heat sink to ambient.
C It should be noted that parallel thermal paths, such as that directly from case to ambient, normally have thermal resistances much higher than the alternative path via the heat sink and so can be neglected, ie $\theta_{c-a} \gg$ $\theta_{c-s}+\theta_{s-a}$

## Example 3

A power amplifier's output transistors, mounted on the same heat sink, dissipate a maximum of 40 watts each. The following information is supplied regarding the transistors:
a Operating temperature range $=-65^{\circ} \mathrm{C}$ to $+200^{\circ} \mathrm{C}$
b Thermal resistance, junction to case $=0.885^{\circ} \mathrm{C} / \mathrm{W}$
c Thermal resistance, case to heatsink $=0.33^{\circ} \mathrm{C} / \mathrm{W}$
Refer to Fig 4.21, and determine the maximum permissible thermal resistance of the heat sink for an ambient temperature of $35^{\circ} \mathrm{C}$


Fig 4-21

## Solution

Let $\mathrm{T}_{j} \max =$ maximum permissible junction temperature. The life expectancy and reliability of the device are dependent on this not being exceeded.
Then $\mathrm{T}_{a}+2 \mathrm{P} \theta_{s-a}+\mathrm{P}\left(\theta_{c-s}+\theta_{j-c}\right) \leqslant \mathrm{T}_{j}$ max ie $35+80 \theta_{s-a}+40(0.33+0.885) \leqslant 200$
$\theta_{s-a} \leqslant 1.455^{\circ} \mathrm{C} / \mathrm{W}$.

### 4.17 Introduction to regulators

A voltage regulator is intended to provide a constant (almost constant, in practice) voltage across a load in spite of variations in the supply voltage and in the load current requirements. The variations in the supply voltage may be variations in the level of the DC supply itself, such as would occur if the supply was derived from the AC mains source of fluctuating level, or could be an AC ripple on such a supply, or both types of variations could be present.

Line regulation is the change in output voltage, for a specified change in input voltage, usually expressed as a percentage.

Load regulation is the change in output voltage, for a specified change in load current, often expressed as a percentage.

### 4.18 Basic discrete series regulator circuit

Fig 4.22 represents a basic discrete series regulator circuit from which it can be seen that: $\mathrm{V}_{\mathrm{L}}=\mathrm{V}_{\mathrm{Z}}-\mathrm{V}_{\mathrm{BE}}$.


Fig 4-22 Basic discrete series regulator circuit
a It can be seen from $V_{L}=V_{Z}-V_{B E}$ that, should $V_{L}$ attempt to decrease, then $\mathrm{V}_{\mathrm{BE}}$ will, as a consequence, increase. ( $\mathrm{V}_{\mathrm{Z}}$ remains virtually constant). This will result in $I_{L}$ increasing, hence increasing $V_{L}$ in opposition to the original attempted change.
b This is a relatively insensitive circuit, since $I_{L}$ responds only to the direct comparison of $\mathrm{V}_{\mathrm{L}}$ with $\mathrm{V}_{\mathrm{Z}}$.
c In the more elaborate circuits used in high performance discrete regulators, the error signal $\left(\mathrm{V}_{\mathrm{L}}-\mathrm{V}_{\mathrm{Z}}\right)$ is amplified and used to control $V_{L}$.

### 4.19 Basic regulator with increased loop gain

In Fig 4.22 the zener diode $\mathrm{V}_{\mathrm{Z}}$ is the reference element which determines the stability of the output voltage. In Fig 4.23 a predetermined fraction of the output voltage is compared with $\mathrm{V}_{\mathrm{Z}}$. The fraction is governed by resistors $\mathrm{R}_{1}$ and $\mathrm{R}_{2}$.


Fig 4-23 Basic regulator with increased loop gain
a If the output voltage is such that $\left(\frac{R_{2}}{R_{1}+R_{2}}\right) V_{L}$ is greater than $V_{Z}$, then the error amplifier, $\mathrm{A}_{e}$, will have a negative error signal, $\mathrm{V}_{e}$, driving it.
This will cause the output of $\mathrm{A}_{e}$ to decrease the voltage applied to the series pass transistor, $\mathrm{V}_{1}$, which, by virtue of $\mathrm{V}_{1}$ being in common collector configuration, will cause $\mathrm{V}_{\mathrm{L}}$ to decrease. Conversely, $\mathrm{V}_{\mathrm{L}}$ will tend to increase if $\left(\frac{R_{2}}{R_{1}+R_{2}}\right) V_{L}$ is less than $V_{Z}$.
b This implies that any deviation from $\left(\frac{R_{2}}{R_{1}+R_{2}}\right) V_{L}$ equalling $V_{Z}$ will be opposed by the consequent changes in signal level at the base of $V_{1}$.
c In Fig 4.23 equilibrium will be reached when:
$V_{Z}=\left(\frac{R_{2}}{R_{1}+R_{2}}\right) V_{L}$.
One of the advantages of using the resistors $R_{1}$ and $R_{2}$ to divide the output voltage before comparing it with $\mathrm{V}_{\mathrm{Z}}$, is that $\mathrm{V}_{\mathrm{L}}$ is no longer directly dependent on $V_{Z}$, but can be adjusted to some required level or varied over a wide range of voltages subject to the overall condition that $\mathrm{V}_{\mathrm{L}}$ must be greater than $\mathrm{V}_{\mathrm{Z}}$.
If $\mathrm{V}_{\mathrm{Z}}$ is a 4.7 V zener diode, biased via R , and if $\mathrm{R}_{1}=10 \mathrm{k}$ and $\mathrm{R}_{2}=$ 4.7 k then $\mathrm{V}_{\mathrm{L}}$ may be determined as follows:
$\mathrm{V}_{\mathrm{L}}=\left(\frac{\mathrm{R}_{1}+\mathrm{R}_{2}}{\mathrm{R}_{2}}\right) \mathrm{V}_{\mathrm{Z}}$, ie $\mathrm{V}_{\mathrm{L}}=\left(\frac{14 \cdot 7}{4 \cdot 7}\right) 4 \cdot 7=14 \cdot 7$ volts
To obtain 14.7 volts from the basic regulator circuit shown in Figure 4.23 would require a 15.3 volt zener diode, or thereabouts. Since the closest standard value is 15 volts this would cause problems, especially if many regulators were to be constructed, as for a production run. If a potentiometer is incorporated in the divider chain, as in Fig 4.24, then the circuit could have its output adjusted to 14.7 volts for any specific zener diode of a type specified as having a zener voltage of $4 \cdot 7 \pm 10 \%$ volts, at the appropriate bias current level.


Fig 4-24 Regulator circuit with adjustable output voltage

## Example 4

The circuit shown in Fig 4.25 is a voltage regulator giving an output voltage of 15 volts.


Fig 4.25

$$
\begin{aligned}
& \text { Determine a the value of } R_{1}, \\
& \text { b } \text { the power dissipated in the series pass transistor } \\
& V_{1}, \\
& \text { for an unregulated input of } 24 \mathrm{~V} .
\end{aligned}
$$

## Solution

a $\quad V_{Z}=\left(\frac{R_{2}}{R_{1}+R_{2}}\right) V_{L}$ at equilibrium, ie $\frac{R_{1}+10 k}{10 k}=\frac{15}{10}$
so, $R_{1}=5 \mathrm{k}$.
b Power dissipated $=V_{C E} I_{C E}$

$$
\begin{aligned}
& =\left(\mathrm{V}_{\mathrm{S}}-\mathrm{V}_{\mathrm{L}}\right) \mathrm{I}_{\mathrm{L}}, \text { neglecting current in } \mathrm{R}_{1} \\
& =(24-15) 1 \cdot 5 \\
& =13 \cdot 5 \text { watts }
\end{aligned}
$$

### 4.20 Regulators producing output voltages lower than the internal reference element

In general, the regulators previously discussed inherently produce output voltages greater than $\mathrm{V}_{\text {ref }}$ since, with reference to Fig 4.23,
$\mathrm{V}_{\mathrm{L}}=\left(\frac{\mathrm{R}_{1}+\mathrm{R}_{2}}{\mathrm{R}_{2}}\right) \mathrm{V}_{\mathrm{Z}}=\left(1+\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\right) \mathrm{V}_{\mathrm{Z}}$.
To obtain voltages lower than $\mathrm{V}_{\mathrm{Z}}$ involves only a simple change to the circuit as shown in Fig 4.26.


Fig 4-26 Basic circuit for regulators producing output voltages lower than the internal reference element

The circuit shown in Fig 4.26 supplies a divided reference voltage to the non-inverting input of the error amplifier and has a direct connection from the output to the inverting input of that amplifier.

Equilibrium will now come about when:
$V_{L}=\left(\frac{R_{2}}{R_{1}+R_{2}}\right) V_{Z}$, ie when $V_{L}$ has a value determined by $\mathrm{R}_{1}, \mathrm{R}_{2}$ and $\mathrm{V}_{\mathrm{Z}}$ but is inherently $\leqslant \mathrm{V}_{\mathrm{Z}}$.

### 4.21 Pre-regulation

The output voltage of a regulator varies in a manner proportional to the voltage of the reference element. It follows that a precision regulator requires a highly stable reference element voltage. Referring to Fig 4.26, relevant details of circuit action are as follows:
a The variations in supply voltage produce significant variations in the voltage, $\mathrm{V}_{\mathrm{Z}}$, across the zener diode $\mathrm{V}_{2}$.
b The current in the zener diode, $V_{Z}$, is given by: $\frac{V_{S}-V_{Z}}{R}$, hence if $V_{S}$ varies from $\mathrm{V}_{\mathrm{S}_{1}}$ to $\mathrm{V}_{\mathrm{S}_{2}}$, the current in the diode will increase from $\frac{\mathrm{V}_{\mathrm{S}_{1}}-\mathrm{V}_{\mathrm{Z}}}{\mathrm{R}}$ to $\frac{\mathrm{V}_{\mathrm{S}_{2}}-\mathrm{V}_{\mathrm{Z}}}{\mathrm{R}}$; ie an increase of $\frac{\mathrm{V}_{\mathrm{S}_{2}}-\mathrm{V}_{\mathrm{S}_{1}}}{\mathrm{R}}$ amperes.
C It is assumed in (b) that the change in $\mathrm{V}_{\mathrm{Z}}$, although significant as far as its reference element properties are concerned, is small by comparison with changes in $\mathrm{V}_{\mathrm{S}}$.
d If the zener diode has an average dynamic resistance, $\mathrm{R}_{\mathrm{Z}}$, the change in $\mathrm{V}_{\mathrm{Z}}$ will be $\left(\frac{\mathrm{V}_{\mathrm{S}_{2}}-\mathrm{V}_{\mathrm{S}_{1}}}{\mathrm{R}}\right) \mathrm{R}_{\mathrm{Z}}$ volts.
e Let $\mathrm{V}_{\mathrm{S}_{1}}=18$ volts, $\mathrm{V}_{\mathrm{S}_{2}}=24$ volts and $\mathrm{V}_{\mathrm{Z}}$ is a 10 V zener diode with $\mathrm{R}_{\mathrm{Z}}$ $=8.5$ ohms. $\mathrm{R}=910$ ohms, giving a nominal bias current of 12 mA for $\mathrm{V}_{\mathrm{S}}=21 \mathrm{~V}$. The change in $\mathrm{V}_{\mathrm{Z}}$, due to changes in $\mathrm{V}_{\mathrm{S}}=\left(\frac{24-18}{910}\right) 8 \cdot 5$ $=56 \mathrm{mV}$, which is of considerable significance when designing a precision regulator.
The problem of variation in $\mathrm{V}_{\mathrm{Z}}$ with $\mathrm{V}_{\mathrm{S}}$ can largely be overcome by driving the reference element from a constant current source as shown in Fig 4.27.


Fig 4-27 Pre-regulation of reference element voltage
a The current biasing $\mathrm{V}_{3}$ is given by: $\frac{\mathrm{V}_{\mathrm{Z}_{1}}-\mathrm{V}_{\mathrm{BE}}}{\mathrm{R}_{2}}$.
b $\quad \mathrm{V}_{\mathrm{Z}_{1}}$ will vary slightly with $\mathrm{V}_{\mathrm{S}}$ and $\mathrm{V}_{\mathrm{BE}}$ will vary slightly with changes in $\mathrm{I}_{\mathrm{Z}_{2}}$. These small changes will only produce small variations in $\mathrm{I}_{\mathrm{Z}_{2}}$, and the subsequent changes in $\mathrm{V}_{\mathrm{Z}_{2}}$ will be much smaller than those without additional pre-regulator circuit.

### 4.22 Current limiting circuit



Fig 4-28 Current limiting circuit
a The current limiting circuit (Fig 4.28) consists of $\mathrm{V}_{2}$ and R .
b Neglecting the current flowing in $\mathrm{R}_{1}$ and $\mathrm{R}_{2}$ as being relatively much smaller, the load current, $I_{L}$, flows through $R$ and, if it increases to a value where $I_{L} R \simeq 0.65 \mathrm{~V}$, will forward bias transistor $V_{2}$.
C This will cause collector current $\mathrm{I}_{\mathrm{C}_{2}}$ to flow to the load via $\mathrm{V}_{2}$ instead of acting as part of the base current $\mathrm{I}_{\mathrm{B}_{1}}$ of $\mathrm{V}_{1}$.
d Clearly, every milliamp of current that flows as $\mathrm{I}_{\mathrm{B}_{1}}$ is converted to $\beta_{1}$ milliamps of load current by $V_{1}$, whereas if it is diverted via $V_{2}$ it only contributes 1 mA to the load current.
e Since the effect of introducing this circuitry is to limit the load current to a value only slightly more than the value that produces 065 volts drop across $R$, it is a current limiting circuit.
$f$ The connection from $R$ to the base of $V_{2}$ is traditionally called the current limit connection, CL, whilst the connection from the emitter of $\mathrm{V}_{2}$ to R is called the current sensing connection, CS .

### 4.23 Integrated circuit regulators

There are two basic types of integrated circuit regulators:
a The three terminal regulator which incorporates all the basic elements of regulators previously mentioned in this text, and usually a thermal overload circuit as well. They give a pre-determined output voltage.
b The type of regulator in which everything is incorporated, except the
actual voltage divider network, which establishes the regulated voltage, and the current limiting resistor.

### 4.24 Three terminal regulators

Fig 4.29 represents the basic concept of a three terminal regulator.


Fig 4-29 Basic connection diagram for a three terminal regulator

Three terminal regulators are usually mounted directly on the circuit board, and are normally used where the board is largely, or entirely, made up of circuitry operating from a standard three terminal regulator voltage such as $5 \mathrm{~V}, 12 \mathrm{~V}, 15 \mathrm{~V}$. Their use largely overcomes many of the interactive supply problems associated with the provision of one voltage level from a separate regulator to a number of boards requiring that voltage.

### 4.25 Integrated circuit series voltage regulator



Fig 4-30 Integrated circuit series voltage regulator

The circuit shown in Fig 4.30 does not show connections made for the purposes of preventing unwanted oscillation or for the production of negative output voltage regulators. Such connections are adequately described in manufacturers' literature.

Fig 4.31 shows a block diagram for a voltage regulator to give a regulated output voltage of about 5 V from an IC regulator with a nominal $\mathrm{V}_{\text {ref }}$ of $7 \cdot 15 \mathrm{~V}$.


Fig 4-31 Basic block diagram of a regulator to produce $\mathbf{V}_{\mathbf{L}}<\mathbf{V}_{\text {ref }}$ using an IC regulator device
a $\mathrm{R}_{1}$ and $\mathrm{R}_{2}$ represent the divider that feeds a reference voltage, derived from $\mathrm{V}_{\text {ref }}$, to the non-inverting input of the error amplifier.
b This voltage will be: $\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{2}}\right) \mathrm{V}_{\text {ref }}=\left(\frac{6 \cdot 8 \mathrm{k}}{3 \mathrm{k}+6 \cdot 8 \mathrm{k}}\right) 7 \cdot 15 \mathrm{~V}$, $=$ 4.96 V (nominal value, since $\mathrm{V}_{\text {ref }}$ can vary slightly from unit to unit).
c The regulated output voltage $\mathrm{V}_{\mathrm{L}}$ is fed to the inverting input of the error amplifier, so equilibrium will occur when $V_{L}=4.96$ volts.
d R is the current sensing resistor and, if it is given in the manufacturer's data that the base emitter voltage of the internal current sensing transistor is, say, 0.65 V , then current limiting will occur when:
$I_{L} R=0.65 \mathrm{~V}$, ie $I_{L}=\frac{0.65}{5} \mathrm{~A}=130 \mathrm{~mA}$.
This is, of course, higher than the actual load current which would be about: $\frac{5 \mathrm{~V}}{50 \Omega}=100 \mathrm{~mA}$.
e The unregulated input voltage $\mathrm{V}_{\mathrm{S}}$ is shown as varying between 12 and 18 V . In practice most integrated circuit regulators would be capable of handling values of $\mathrm{V}_{\mathrm{S}}$ down to about 8 V for a 5 V regulated output.

There must normally be a difference of at least 3 V between $\mathrm{V}_{\mathrm{S}}$ and $\mathrm{V}_{\mathrm{L}}$ to ensure that the series pass transistor does not go into saturation. It is essential that this differential voltage is maintained when there is ripple on the input supply line.

### 4.26 Important review points

A Proof of:
a $P_{C C}=\frac{2 \mathrm{~V}_{\mathrm{CC}}^{2}}{\pi \mathrm{R}_{2}}$ at $\mathrm{P}_{o}$ (max) (From Section 4.5.)
$b$ the efficiency of $\mathrm{P}_{o}(\max )=78.5 \% \quad$ (From Section 4.7.)


Fig 4-32 Transformer-coupled push-pull amplifier
a Average power from supply, $\mathrm{P}_{\mathrm{CC}}=\mathrm{V}_{\mathrm{CC}} \times \mathrm{I}_{\mathrm{DC}(\mathrm{av})}$ where $I_{D C(a v)}$ is the average supply current. The peak supply current when $\mathrm{P}_{o}$ (max) is being delivered to the load is $\frac{\mathrm{V}_{\mathrm{CC}}}{\mathrm{R}_{\mathrm{L}}^{\prime}}$, and since the supply current has the nature of a full wave rectified sinusoidal signal, its average value will be $\frac{2}{\pi} \frac{\mathrm{~V}_{\mathrm{CC}}}{\mathrm{R}_{\mathrm{L}}^{\prime}}$, so average supply power, $\mathrm{P}_{\mathrm{CC}(a v)}$ $=\mathrm{V}_{\mathrm{CC}} \times \frac{2 \mathrm{~V}_{\mathrm{CC}}}{\pi \mathrm{R}_{\mathrm{L}}^{\prime}}=\frac{2 \mathrm{~V}_{\mathrm{CC}}^{2}}{\pi \mathrm{R}_{\mathrm{L}}^{\prime}}$.
Notes: i At less than $P_{o}(\max ) \mathrm{P}_{\mathrm{CC}}$ equals $\frac{\mathrm{V}_{\mathrm{CC}} \times 2 \mathrm{~V}}{\pi \mathrm{R}_{\mathrm{L}}^{\prime}} \ldots$ (1) where V is the corresponding peak swing across each half of the primary of $T_{2}$; ii $P_{o}$ then equals $\frac{V^{2}}{2 R_{L}^{\prime}}$ watts. iii Efficiency, in general is: $\frac{\mathrm{V}^{2} / 2 \mathrm{R}_{\mathrm{L}}^{\prime}}{2 \mathrm{~V}_{\mathrm{CC}} \times \mathrm{V} / \pi \mathrm{R}_{\mathrm{L}}^{\prime}} \times 100 \%=\frac{25 \pi \mathrm{~V}}{\mathrm{~V}_{\mathrm{CC}}} \%$.
b The peak sinusoidal voltages swing across the load is $\mathrm{V}_{\mathrm{CC}}$, so:

$$
\mathrm{P}_{o}(\max )=\frac{\left(\mathrm{V}_{\mathrm{rms}}\right)^{2}}{\mathrm{R}_{\mathrm{L}}^{\prime}}=\frac{\left(\frac{\mathrm{V}_{\mathrm{CC}}}{\sqrt{2}}\right)^{2}}{\mathrm{R}_{\mathrm{L}}^{\prime}}=\frac{\mathrm{V}_{\mathrm{CC}}^{2}}{2 \mathrm{R}_{\mathrm{L}}^{\prime}}
$$

From (1): $\mathrm{P}_{\mathrm{CC}}=\frac{2 \mathrm{~V}_{\mathrm{CC}}^{2}}{\pi \mathrm{R}_{\mathrm{L}}^{\prime}}$ at $\mathrm{P}_{o}(\max )$

$$
\begin{aligned}
\text { so efficiency } & =\frac{\frac{\mathrm{V}_{\mathrm{CC}}^{2}}{2 \mathrm{R}_{\mathrm{L}}^{\prime}}}{\frac{2 \mathrm{~V}_{\mathrm{CC}}^{2}}{\pi \mathrm{R}_{\mathrm{L}}^{\prime}}}=\frac{\pi}{4} \times 100 \% \\
& =78.5 \% \text { at } \mathrm{P}_{o} \text { (max). }
\end{aligned}
$$

## B Notes on biasing for single supply operation

## From Section 4.10.

In order that maximum output voltage swing may be obtained, with sinusoidal operation, it is necessary to bias the op-amp output to $\frac{\mathrm{V}_{\mathrm{CC}}}{2}$ volts where $\mathrm{V}_{\mathrm{CC}}$ is the single bias rail voltage.


Fig 4-33 Single supply biasing arrangements

The arrangement in Fig 4.33 will accept sinusoidal input signals, amplify them 11 times at frequencies where the reactance of capacitors may be neglected, and produce a sinusoidal output voltage. $\mathrm{C}_{1}$ both prevents DC entering the signal source and also prevents the signal source shorting out the DC voltage across $\mathrm{R}_{\mathrm{B}} \cdot \mathrm{C}_{2}$ causes the circuit to act as a voltage follower at DC from non-inverting input to output since it does not allow DC to pass through $\mathbf{R}_{2}$. This means that feedback is via $R_{1}$ and $R_{X}$. Since ( + ) input is at 7.5 volts so must the ( - ) input and output also will be at 7.5 volts under quiescent conditions. $\mathrm{C}_{3}$ prevents the DC bias voltage at the output passing to the load so the actual output across $\mathrm{R}_{\mathrm{L}}$ is a sinusoidal signal symmetrical about zero volts.

## C Alternative biasing arrangement requiring one less capacitor

The circuit shown in Fig 4.34 has a gain of 11 at operational frequencies which falls to zero at DC. Since the gain from the + input to the amplifier output remains at 11 down to DC this means that any bias voltage present at the + input will also be amplified with this gain.

For the gain to stay at 11 down towards DC means that any bias voltage present at the $(+)$ input will also be amplified by the gain of 11 (Fig 4.34).


Fig 4-34 Alternative single supply arrangements

To obtain an output bias level of 7.5 V would require that the bias level at the $(+)$ input be lowered to $(7 \cdot 5 / 11)$ volts, ie 0.682 V . This means that: $\left(\frac{\mathrm{R}_{\mathrm{B}}}{\mathrm{R}_{\mathrm{A}}+\mathrm{R}_{\mathrm{B}}}\right) \mathrm{V}_{\mathrm{CC}}=0.682$; ie $\frac{\mathrm{R}_{\mathrm{B}}}{\mathrm{R}_{\mathrm{A}}+\mathrm{R}_{\mathrm{B}}}=\frac{0.682}{15}=0.0455$. hence $R_{A}=21 R_{B}$.
$R_{A}=1 \mathrm{M}$ and $\mathrm{R}_{\mathrm{B}}=47 \mathrm{k}$ would give a bias voltage of 0.673 V at $(+)$ input and 7.41 V at output. The input impedance of the circuit at operational frequencies would now be about 45 k instead of the previous 50 k (ie $\mathrm{R}_{\mathrm{A}} \| \mathrm{R}_{\mathrm{B}}$ ) refer to Fig 4.33. Providing $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ were large capacity capacitors, the frequency response would extend down towards zero Hz , eg for input and output breakpoint at 1 Hz , one would require:
$1 \mathrm{~Hz}=\frac{1}{2 \pi \mathrm{C}_{1}\left(\mathrm{R}_{\mathrm{A}} \| \mathrm{R}_{\mathrm{B}}\right)}$ hence $\mathrm{C}_{1}=3.55 \mu \mathrm{~F}$
$1 \mathrm{~Hz}=\frac{1}{2 \pi \mathrm{C}_{2} \mathrm{R}_{\mathrm{L}}} \quad$ so $\mathrm{C}_{2}=15.9 \mu \mathrm{~F}$.

### 4.27 Problems for readers

## Example 5

Fig 4.35 shows the essential elements of a bridge power amplifier driving an $8 \Omega$ load.


Fig 4-35
Each amplifier has a voltage gain of 30 times, has its output biased to 12 V , and saturates at the 22 V and 2 V output levels.
a Determine the value of $\mathrm{v}_{\mathrm{S}}(\mathrm{rms})$ if the power delivered to the load is 2 watts.
b Determine the maximum power that can be delivered to the load and the value of $\mathrm{v}_{\mathrm{S}}$ necessary to produce it.

## Solutions

a $\quad 66.7 \mathrm{mV}$ ( rms )
b 25 watts, 236 mV (rms)

## Example 6

In the circuit shown in Fig 4.36 it can be assumed that the capacitors have negligible reactance at operational frequencies.


Fig 4-36
a Determine the maximum power output that can be delivered to the load if the saturation voltages of $N_{1}, V_{1}$ and $V_{2}$ are neglected.
$b$ If $N_{1}$ saturates at the 2 V and 16 V levels, and $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ have collector-emitter saturation voltages of 1.5 volts, determine the maximum output power that can be delivered to $\mathrm{R}_{\mathrm{L}}$ if the base emitter voltage drops of $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ are neglected.
c What is the approximate value of $\mathrm{v}_{\mathrm{S}}$ (rms) necessary to obtain full output power under the condition of (b) above.

## Solutions

a 5.06 watts
b 3.06 watts
C 0.103 volts (rms)

## Chapter 5

## SELECTED <br> APPLICATIONS OF OPERATIONAL AMPLIFIERS

### 5.1 Introduction

Clearly, the operational amplifier is a popular and extremely useful device which has a very wide range of applications. Operational amplifiers are so versatile that their applications are limited only by the imagination of the circuit designer. Some uses of operational amplifiers are: alarm circuits, audio and electronic music circuits, automobile electronic circuits, basic building blocks in computers, many types of control circuits, analogue converters, digital work, medical electronics, displays, filters, video games, indicators, opto-electronics and photography, power supplies, switching/ timing devices, test and measurement. Readers will find examples of such circuits in appropriate electronic magazines.

Design engineers take into consideration such factors as offset voltage, CMMR and slew rate when selecting an operational amplifier for use in a particular circuit, and they must make considerable use of the manufacturers' data sheets.

In many non-critical applications a general purpose operational amplifier such as the 741 type is usually adequate. However, there are many applications for which high frequency gain, very high slew rate or low input offset voltage (or some other special requirement) will require a special type of operational amplifier to give the desired performance.

Brief explanations will be given in this chapter of some operational amplifier applications in the following areas:

- audio circuits
- precision rectifiers
- high impedance DC voltmeter
- medical electronics
- measurement of incident radiation using photodiode
- full wave ideal rectifier
- peak detector
- variable gain AC amplifier
- differential light intensity circuit
- filter applications
- linear read-out amplifier for resistive bridge circuit
- bass and treble tone control circuit
- scratch filter circuit
- switching power amplifier
- $\log$ converter circuit
- musical chiming circuit
- an R-S flip flop


### 5.2 Audio circuits

Pre-emphasis Many audio circuits require carefully determined frequency responses. Pre-emphasising, or boosting the signal source's high frequency signal components and de-emphasising or reducing the response of the signal processing circuitry, is often used to improve the overall signal to noise ratios of audio systems whilst still retaining an overall flat frequency response. Operational amplifiers are well suited to these applications because of their high gain and easily manipulated closed loop frequency response.
Filters Filters are often used to improve the overall quality, and once again effective use of operational amplifiers can be made.
Tone control Tone control of audio involves modifying the flat response to emphasise low and/or high frequencies dependent upon listener preference. Operational amplifier circuits are able to satisfy these requirements most effectively.
Balance and loudness control Balance and loudness controls also use operational amplifiers. Due to the non-linearity of the human hearing system, low frequencies must be boosted at low listening levels. Balance, ie varying the relative level of the left and right-hand channel of stereo systems, level and loudness controls provide all the necessary listening controls to produce the desired audio/music response. Once again operational amplifier closed loop responses are readily tailored to meet such requirements.

Details of audio circuits may be found in appropriate texts.

### 5.3 Precision rectifiers

The ideal semiconductor diode would have infinite resistance when its anode was more negative than its cathode, and zero resistance when forward biased. In practice there is a threshold, or knee, voltage of about 0.6 volts, for silicon diodes, before significant conduction occurs when forward biased. This is a serious problem, in the case of low level
applications of circuits such as rectifiers, clippers, clampers, AC voltmeters, rectangular to polar converters and peak detectors that utilize diodes. Fortunately operational amplifiers may be used in conjunction with the diodes to reduce the effective threshold voltage by a very large factor.

In the case of rectifier circuits the resulting circuits are termed either 'precision rectifiers' or 'absolute value circuits', depending on the application. Section 5.7 has details of a precision full wave rectifier circuit.

### 5.4 High impedance DC voltmeter

In Fig 5.1 the voltage to be measured, $\mathrm{V}_{1}$, is applied to the $(+)$ input terminal.


Fig 5-1 Basic high impedance DC voltmeter
a The meter current, $\mathrm{I}_{m}$, is set by $\mathrm{V}_{1}$ and $\mathrm{R}_{1}$.
b $V_{1}$ sees the very high impedance of the $(+)$ input. Since the $(+)$ input draws negligible current, it will not load the voltage being measured.
c The meter resistance has no effect on the meter current.
d If the full scale deflection current for the meter is $\mathrm{I}_{f s d}$, then to obtain full scale deflection requires $\mathrm{R}_{1}=\frac{\mathrm{V}_{1}}{\mathrm{I}_{f s d}}$.
e The actual input resistance seen by $\mathrm{V}_{1}$ is given by:
$\mathrm{R}_{i n}\left[\frac{\mathrm{~A}_{\mathrm{OL}}}{\mathrm{A}_{\mathrm{CL}}}\right]=\mathrm{R}_{i n}\left[\frac{\mathrm{~A}_{\mathrm{OL}}}{1+\frac{\mathrm{R}_{m}}{\mathrm{R}_{1}}}\right]$
where $\mathrm{R}_{\text {in }}$ is the input resistance of the operational amplifier and $\mathrm{A}_{\mathrm{OL}}$ its open loop gain.

## Example 1

A $50 \mu \mathrm{~A} f s d$ meter with internal resistance of 1 k is to be used in the circuit of a high impedance voltmeter intended to give full scale deflection when 1 volt is applied to it. Determine the voltmeter's input resistance and the value of $\mathrm{R}_{1}$. Assume the operational amplifier's open loop gain and input resistance are 100000 and $1 \mathrm{M} \Omega$ respectively.
For $f s d$ with 1 V , need $\mathrm{R}_{1}=\frac{1 \mathrm{~V}}{50 \mu \mathrm{~A}}=20 \mathrm{k}$ $\mathrm{R}_{\text {in }}$ seen by 1 V signal will be:
$1 \times 10^{6}\left[\frac{100000}{1+\frac{1000}{20000}}\right]=9.52 \times 10^{10} \Omega$

### 5.5 Application in medical electronic monitoring systems

Operational amplifiers are used effectively in many medical electronic monitoring systems. A common use (in the case of stroke patients) is monitoring the electromyogram (EMG) of the muscle.

When a muscle contracts, a very small voltage appears on the surface of the skin covering the muscle. The voltage waveform is called the EMG of the muscle. This EMG signal is usually less than 1 mV in amplitude and a differential amplifier with good common mode rejection ratio is required to amplify it to a useful amplitude, in isolation from the relatively noisy electronic environment. Such a function is appropriate to suitable operational amplifiers.


Fig 5-2 Circuit diagram for an audio EMG monitor
a Fig 5.2 represents a schematic circuit diagram for an audio EMG monitor.
b The input is obtained from the two electrodes taped to the skin over the muscles being examined. The differential amplifier circuit gain can be varied by adjusting $R_{1}$.
c $\mathrm{V}_{1}$ acts as a half wave rectifier by amplifying only half sections of the output from the operational amplifier. The bias of $\mathrm{V}_{1}$ is controlled by $\mathrm{R}_{2} . \mathrm{C}_{1}$ averages the rectified output of $\mathrm{V}_{1}$. Hence, the averaged amplified EMG signal controls the base current of $\mathrm{V}_{2}$.
d $V_{2}$ controls the charging current of $C_{2}$ and hence the oscillation frequency of the unijunction oscillator, $\mathrm{V}_{3}$, which in turn controls the pitch of the tone produced by the speaker.

### 5.6 Measurement of incident radiation using a photodiode

Fig 5.3 shows a photodiode in a circuit whereby the current I is converted into a voltage by the resistance, R .


Fig 5-3 Measurement of incident radiation using a photodiode
a The photodiode is reverse-biased by $\mathrm{V}_{\mathrm{B}}$.
b In darkness, the photodiode possesses a small leakage current which is usually only a few nanoamperes in magnitude.
C Light striking the diode will normally increase the current to perhaps $50 \mu \mathrm{~A}$ or more. This current bears a linear relationship to the incident radiation over many decades of irradiance.
d The current depends only on the light striking the photodiode and not on $\mathrm{V}_{\mathrm{B}}$, so the output voltage, $\mathrm{V}_{o}=-\mathrm{IR}$ is proportional to I and hence to the radiation incident upon the photodiode.

### 5.7 Full wave ideal rectifier



Fig 5-4 Full wave ideal rectifier
a Diodes $V_{1}$ and $V_{2}$ will start to conduct when the output of $\mathrm{N}_{1}$ reaches a (0-pk) amplitude of about 0.6 V , because they are connected back to the inverting input of $N_{1}$ via $R_{F A}$ and $R_{F B}$, and the inverting input will stay very close to ground potential due to the negative feedback.
b Assuming $N_{1}$ has an open loop gain of $200000 \mathrm{~V}_{1}$ and $\mathrm{V}_{2}$ will conduct when $\mathrm{v}_{\text {in }}$ reaches about $3 \mu \mathrm{~V}(0-\mathrm{pk})$. Before this level is reached, $\mathrm{N}_{1}$ is isolated from $\mathrm{N}_{2}$ and the output, $\mathrm{v}_{o}$, because $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ will be effectively open circuits to signals.
c There is no contribution to $v_{o}$ as a result of $v_{i n}$ being applied directly to $N_{2}$ via $R_{F A}$ and $R_{F B}$ (providing $R_{F A}=R_{F B}$ ), because $N_{2}$ and the resistors $R, R_{F A}$ and $R_{F B}$ will act as a differential amplifier with zero differential input signal.
d $\mathrm{V}_{1}$ conducts during negative half cycles of $\mathrm{v}_{\text {in }}$ and $\mathrm{V}_{2}$ conducts during positive half cycles when the amplitude of $v_{i n}$ exceeds $3 \mu \mathrm{~V}$. The current in $\mathrm{R}_{\mathrm{S}}=\frac{\mathrm{v}_{\mathrm{S}}}{\mathrm{R}_{\mathrm{S}}}$ because of the virtual earth at the ( - ) input. For practical purposes, all this current flows through either $\mathrm{R}_{\mathrm{FA}}$ or $\mathrm{R}_{\mathrm{FB}}$ depending upon which diode is conducting. It follows that the voltages at $X$ and $Y$ will be $-\left(\frac{R_{F}}{R_{S}}\right) v_{S}$, where $R_{F A}=R_{F B}=R_{F}$ with
$\mathrm{V}_{x}$ being made up of positive half cycles and $\mathrm{v}_{y}$ negative half cycles.
e The resistors R , and $\mathrm{N}_{2}$ act as a unity gain differential amplifier to $\mathrm{v}_{y}$ and $\mathrm{v}_{x}$, so that: $\mathrm{v}_{o}=\left(\mathrm{v}_{y}-\mathrm{v}_{x}\right)$.
f Since $\mathrm{v}_{y}$ consists of negative going half cycles and $\mathrm{v}_{x}$ of positive, $\mathrm{v}_{o}$ is made up entirely of negative going half cycles, as shown in Figure 5.4.
$g$ The output is a full wave rectified version of $\mathrm{v}_{\boldsymbol{S}}$, without the errors introduced by the forward voltage drops of the diodes, as for conventional full wave or bridge rectifier circuits. Only $3 \mu \mathrm{~V}$ of the signal $\mathrm{v}_{i n}$ is ineffective.

### 5.8 Peak detector



Fig 5-5 Peak detector

The peak detector is used in such areas as bar code readers and instrumentation circuits.
a A peak detector's output signal corresponds to the highest input voltage received during the period after the circuit has been reset.
b $\mathrm{N}_{1}$ acts as a voltage follower to positive input signals since $\mathrm{V}_{2}$ then conducts and acts as a negative feedback path.
c If $v_{\text {in }}$ exceeds the voltage on $\mathrm{C}_{1}$, then $\mathrm{V}_{1}$ will conduct and allow $\mathrm{C}_{1}$ to charge up to a voltage close to $\mathrm{v}_{i n}$. This voltage is transferred to $\mathrm{v}_{o}$ by $\mathrm{N}_{2}$, which is connected as a voltage follower. The combination of $\mathrm{N}_{1}$ and $\mathrm{N}_{2}$ is also forced to act as a voltage follower because of the presence of $\mathrm{R}_{\mathrm{F}}$.
d If $v_{i n}$ is less than the voltage on $C_{1}$, then $V_{1}$ will not be forced into conduction.
e If $V_{2}$ was not part of the circuit, then $N_{1}$ would act as an open-loop gain device when $\mathrm{v}_{\text {in }}$ was less than $\mathrm{v}_{o}$, and its output would be driven into saturation. There would then be a short period before the circuit could respond to any input voltage higher than that of $C_{1}$, because of the time taken to recover from the overdrive. $\mathrm{V}_{2}$ prevents such saturation occurring, however, since it conducts if $\mathrm{v}_{1}<\mathrm{v}_{o}$.
$f$ The high input impedance of $\mathrm{N}_{2}$ minimises the leakage from $\mathrm{C}_{1}$, but not entirely, so there is a limit to the period for which $\mathrm{v}_{o}$ can be considered as corresponding to the highest input voltage.
$g$ There is also a small reverse leakage via the reverse biased $\mathrm{V}_{1}$. It follows that $V_{1}$ should be chosen to have a low value of reverse leakage current.

### 5.9 Variable gain AC amplifier

Variable gain AC amplifiers are used in such areas as audio circuits and instrumentation circuits.


Fig 5-6 Variable gain AC amplifier
a $\quad \mathrm{R}_{\mathrm{V}}$ can be adjusted from zero to a maximum value of $\mathrm{R}_{2}$.
$b$ The voltage at the non-inverting input is $\left(\frac{R_{V}}{R_{V}+R_{1}}\right) v_{S}$, assuming $C$ as having negligible reactance at operational frequencies.
c The negative feedback connection via $R_{2}$ ensures that the voltage at the inverting input is effectively that at the non-inverting input, so that nodal analysis gives the relationship:
$\frac{\mathrm{v}_{\mathrm{S}}}{\mathrm{R}_{1}}+\frac{\mathrm{v}_{o}}{\mathrm{R}_{2}}=\left(\frac{\mathrm{R}_{\mathrm{V}}}{\mathrm{R}_{\mathrm{V}}+\mathrm{R}_{1}}\right) \mathrm{v}_{\mathrm{S}} \cdot\left(\frac{1}{\mathrm{R}_{1}}+\frac{1}{\mathrm{R}_{2}}\right)$

Then, if $\mathrm{R}_{\mathrm{V}}$ has its minimum value of zero, it can be shown that $\mathrm{v}_{o}=$ $-\left(\frac{R_{2}}{R_{1}}\right) v_{S}$
whereas if $\mathrm{R}_{\mathrm{V}}$ has its maximum value of $\mathrm{R}_{2}$, then it can be shown that $\mathrm{v}_{o}=$ zero,
so gain is adjustable over the range zero to $-\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}}$.
d The input resistance is given by: $\mathrm{R}_{1} \|\left(\mathrm{R}_{1}+\mathrm{R}_{\mathrm{V}}\right)$ so this varies from $\frac{\mathrm{R}_{1}}{2}$ to $R_{1} \|\left(R_{1}+R_{2}\right)$. Consequently, if the maximum design gain was 100 , the input resistance variation is from $0.5 \mathrm{R}_{1}$ to $\mathrm{R}_{1} \| 101 \mathrm{R}_{1}$, ie $0.99 \mathrm{R}_{1}$.

This is not a large variation, and for a low impedance source could be considered as more or less constant as far as its effect upon the circuit is concerned. For unity maximum gain the variation is from 0.5 to $0.67 \mathrm{R}_{1}$.

### 5.10 Differential light intensity circuit



Fig 5.7 Circuit which responds to differential light intensity
a Fig 5.7 illustrates a circuit that could be used to provide a signal to a relay to, say, switch off electric lighting when the outside light exceeded that inside the room.
b The resistive divider circuit can be used to cancel out the effect of input offset voltage, by applying an opposing signal to the amplifier input by adjustment of $\mathrm{RV}_{1}$.
c Since both ends of $R_{1}$ will ideally be at zero volts there will be no current in $\mathrm{R}_{1}$. Hence, the combined current for the two photoelectric cells will flow via $\mathrm{R}_{2}$, causing the amplifier output potential to be ( $\mathrm{i}_{1}-\mathrm{i}_{2}$ ) $\mathrm{R}_{2}$ volts.

### 5.11 Filter applications

Fig 5.8 represents an example of a low pass filter.


Fig 5-8 Low pass filter
a Operational amplifiers may be used to produce filters superior to those containing only passive elements.
b The main improvement is that the output impedance becomes very low, so that the load on the filter network has no effect upon its characteristics. High pass, low pass and band pass filters may be constructed.
c The circuit shown in Fig 5.7 has a -3 dB frequency of 1 kHz and is 40 dB down in its response at 10 kHz , and there is no transmission loss at low frequencies.
d If some gain is required at low frequencies, then the amplifier may be changed from a voltage follower to a non-inverting amplifier of the required gain.

### 5.12 Linear read-out amplifier for resistive bridge circuit

Fig 5.9 shows a linear readout for a resistive bridge. This type of circuit is used for matching resistor values in circuits similar to the Wheatstone bridge.


Fig 5-9 Linear readout amplifier for a resistive bridge circuit
a Assume that the resistor $\mathrm{R}_{x}$ is being checked to see whether it matches the resistor R .
b Let its value be $(1+\gamma)$ R. The voltage at the positive and negative inputs to the operational amplifier must effectively be equal, because of the negative feedback supplied by $\mathrm{R}_{x}$.
Hence: $\frac{\mathrm{E}}{2}=\frac{\mathrm{E}(1+\gamma) \mathrm{R}+e_{o} \mathrm{R}}{(1+\gamma) \mathrm{R}+\mathrm{R}}=\frac{\mathrm{E}(1+\gamma)+e_{o}}{2+\gamma}$.
Thus:

$$
(2+\gamma) \mathrm{E}=2 \mathrm{E}(1+\gamma)+2 e_{o}
$$

ie $\quad 2 \mathrm{E}+\gamma \mathrm{E}-2 \mathrm{E}-2 \mathrm{E} \gamma=2 e_{o}$
so,

$$
e_{o}=\mathrm{E}\left(-\frac{\gamma}{2}\right)
$$

Hence, $e_{o}$ is proportional to the fractional difference in resistance between the resistor under test and the standard.
c Thus, if $\mathrm{E}=10 \mathrm{~V}$ and $\mathrm{R}_{x}=110 \Omega$, while $\mathrm{R}=100 \Omega$.
Then, $\gamma=0.1$ and $e_{o}=-10 \mathrm{~V} \times \frac{0 \cdot 1}{2}=-0.5 \mathrm{~V}$.
When $\mathrm{R}_{x}=\mathrm{R}=100 \Omega$, then $e_{o}=0 \mathrm{~V}$. A table could be developed as follows:

| $\mathrm{R}_{x}(\Omega)$ | $\mathrm{R}(\Omega)$ | $\gamma$ | $e_{o}$ |
| :---: | :---: | :---: | :---: |
| 50 | 100 | $-0 \cdot 5$ | 2.5 |
| 80 | 100 | $-0 \cdot 2$ | $1 \cdot 0$ |
| 90 | 100 | $-0 \cdot 1$ | 0.5 |
| 100 | 100 | 0 | 0 |
| 110 | 100 | $+0 \cdot 1$ | -0.5 |
| 150 | +0.5 | -2.5 |  |

$e_{o}$ has units of $-50 \mathrm{mV} / \Omega$ error.

### 5.13 Miscellaneous circuit functions of operational amplifiers

The following circuit diagrams represent a few miscellaneous functions of operational amplifiers.

## - Bass and treble tone control circuit

The circuit shown in Fig 5.10 illustrates a bass and treble tone control circuit. The operational amplifier can be any type suitable for audio work.


Fig 5-10 Bass and treble tone control circuit

## - Scratch filter circuit

The circuit shown in Fig 5.11 illustrates a scratch filter circuit. The input must have a DC path to ground. $\mathrm{R}_{1}$ can vary from 10 k to 20 k and $\mathrm{C}_{1}$ should be about 1.5 nF . $f_{\mathrm{C}}$ will range from 5 kHz to 10 kHz .


Fig 5-11 Scratch filter circuit

## - Switching power amplifier

Fig 5.12 represents a switching power amplifier. Two 311 comparator integrated circuits may be used as the driver stage for class B amplifier. The output transistor ( 2 N 3763 ) only conducts when alternate input cycles exceed a small preset threshold voltage.


Fig 5-12 Switching power amplifier

## - Log converter circuit

Fig 5.13 represents a log converter. $v_{o}$ changes by 1 volt for every octave change in $i_{i n}$ current. The matched transistors can be BC 212L type.


Fig 5-13 Log converter circuit

## - Musical chiming circuit

Fig 5.14 shows a musical chiming circuit. It could be used to add a chime output to a percussion synthesiser. $\mathrm{V}_{o}$ 'rings' in response to a narrow pulse input. The amplitude of the damped oscillation peaks rapidly then decreases exponentially. Different tuning arrangements will produce varied output sounds.


Fig 5-14 Musical chiming circuit

## - R-S flip flop

Many logic systems operate in a series of steps. As memories, they hold data from one period in the sequence to another. The circuits for counters and frequency dividers are similar and often one circuit can be used for both purposes. An R-S flip flop (Reset-Set) circuit is shown in Fig 5.15.
Any operational amplifier may be used. $\mathrm{R}_{2}=24 \mathrm{R}_{1}$ and $\mathrm{R}_{2}<\frac{\mathrm{V}}{0 \cdot 05}$.


Fig 5-15 Operational amplifier R-S flip flop

### 5.14 Additional worked examples

## Example 2

In the circuit diagram shown in Fig 5.16 determine the following:
a The rms current in $\mathrm{R}_{1}$.
b The rms current in $\mathrm{R}_{\mathrm{L}}$ and its phase, relative to $\mathrm{v}_{s}$.
c The input resistance, designated as $\mathrm{r}_{\text {in }}$ on the circuit diagram.
d The amplifier output current, $i_{o}$, magnitude and direction.


Fig 5-16

## Solution

a The current in $R_{1}=\frac{v_{s}}{R_{1}}$, since inverting input may be treated as a virtual earth point because the non-inverting terminal is grounded.

$$
=\frac{0.25}{15 \mathrm{k}} \mathrm{~A}(\mathrm{rms})=16.7 \mu \mathrm{~A}(\mathrm{rms})
$$

b $\mathrm{v}_{o}=-\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}}\right) \mathrm{v}_{s}=-\left(\frac{330 \mathrm{k}}{15 \mathrm{k}}\right) 0 \cdot 25=-5 \cdot 5 \mathrm{~V}(\mathrm{rms})$
Current in $\mathrm{R}_{\mathrm{L}}=i_{\mathrm{L}}=\frac{\mathrm{v}_{o}}{\mathrm{R}_{\mathrm{L}}}=-\frac{5 \cdot 5}{10 \mathrm{k}} \mathrm{A}(\mathrm{rms})$
That is, $550 \mu \mathrm{~A}$ (rms) antiphase to $\mathrm{v}_{s}$.
c By Miller's Theorem (see a suitable text if you don't know this theorem):
$\mathrm{r}_{i n}=\frac{\mathrm{R}_{2}}{1-\mathrm{A}_{V}} \| \mathrm{R}_{i n}$.
(The effective answer is obtainable without use of Miller's Theorem.)

$$
\mathrm{A}_{V}=-\mathrm{A}_{d}
$$

Hence: $r_{\text {in }}=\frac{\mathrm{R}_{2}}{1+\mathrm{A}_{d}}\left\|\mathrm{R}_{\text {in }} \xlongequal{\sim} \frac{\mathrm{R}_{2}}{\mathrm{~A}_{d}}\right\| \mathrm{R}_{\text {in }}$
so $\quad r_{i n}=\frac{330 \mathrm{k}}{100000}\|1 \mathrm{M}=3.3 \Omega\| 1 \mathrm{M}$.
Hence: $r_{i n}=3.3 \Omega$ approximately
ie a low impedance to ground consistent with inverting input being a virtual earth point.
d Since current, $i_{2}$, in $\mathrm{R}_{2}$ is almost exactly equal to that in $\mathrm{R}_{1}$, it will be $16.7 \mu \mathrm{~A}$.

Hence, as can be seen in Fig 5.17 the amplifier output current $=i_{2}-i_{\mathrm{L}}$
$i_{o}=16.7 \mu \mathrm{~A}-(-550 \mu \mathrm{~A})$
so $i_{o}=567 \mu \mathrm{~A}$ (rms).


Fig 5-17

## Example 3

From Fig 5.18 determine the total voltage at points A, B and C, making reasonable practical approximations. Assume $C_{1}$ and $C_{2}$ have negligible reactance at 2 kHz .


Fig 5-18
Solution
Point A
$\mathrm{V}^{+}=+7.5 \mathrm{~V}$ due to the voltage divider $\mathrm{R}_{3}, \mathrm{R}_{4}$.
$=\mathrm{DC}$ voltage present at $(-)$ input terminal.

The AC signal at ( - ) input terminal will be negligibly small by comparison with $\mathrm{v}_{s}$.

Hence, total voltage at point A will be given by:
a The DC component is zero.
b The AC component, where the ( - ) input terminal may be treated as AC ground potential).
So AC component $=\left(\frac{\mathrm{R}_{1}}{\mathrm{R}_{1}+\mathrm{R}_{s}}\right) \mathrm{v}_{s}=\left(\frac{24 \mathrm{k}}{25 \mathrm{k}}\right) 100 \mathrm{mV}=96 \mathrm{mV}$ (rms)

## Point B

Total voltage at Point B will be given by:
a The AC component $=\frac{\mathrm{v}_{o}}{-\mathrm{A}_{d}}=\frac{-0 \cdot 48}{-200000}$
$=2.4 \mu \mathrm{~V}$ relative to ( + input) terminal (which is negligibly small compared with $\mathrm{v}_{s}$ ).
b The DC component will be +7.5 V .

## Point C

Total voltage at Point C will be given by:
a The AC output voltage, $\mathrm{v}_{o}=-\left(\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}+\mathrm{R}_{s}}\right) \mathrm{v}_{s}=-\left(\frac{120 \mathrm{k}}{25 \mathrm{k}}\right) 0 \cdot 1$

$$
=-0.48 \mathrm{~V}(\mathrm{rms})
$$

b The DC component $=+7 \cdot 5$ volts.

## Example 4

From Fig 5.19 determine the exact value of $\mathrm{v}_{o}$, allowing for effect of $\mathrm{R}_{\text {in }}$ and $\mathrm{A}_{d}$ being finite quantities.


Fig 5-19

## Solution

An appropriate equivalent circuit would be:


## Fig 5-20

Refer to Fig 5.20.
Signal voltage at point $A=\left(v_{s}-v_{d}\right)$
so, using nodal analysis:
$\frac{\mathrm{v}_{s}}{\mathrm{R}_{\text {in }}}+\frac{\mathrm{A}_{d} \mathrm{v}_{d}}{\mathrm{R}_{1}}+\frac{o}{\mathrm{R}_{2}}=\left(\mathrm{v}_{s}-\mathrm{v}_{d}\right)\left[\frac{1}{\mathrm{R}_{1}}+\frac{1}{\mathrm{R}_{2}}+\frac{1}{\mathrm{R}_{\text {in }}}\right]$
$=\frac{0.2}{10^{6}}+\frac{100000 \mathrm{v}_{d}}{9 \times 10^{3}}=\left(0.2-\mathrm{v}_{d}\right)\left[\frac{1}{9 \times 10^{3}}+\frac{1}{10^{3}}+\frac{1}{10^{6}}\right]$.
That is, $11.11222 \mathrm{v}_{d}=2.22222 \times 10^{-4}$
Hence: $v_{d}=1.9998 \times 10^{-5} \mathrm{~V}$
$\mathbf{v}_{o}=\mathrm{A}_{d} \mathbf{v}_{d}$
$=100000 \times 1.9998 \times 10^{-5}$
Hence: $\mathrm{v}_{o}=1.9998 \mathrm{~V}$ (rms)
In other words, very close to the expected value of 2.0 V .

## Example 5

The series pass transistor of a voltage regulator has the following thermal characteristics:
$\mathrm{T}_{\mathrm{J}}(\max )=200^{\circ} \mathrm{C}$
$\mathrm{P}_{\mathrm{D}}(\max )$ at $\mathrm{T}_{\mathrm{C}}=25^{\circ} \mathrm{C}=115 \mathrm{~W}$.
The regulator is intended to operate in a maximum ambient temperature of $60^{\circ} \mathrm{C}$. Its unregulated supply voltage can vary from 24 to 32 volts, whilst its output is adjustable over the range 10 to 18 volts. The load resistance may be any value from $8 \Omega$ to infinity.

The transistor requires a heat sink, which is to be attached to it via an electrical insulating washer with thermal resistance of $1.5^{\circ} \mathrm{C} / \mathrm{W}$. Determine the maximum permissible thermal resistance of the heat sink to ambient.

## Solution

Considering the transistor, it is evident that with 115 W dissipation at a case temperature of $25^{\circ} \mathrm{C}$, the junction temperature must just reach $200^{\circ} \mathrm{C}$.

Hence the thermal diagram is as shown in Fig 5.21.

```
So }\mp@subsup{\textrm{T}}{c}{}+\textrm{P}\mp@subsup{0}{j-c}{}=\mp@subsup{\textrm{T}}{j}{}(\mathrm{ max )
ie 25+115 自-c}=20
hence }\quad\mp@subsup{0}{j-c}{}=1.521\mp@subsup{7}{}{\circ}\textrm{C}/\textrm{W
```



Fig 5-21

The thermal diagram for the transistor-heat sink combination will be as shown in Fig 5.22.


Fig 5-22

Now the dissipation in the transistor is determined by $\mathrm{V}_{\mathrm{CE}} \mathrm{I}_{\mathrm{C}}$ and will be greatest for a supply voltage of 32 V and a load resistance of $8 \Omega$.
So $\mathrm{P}_{\mathrm{D}}(\max )=\left(32-\mathrm{V}_{\mathrm{L}}\right) \frac{\mathrm{V}_{\mathrm{L}}}{8} \mathrm{~W}$.
It should be evident from this relationship that if $\mathrm{V}_{\mathrm{L}}$ is reduced, $\mathrm{V}_{\mathrm{CE}}$ increases, but $I_{C}$ decreases. Hence, it is necessary to determine the value of $\mathrm{V}_{\mathrm{L}}$ which maximises $\mathrm{P}_{\mathrm{D}}$. There are two ways of doing this: by calculus, and graphically.
a The calculus approach involves determining when $\frac{\mathrm{dP}_{\mathrm{D}}}{\mathrm{dV}}=0$, ie when $\left[\left(32-\mathrm{V}_{\mathrm{L}}\right) \times \frac{1}{8}\right]+\left[(-1) \frac{\mathrm{V}_{\mathrm{L}}}{8}\right]=0$.
So $\mathrm{V}_{\mathrm{L}}=16 \mathrm{~V}$, which corresponds to a $\mathrm{P}_{\mathrm{D}}$ of 32 W .
b The graphical approach consists of plotting $P_{D}$ against $V_{L}$ and noting when $\mathrm{P}_{\mathrm{D}}$ has its maximum value.

A table showing $P_{D}$ values corresponding to various $V_{L}$ values is shown.

| $\mathrm{V}_{\mathrm{L}}(\mathrm{V})$ | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}_{\mathrm{D}}(\mathrm{W})$ | 27.5 | 28.875 | 30 | 30.875 | 31.5 | 31.875 | 32 | 31.875 | 31.5 |

It is obvious from these results that, if they were plotted, the peak value of $P_{D}$ occurs when $V_{L}$ is $16 \mathrm{~V} . \mathrm{P}_{\mathrm{D}}$ is then 32 W .

Considering the thermal diagram shown in Fig 5.22
$\mathrm{T}_{a}(\max )+\mathrm{P}_{\mathrm{D}}(\max )\left[\theta_{s-a}+\theta_{c-s}+\theta_{j-c}\right] \leqslant \mathrm{T}_{j}(\max )$
so $60+32\left[\theta_{s-a}+1 \cdot 5+1 \cdot 522\right] \leqslant 200$;
ie $\theta_{s-a} \leqslant 1.353^{\circ} \mathrm{C} / \mathrm{W}$ or $\theta_{s-a}(\max )=1.353^{\circ} \mathrm{C} / \mathrm{W}$.

## Example 6

An electrically ideal complementary symmetry amplifier has its two matched output transistors fixed to a common heat sink via electrical insulating washers with thermal resistance of $1.4^{\circ} \mathrm{C} / \mathrm{W}$. The transistor's maximum junction temperature is $200^{\circ} \mathrm{C}$ and their thermal resistance, junction to case, is $2.0^{\circ} \mathrm{C} / \mathrm{W}$. The circuit operates from a 75 volt supply rail and delivers its output power to a $10 \Omega$ load.

The heat sink has a thermal resistance of $3.5^{\circ} \mathrm{C} / \mathrm{W}$ and the amplifier is intended to operate in ambient temperatures up to $50^{\circ} \mathrm{C}$.
a Determine the maximum power output which the amplifier can deliver to the $10 \Omega$ load under maximum ambient temperature conditions.
b During manufacture, one amplifier has one of its output transistors incorrectly assembled to the heat sink, so that the thermal resistance from case to sink becomes $4^{\circ} \mathrm{C} / \mathrm{W}$ instead of $1.4^{\circ} \mathrm{C} / \mathrm{W}$. Determine the power output level at which the amplifier should theoretically suffer thermal failure.

## Solution

a $\mathrm{P}_{o}(\max )=\frac{\mathrm{V}_{(\mathrm{rms})}^{2}}{\mathrm{R}_{\mathrm{L}}}=\frac{\left[\left(\frac{75}{2}\right) \frac{1}{\sqrt{ } 2}\right]^{2}}{10}=70.31 \mathrm{~W}$
b The thermal diagram of the faulty amplifier is shown in Fig 5.23.


Fig 5-23

The incorrectly assembled transistor will suffer thermal failure first, when
$\mathrm{T}_{a}(\max )+\left(2 \mathrm{P}_{\mathrm{D}} \times \theta_{s-a}\right)+\mathrm{P}_{\mathrm{D}}\left(\theta_{c-s}+\theta_{j-c}\right)>200^{\circ} \mathrm{C}$
ie $50+\left(2 \mathrm{P}_{\mathrm{D}} \times 3.5\right)+\mathrm{P}_{\mathrm{D}}(4.0+2.0)>200$ ie $50+\left(2 \mathrm{P}_{\mathrm{D}} \times 3 \cdot 5\right)+\mathrm{P}_{\mathrm{D}}(4 \cdot 0+2 \cdot 0)>200$
$\mathrm{P}_{\mathrm{D}}>11.54 \mathrm{~W}$
Now $\mathrm{P}_{\mathrm{DC}(\text { av })}=\mathrm{P}_{o}+2 \mathrm{P}_{\mathrm{D}}$, ie $\mathrm{V}_{\mathrm{CC}} \times \mathrm{I}_{\mathrm{DC}(\mathrm{av})}=\mathrm{I}_{\text {rms }}^{2} \mathrm{R}_{\mathrm{L}}+2 \mathrm{P}_{\mathrm{D}}$
so $\mathrm{V}_{\mathrm{CC}}\left(\frac{\mathrm{I}_{(\mathrm{rms})} \sqrt{ } 2}{\pi}\right)=\left(\mathrm{I}_{\mathrm{rms}}^{2} \mathrm{R}_{\mathrm{L}}\right)+2 \mathrm{P}_{\mathrm{D}}$
so $I_{r m s}^{2} R_{L}-\frac{V_{C C} \sqrt{ } 2 I_{r m s}}{\pi}+2 P_{D}=0$
$10 I_{\text {rms }}^{2}-33.76 I_{\text {rms }}+23.07=0$
Solving this quadratic equation for $\mathrm{I}_{(\mathrm{rms})}$ gives values.
ie $I_{\text {rms }}=2.42$ or 0.952 A .
It then follows that $P_{o}$ must be $I_{r m s}^{2} R_{L}$,
ie 58.8 W or 9.06 W .

The transistor failure will occur at 9.06 watts output because this output level will be reached before 58.8 watts. However, why are there two answers? Do both in fact give the same transistor dissipation?

At $\mathrm{P}_{\mathrm{o}}=9.06 \mathrm{~W} \quad \mathrm{I}_{\mathrm{rms}}=0.952 \mathrm{~A}$.
The value of $P_{D C}$ will be $V_{C C I} I_{D C(a v)}$, ie $V_{C C} I_{r m s}\left(\frac{\sqrt{ } 2}{\pi}\right)=32 \cdot 1 \mathrm{~W}$ so $\mathrm{P}_{\mathrm{D}}=\frac{\mathrm{P}_{\mathrm{DC}}-\mathrm{P}_{o}}{2}=\frac{32.1-9.06}{2}=11.5 \mathrm{~W}$.

Similarly it can be shown that when $\mathrm{P}_{o}=58.7 \mathrm{~W} . \mathrm{P}_{\mathrm{D}}=11.5 \mathrm{~W}$. Hence, there is exactly the same dissipation in the transistors. It should also be noted that both values are otherwise acceptable because they are both power outputs which are less than $\mathrm{P}_{o}(\max )$ ie $<70 \cdot 3 \mathrm{~W}$.

## INDEX

$\mathrm{A}_{\mathrm{CL}}, 6,23,40,41$
adder circuit, 12
adjustable gain, 117, 118
amplifiers
bridge, $87,92,93$
classification, 76-9
complementary symmetry, 84, 85
differential, 25
gain, 25, 117, 118
integrator, 24
power, $76,85,86,90,91,92$
push-pull, 80-4
unity gain, $16,25,26$
voltage follower, 16, 25, 26
$\mathrm{A}_{\text {OL }}, 11,35,40,41$
astable multivibrator, 51
audio circuits, 111
$\mathrm{A}_{\mathrm{VO}}, 1$
bandwidth, $1,33,34,35,39,40$
base and treble tone control, 121
biasing arrangements, 106-08
bistable multivibrator, 51-3
bridge amplifier, 87

CMRR, 3, 4
common mode voltage gain, 3
crossover distortion, 82,83
current limiting circuit, 102
cut off frequency, 34

DC voltmeter, 112, 113
differential amplifier, 12
differential amplifier gain, 3
differential gain, 11
differential input signal, 3
differentiator, 15, 16
drift, 14
dual-in-line package, 20, 21

EMG monitor, 113, 114
error components
bias currents, 14
offset current, 14
offset voltage, 14
slew rate, 42-7
feedback, $5,21,11$
filter applications, 119
flip-flop multivibrator, 51
free-running multivibrator, 53, 54
frequency response, 33
gain
adjustable, 117, 118
common-mode voltage, 3
differential, 3
unity, 16, 25, 26
gain bandwidth product, 34
generators, see signal generators
heat sink, 93-5
high frequency cut off, 39-40

IC regulators, 96-104
ideal op amp characteristics, 1,6
input bias current, 14
input offset current, 14
input offset voltage, 14
input resistance, 1
input signal variation, 35
integrator, 14,15
internal frequency compensation, 33
inverting operational amplifier, 5-7
light intensity circuit, 118,119
load lines, 77-9
log converter circuit, 123
low cut off frequency, 34
monostable multivibrator, 51
meter resistance, 112,113
musical chiming circuit, 123
negative feedback, 5, 21, 22
nodal analysis, 28-30
offset current, 14
offset voltage, 14
one-shot multivibrator, 51
operational amplifier regulator, 96-104
operational amplifiers
advantages, 1,2
basic terminals, 2-5, 8
bias currents, 14
circuit symbols, 4
closed loop gain, 6, 23, 40, 41
differential input, 3
drift, 12
frequency compensation, 33
frequency response curves, 36-8, 48
gain-bandwidth product, 34
ideal, 1
input power, 35,36
inverting, 5-7
multivibrators, 53-8
non-inverting, 7-9
output power, 35,36
output resistance, $1,40,41$
packages, 20, 21
parameters, 11
power supply, 96-104
ramp generator, 58
sawtooth wave generator, 61,62
sine wave oscillator, 62-4
slew rate, 42-7
terminals, 20, 21
triangular wave generator, 59-61
unity gain bandwidth, 16, 25, 26
voltage follower, 16, 25, 26
oscillation, 47
packages, 20, 21
peak detectors, 116, 117
phase angle, 37, 63 .
phase shift, 48, 62,63
phase splitter, 84
photodiode, 114, 115
positive feedback, 47, 62-4
power amplifiers, $76,85,86,90-2$
power supply, 96-104
power transformer, 78-81
precision rectifier, 111, 112
pre-regulation, 100, 101
programmable unijunction transistor, 62
push-pull amplifier, 81-4
ramp generator, 58
rectifiers, $111,112,115$
regulated power supply, 96-104
resistive bridge, 120,121
rise time, $38,39,48,49$
roll off, 34
R-S flip flop, 124
sawtooth wave generator, 61,62
scratch filter circuit, 122
signal generators
astable, 51
bistable, 51-3
monostable, 51
one-shot, 51
ramp, 58
sine wave, 62-4
square wave, 51
Wien bridge, 65, 72, 73
slew rate, 42-7
summing amplifier, 12,13
superposition theorem, 26-8
switching power amplifier, 122
terminals, 20, 21
thermal protection, 93-5
three terminal regulators, 103
triangular wave generator, 59-61
unity gain bandwidth, 16, 25, 26
unregulated power supply, 96-104
unstable state, 53-8
upper cut off frequency, 39,40
variable gain, 117, 118
virtual ground, 12
voltage follower, 16, 25, 26
waveform generators, see signal generators
Wien bridge oscillator, 65, 72, 73
zener diode, 60, 61, 74, 96-101

